

LEVEL ONE

THIS IS HOW IT ALL STARTS

LEVEL ONE This Is How It All Starts	LEVEL TWO Tools for Evaluating Alternatives	LEVEL THREE Making Decisions on Real-World Projects	LEVEL FOUR Rounding Out the Study
Chapter 1 Foundations of Engineering Economy	Chapter 5 Present Worth Analysis	Chapter 11 Replacement and Retention Decisions	Chapter 14 Effects of Inflation
Chapter 2 Factors: How Time and Interest Affect Money	Chapter 6 Annual Worth Analysis	Chapter 12 Selection from Independent Projects under Budget Limitation	Chapter 15 Cost Estimation and Indirect Cost Allocation
Chapter 3 Combining Factors	Chapter 7 Rate of Return Analysis: Single Alternative	Chapter 13 Breakeven Analysis	Chapter 16 Depreciation Methods
Chapter 4 Nominal and Effective Interest Rates	Chapter 8 Rate of Return Analysis: Multiple Alternatives	Chapter 9 Benefit/Cost Analysis and Public Sector Economics	Chapter 17 After-Tax Economic Analysis
	Chapter 10 Making Choices: The Method, MARR, and Multiple Attributes		Chapter 18 Formalized Sensitivity Analysis and Expected Value Decisions
			Chapter 19 More on Variation and Decision Making under Risk

MASTER ①

The foundations of engineering economy are introduced in these four chapters. When you have completed level one, you will be able to understand and work problems that account for the *time value of money*, *cash flows* occurring at different times with different amounts, and *equivalence* at different interest rates. The techniques you master here form the basis of how an engineer in any discipline can take *economic value* into account in virtually any project environment.

The eight factors commonly used in all engineering economy computations are introduced and applied in this level. Combinations of these factors assist in moving monetary values forward and backward through time and at different interest rates. Also, after these four chapters, you should be comfortable with using many of the Excel spreadsheet functions to solve problems.



CHAPTER 1

Foundations of Engineering Economy

The need for engineering economy is primarily motivated by the work that engineers do in performing analysis, synthesizing, and coming to a conclusion as they work on projects of all sizes. In other words, engineering economy is at the heart of *making decisions*. These decisions involve the fundamental elements of *cash flows of money, time, and interest rates*. This chapter introduces the basic concepts and terminology necessary for an engineer to combine these three essential elements in organized, mathematically correct ways to solve problems that will lead to better decisions. Many of the terms common to economic decision making are introduced here and used in later chapters of the text. Icons in the margins serve as back and forward cross-references to more fundamental and additional material throughout the book.

The case study included after the end-of-chapter problems focuses on the development of engineering economy alternatives.

MASTER ①**LEARNING OBJECTIVES**

Purpose: Understand the fundamental concepts of engineering economy.

This chapter will help you:

- | | |
|---|--|
| <p>Questions</p> | 1. Understand the types of questions engineering economy can answer. |
| <p>Decision making</p> | 2. Determine the role of engineering economy in the decision-making process. |
| <p>Study approach</p> | 3. Identify what is needed to successfully perform an engineering economy study. |
| <p>Interest rate</p> | 4. Perform calculations about interest rates and rate of return. |
| <p>Equivalence</p> | 5. Understand what equivalence means in economic terms. |
| <p>Simple and compound interest</p> | 6. Calculate simple interest and compound interest for one or more interest periods. |
| <p>Symbols</p> | 7. Identify and use engineering economy terminology and symbols. |
| <p>Spreadsheet functions</p> | 8. Identify the Excel [®] spreadsheet functions commonly used to solve engineering economy problems. |
| <p>Minimum Attractive Rate of Return</p> | 9. Understand the meaning and use of Minimum Attractive Rate of Return (MARR). |
| <p>Cash flows</p> | 10. Understand cash flows, their estimation, and how to graphically represent them. |
| <p>Doubling time</p> | 11. Use the rule of 72 to estimate a compound interest rate or number of years for a present worth amount to double. |
| <p>Spreadsheets</p> | 12. Develop a spreadsheet that involves simple and compound interest, incorporating sensitivity analysis. |



