[3-5]

[3-6]

### **CHAPTER 3**

· Population mean, raw data

$$\mu = \frac{\sum X}{N}$$
 [3–1]

Sample mean, raw data

$$\overline{X} = \frac{\sum X}{n}$$
 [3-2]

· Weighted mean

$$\overline{X}_w = \frac{w_1 X_1 + w_2 X_2 + \dots + w_n X_n}{w_1 + w_2 + \dots + w_n}$$
 [3-3]

· Geometric mean

$$GM = \sqrt[n]{(X_1)(X_2)(X_3)\cdots(X_n)}$$
 [3-4]

· Geometric mean rate of increase

$$GM = \sqrt[n]{\frac{\text{Value at end of period}}{\text{Value at start of period}}} - 1$$

Range = Highest value - Lowest value

Mean deviation

$$MD = \frac{\sum |X - \overline{X}|}{n}$$
 [3-7]

Population variance

$$\sigma^2 = \frac{\Sigma (X - \mu)^2}{M}$$
 [3–8]

• Population standard deviation

$$\sigma = \sqrt{\frac{\Sigma (X - \mu)^2}{N}}$$
 [3–9]

· Sample variance (deviation)

$$s^2 = \frac{\sum (X - \overline{X})^2}{n - 1}$$
 [3–10]

Sample variance (direct)

$$s^{2} = \frac{\sum X^{2} - \frac{(\sum X)^{2}}{n}}{n-1}$$
 [3-11]

• Sample standard deviation (direct)

$$s = \sqrt{\frac{\sum X^2 - \frac{(\sum X)^2}{n}}{n-1}}$$
 [3-12]

Coefficient of variation

$$CV = \frac{s}{X}(100)$$
 [3–13]

· Coefficient of skewness

$$sk = \frac{3(\overline{X} - \text{median})}{s}$$
 [3–14]

· Location of percentile

$$L_{\rho} = (n+1)\frac{P}{100}$$
 [3–15]

Sample mean grouped data

$$\overline{X} = \frac{\Sigma fM}{n}$$

· Sample standard deviation, grouped data

$$s = \sqrt{\frac{\sum fM - \frac{(\sum fM)^2}{n}}{n-1}}$$
 [3-17]

#### **CHAPTER 4**

Special rule of addition

$$P(A \text{ or } B) = P(A) + P(B)$$
 [4-2]

Complement rule

$$P(A) = 1 - P(\sim A)$$
 [4-3]

General rule of addition

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$
 [4-4]

• Special rule of multiplication

$$P(A \text{ and } B) = P(A)P(B)$$
 [4-5]

• General rule of multiplication

$$P(A \text{ and } B) = P(A)P(B|A)$$
 [4-6]

• Number of permutations

$$_{n}P_{r} = \frac{n!}{(n-r)!}$$
 [4–8]

Number of combinations

$$_{n}C_{r} = \frac{n!}{r!(n-r)!}$$
 [4–9]

CHAPTER 5Mean of a probability distribution

$$\mu = \Sigma[xP(x)]$$
 [5–1]

• Variance of a probability distribution

$$\sigma^2 = \Sigma[(x - \mu)^2 P(x)]$$
 [5–2]

Binomial distribution

$$P(x) = {}_{n}C_{x} p^{x} (1 - p)^{n-x}$$
 [5–3]

· Mean of a binomial distribution

$$\mu = np ag{5-4}$$

· Variance of a binomial distribution

$$\sigma^2 = np (1 - p)$$
 [5–5]

· Hypergeometric probability distribution

$$P(x) = \frac{({}_{S}C_{x})({}_{N-S}C_{n-x})}{{}_{N}C_{n}}$$
 [5–6]

· Poisson probability distribution

$$P(x) = \frac{\mu^x e^{-\mu}}{x!}$$
 [5-7]

[3-16]

Standard normal value

$$z = \frac{X - \mu}{\sigma}$$
 [6-1]

### **CHAPTER 7**

• Standard error of mean

$$\sigma_{\overline{\chi}} = \frac{\sigma}{\sqrt{p}}$$
 [7–1]

• z-value, μ and σ known

$$z = \frac{\overline{X} - \mu}{\sigma / \sqrt{n}}$$
 [7-2]

• z-value, population shape and  $\sigma$  unknown

$$z = \frac{\overline{X} - \mu}{s/\sqrt{n}}$$
 [7–3]

### **CHAPTER 8**

• Confidence interval for  $\mu$ , n > 30

$$\overline{X} \pm z \frac{s}{\sqrt{n}}$$
 [8–1]

• Confidence interval for μ, σ unknown

$$\overline{X} \pm t \frac{s}{\sqrt{n}}$$
 [8–2]

• Confidence interval for proportion

$$\hat{\rho} \pm z \, \sigma_p$$
 where  $\sigma_p = \sqrt{\frac{p(1-p)}{n}}$  [8-4]

• Standard error of sample proportion

$$s_p = \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$
 [8-5]

· Confidence interval for population proportion

$$\hat{\rho} \pm z \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$
 [8-6]

· Sample size for estimating population mean

$$n = \left(\frac{zs}{E}\right)^2$$
 [8–9]