1.1 WHY ENGINEERING ECONOMY IS IMPORTANT TO ENGINEERS (and other professionals)

Decisions made by engineers, managers, corporation presidents, and individuals are commonly the result of choosing one alternative over another. Decisions often reflect a person's educated choice of how to best invest funds, also called *capital*. The amount of capital is usually restricted, just as the cash available to an individual is usually limited. The decision of how to invest capital will invariably change the future, hopefully for the better; that is, it will be *value adding*. Engineers play a major role in capital investment decisions based on their analysis, synthesis, and design efforts. The factors considered in making the decision are a combination of economic and noneconomic factors. Additional factors may be intangible, such as convenience, goodwill, friendship, and others.

Fundamentally, engineering economy involves formulating, estimating, and evaluating the economic outcomes when alternatives to accomplish a defined purpose are available. Another way to define engineering economy is as a collection of mathematical techniques that simplify economic comparison.

For many corporations, especially larger ones, many of the projects and services are international in scope. They may be developed in one country for application in another. People and plants located in sites around the world routinely separate product design and manufacturing from each other, and from the customers who utilize the product. The approaches presented here are easily implemented in multinational settings or within a single country or location. Correct use of the techniques of engineering economy is especially important, since virtually any project—local, national, or international—will affect costs and/or revenues.

Some of the typical questions that can be addressed using the material in this book are posed below.

For Engineering Activities

- Should a new bonding technique be incorporated into the manufacture of automobile brake pads?
- If a computer-vision system replaces the human inspector in performing quality tests on an automobile welding line, will operating costs decrease over a time horizon of 5 years?
- Is it an economically wise decision to upgrade the composite material production center of an airplane factory in order to reduce costs by 20%?
- Should a highway bypass be constructed around a city of 25,000 people, or should the current roadway through the city be expanded?
- Will we make the required rate of return if we install the newly offered technology onto our medical laser manufacturing line?

For Public Sector Projects and Government Agencies

- How much new tax revenue does the city need to generate to pay for an upgrade to the electric distribution system?
- Do the benefits outweigh the costs of a bridge over the intracoastal waterway at this point?

MASTER 1

SECTION 1.2 Role of Engineering Economy in Decision Making

7

- Is it cost-effective for the state to cost-share with a contractor to construct a new toll road?
- Should the state university contract with a local community college to teach foundation-level undergraduate courses or have university faculty teach them?

For Individuals

- Should I pay off my credit card balance with borrowed money?
- What are graduate studies worth financially over my professional career?
- Are federal income tax deductions for my home mortgage a good deal, or should I accelerate my mortgage payments?
- Exactly what rate of return did we make on our stock investments?
- Should I buy or lease my next car, or keep the one I have now and pay off the loan?

EXAMPLE 1.1

Two lead engineers with a mechanical design company and a structural analysis firm work together often. They have decided that, due to their joint and frequent commercial airline travel around the region, they should evaluate the purchase of a plane co-owned by the two companies. What are some of the economics-based questions the engineers should answer as they evaluate the alternatives to (1) co-own a plane or (2) continue to fly commercially?

Solution

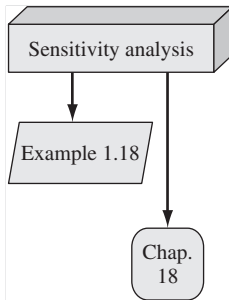
Some questions (and what is needed to respond) for each alternative are as follows:

- How much will it cost each year? (Cost estimates are needed.)
- How do we pay for it? (A financing plan is needed.)
- Are there tax advantages? (Tax law and tax rates are needed.)
- What is the basis for selecting an alternative? (A selection criterion is needed.)
- What is the expected rate of return? (Equations are needed.)
- What happens if we fly more or less than we estimate now? (Sensitivity analysis is needed.)

1.2 ROLE OF ENGINEERING ECONOMY IN DECISION MAKING

People make decisions; computers, mathematics, and other tools do not. The techniques and models of engineering economy *assist people in making decisions*. Since decisions affect what will be done, the time frame of engineering economy is primarily *the future*. Therefore, numbers used in an engineering economic analysis are *best estimates of what is expected to occur*. These estimates often involve the three essential elements mentioned earlier: cash flows, time of occurrence, and interest rates. These estimates are about the future, and will be somewhat different than what actually occurs, primarily because of changing circumstances and unplanned-for events. In other words, the *stochastic nature* of estimates will likely make the observed value in the future differ from the estimate made now.

Commonly, *sensitivity analysis* is performed during the engineering economic study to determine how the decision might change based on varying estimates,



especially those that may vary widely. For example, an engineer who expects initial software development costs to vary as much as $\pm 20\%$ from an estimated \$250,000 should perform the economic analysis for first-cost estimates of \$200,000, \$250,000, and \$300,000. Other uncertain estimates about the project can be “tweaked” using sensitivity analysis. (Sensitivity analysis is quite easy to perform using electronic spreadsheets. Tabular and graphical displays make analysis possible by simply changing the estimated values. The power of spreadsheets is used to advantage throughout this text and on the supporting website.)

Engineering economy can be used equally well to analyze outcomes of *the past*. Observed data are evaluated to determine if the outcomes have met or not met a specified criterion, such as a rate of return requirement. For example, suppose that 5 years ago, a United States–based engineering design company initiated a detailed-design service in Asia for automobile chassis. Now, the company president wants to know if the actual return on the investment has exceeded 15% per year.

There is an important procedure used to address the development and selection of alternatives. Commonly referred to as the *problem-solving approach* or the *decision-making process*, the steps in the approach follow.

1. **Understand the problem and define the objective.**
2. **Collect relevant information.**
3. **Define the feasible alternative solutions and make realistic estimates.**
4. **Identify the criteria for decision making using one or more attributes.**
5. **Evaluate each alternative, using sensitivity analysis to enhance the evaluation.**
6. **Select the best alternative.**
7. **Implement the solution and monitor the results.**

Engineering economy has a major role in all steps and is primary to steps 2 through 6. Steps 2 and 3 establish the alternatives and make the estimates for each one. Step 4 requires the analyst to identify attributes for alternative selection. This sets the stage for the technique to apply. Step 5 utilizes engineering economy models to complete the evaluation and perform any sensitivity analysis upon which a decision is based (step 6).

EXAMPLE 1.2

Reconsider the questions presented for the engineers in the previous example about co-owning an airplane. State some ways in which engineering economy contributes to decision making between the two alternatives.

Solution

Assume that the objective is the same for each engineer—available, reliable transportation that minimizes total cost. Use the steps above.

Steps 2 and 3: The framework for an engineering economy study assists in identifying what should be estimated or collected. For alternative 1 (buy the plane), estimate the purchase cost, financing method and interest rate, annual operating costs, possible

MASTER 1

SECTION 1.3

Performing an Engineering Economy Study

9

increase in annual sales revenue, and income tax deductions. For alternative 2 (fly commercial) estimate commercial transportation costs, number of trips, annual sales revenue, and other relevant data.

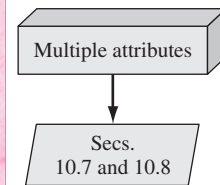
Step 4: The selection criterion is a numerically valued attribute called a *measure of worth*. Some measures of worth are

Present worth (PW)	Future worth (FW)	Payback period
Annual worth (AW)	Rate of return (ROR)	Economic value added
Benefit/cost ratio (B/C)	Capitalized cost (CC)	

When determining a measure of worth, the fact that money today is worth a different amount in the future is considered; that is, the *time value of money* is accounted for.

There are many noneconomic attributes—social, environmental, legal, political, personal, to name a few. This multiple-attribute environment may result in less reliance placed on the economic results in step 6. But this is exactly why the decision maker must have adequate information for all factors—economic and noneconomic—to make an informed selection. In our case, the economic analysis may favor the co-owned plane (alternative 1), but because of noneconomic factors, one or both engineers may select alternative 2.

Steps 5 and 6: The actual computations, sensitivity analysis, and alternative selection are accomplished here.



The concept of the *time value of money* was mentioned above. It is often said that money makes money. The statement is indeed true, for if we elect to invest money today, we inherently expect to have more money in the future. If a person or company borrows money today, by tomorrow more than the original loan principal will be owed. This fact is also explained by the time value of money.