Sample size for population proportion

$$n = \hat{\rho}(1 - \hat{\rho})\left(\frac{z}{E}\right)^2$$
 [8–10]

### **CHAPTER 9**

· z distribution as a test statistic

$$z = \frac{\overline{X} - \mu}{\sigma / \sqrt{n}}$$
 [9-1]

z statistic, σ unknown

$$z = \frac{\overline{X} - \mu}{s / \sqrt{n}}$$
 [9-2]

· Test of hypothesis, one proportion

$$z = \frac{\hat{\rho} - \rho}{\sqrt{\frac{\rho(1-\rho)}{n}}}$$
 [9-4]

· One sample test of mean, small sample

$$t = \frac{\overline{X} - \mu}{s/\sqrt{n}}$$
 [9–5]

## **CHAPTER 10**

• Test statistic for difference between two large sample means

$$z = \frac{\overline{X}_1 - \overline{X}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$
 [10-2]

• Two-sample test of proportions

$$z = \frac{\hat{\rho}_1 - \hat{\rho}_2}{\sqrt{\frac{\rho_c(1 - \rho_c)}{n_1} + \frac{\rho_c(1 - \rho_c)}{n_2}}}$$
 [10-3]

Pooled proportion

$$\rho_c = \frac{X_1 + X_2}{n_1 + n_2}$$
 [10-4]

Pooled variance

$$s_p^2 = \frac{(n_1 - 1) s_1^2 + (n_2 - 1) s_2^2}{n_1 + n_2 - 2}$$
 [10-5]

• Two-sample test of means—small samples

$$t = \frac{\overline{X}_1 - \overline{X}_2}{\sqrt{s_p^2 \left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$$
 [10-6]

• Paired t test

$$t = \frac{\overline{d}}{s_d / \sqrt{n}}$$
 [10–7]

### **CHAPTER 11**

• Test for equal variance

$$F = \frac{S_1^2}{S_2^2}$$
 [11–1]

· Sum of squares, total

SS total = 
$$\Sigma X^2 - \frac{(\Sigma X)^2}{n}$$
 [11–2]

· Sum of squares, treatments

$$SST = \Sigma \left[ \frac{T_c^2}{n_c} \right] - \frac{(\Sigma X)^2}{n}$$
 [11–3]

· Sum of squares, error

$$SSE = SS \text{ total} - SST$$
 [11–4]

• Confidence interval for means

$$(\overline{X}_1 - \overline{X}_2) \pm t \sqrt{\mathsf{MSE}(\frac{1}{n_1} + \frac{1}{n_2})}$$
 [11-5]

# **CHAPTER 12**

• Coefficient of correlation

$$r = \frac{n(\Sigma XY) - (\Sigma X)(\Sigma Y)}{\sqrt{[n(\Sigma X^2) - (\Sigma X)^2][n(\Sigma Y^2) - (\Sigma Y)^2]}}$$
 [12-2]

• Correlation test of hypothesis

$$t = \frac{r\sqrt{n-2}}{\sqrt{1-r^2}}$$
 [12-3]

· Slope of a regression line

$$b = \frac{n(\Sigma XY) - (\Sigma X)(\Sigma Y)}{n(\Sigma X^2) - (\Sigma X)^2}$$
 [12-5]

• Intercept of a regression line

$$a = \frac{\sum Y}{n} - b \left( \frac{\sum X}{n} \right)$$
 [12-6]

· Standard error of estimate

$$s_{y imes x} = \sqrt{\frac{\sum Y^2 - a(\sum Y) - b(\sum XY)}{n - 2}}$$
 [12–8]

Confidence interval

When variables 
$$Y' \pm t(s_{y \cdot x}) \sqrt{\frac{1}{n} + \frac{(X - \overline{X})^2}{\sum X^2 - \frac{(\sum X)^2}{n}}}$$
 [12-9]

Prediction interval

$$Y' \pm t(s_{y \cdot x}) \sqrt{1 + \frac{1}{n} + \frac{(X - \overline{X})^2}{\sum X^2 - \frac{(\sum X)^2}{n}}}$$
 [12-10]

## **CHAPTER 13**

• Multiple regression equation

$$Y' = a + b_1 X_1 + b_2 X_2 + \cdots + b_k X_k$$
 [13–3]

Multiple standard error

$$s_{y \cdot 12 \cdot \cdot \cdot k} = \sqrt{\frac{\Sigma (Y - Y')^2}{n - (k + 1)}}$$
 [13-4]

• Coefficient of multiple determination

$$R^2 = \frac{\text{SSR}}{\text{SS total}}$$
 [13–5]

· Global test of hypothesis

$$F = \frac{SSR/k}{SSE/(n - (k + 1))}$$
 [13-6]

Testing for a particular regression coefficient

$$t = \frac{b_i - 0}{s_{b_i}}$$
 [13–7]

## **CHAPTER 14**

• Chi-square test statistic

$$\chi^2 = \Sigma \left[ \frac{(f_o - f_\theta)^2}{f_\theta} \right]$$
 [14–1]

· Expected frequency

$$f_{\rm e} = {{\rm (Row\ total)(Column\ total)} \over {\rm Grand\ total}}$$
 [14–2]