The change in the amount of money over a given time period is called the *time value of money*; it is the most important concept in engineering economy.

1.3 PERFORMING AN ENGINEERING ECONOMY STUDY

Consider the terms *engineering economy*, *engineering economic analysis*, *economic decision making*, *capital allocation study*, *economic analysis*, and similar terms to be synonymous throughout this book. There is a general approach, called the *Engineering Economy Study Approach*, that provides an overview of the engineering economic study. It is outlined in Figure 1–1 for two alternatives. The decision-making process steps are keyed to the blocks in Figure 1–1.

Alternative Description The result of decision-making process step 1 is a basic understanding of what the problem requires for solution. There may initially be many alternatives, but only a few will be feasible and actually evaluated. If

alternatives *A, B, and C* have been identified for analysis, when method *D*, though not recognized as an alternative, is the most attractive, the wrong decision is certain to be made.

Alternatives are stand-alone options that involve a word description and best estimates of parameters, such as *first cost* (including purchase price, development, installation), *useful life*, *estimated annual incomes and expenses*, *salvage value* (resale or trade-in value), an *interest rate* (rate of return), and possibly *inflation* and *income tax effects*. Estimates of annual expenses are usually lumped together and called annual operating costs (AOC) or maintenance and operation (M&O) costs.

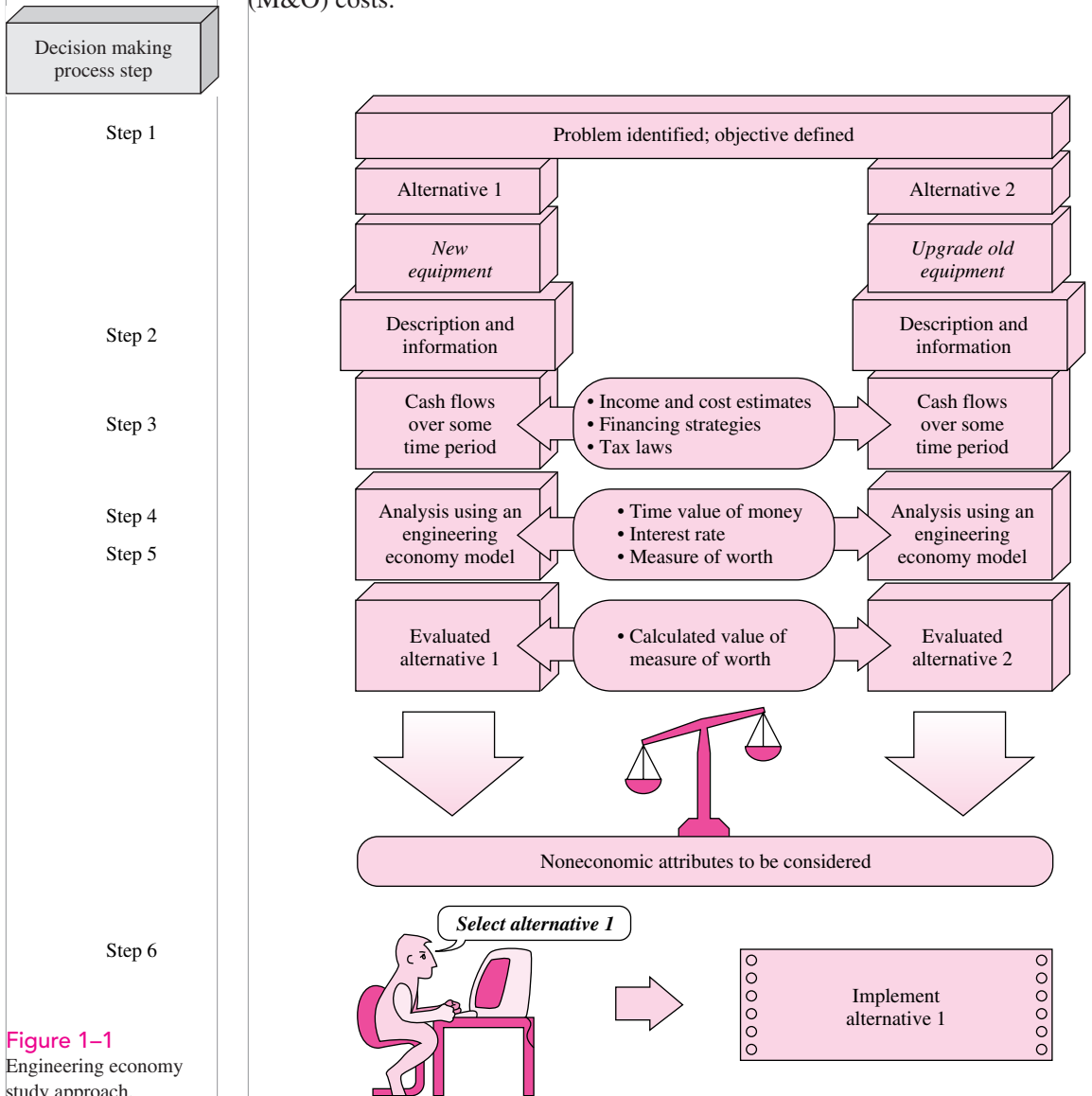


Figure 1-1
Engineering economy study approach.

MASTER ①

SECTION 1.3

Performing an Engineering Economy Study

11

Cash Flows The estimated inflows (revenues) and outflows (costs) of money are called cash flows. These estimates are made for each alternative (step 3). Without cash flow estimates over a stated time period, no engineering economy study can be conducted. Expected variation in cash flows indicates a real need for sensitivity analysis in step 5.

Analysis Using Engineering Economy Computations that consider the time value of money are performed on the cash flows of each alternative to obtain the measure of worth.

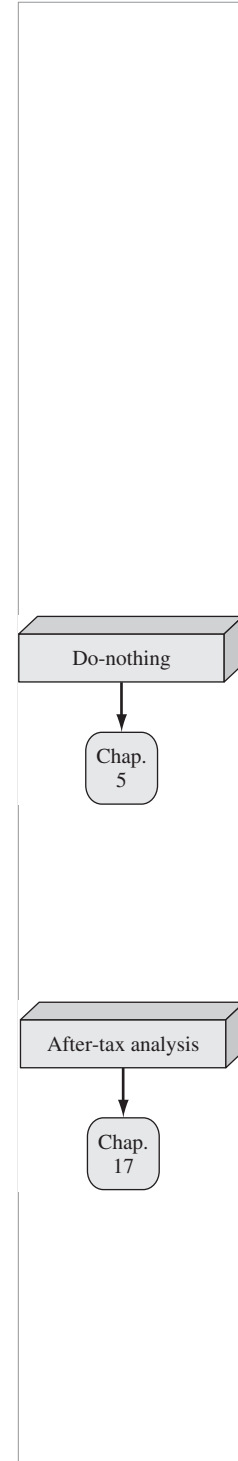
Alternative Selection The measure-of-worth values are compared, and an alternative is selected. This is the result of the engineering economy analysis. For example, the result of a rate-of-return analysis may be: Select alternative 1, where the rate of return is estimated at 18.4% per year, over alternative 2 with an expected 10% per year return. Some combination of economic criteria using the measure of worth, and the noneconomic and intangible factors, may be applied to help select one alternative.

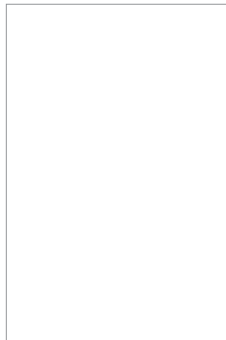
If only one feasible alternative is defined, a second is often present in the form of the *do-nothing alternative*. This is the *as-is* or *status quo* alternative. Do nothing can be selected if no alternative has a favorable measure of worth.

Whether we are aware of it or not, we use criteria every day to choose between alternatives. For example, when you drive to campus, you decide to take the “best” route. But how did you define *best*? Was the best route the safest, shortest, fastest, cheapest, most scenic, or what? Obviously, depending upon which criterion or combination of criteria is used to identify the best, a different route might be selected each time. In economic analysis, *financial units* (dollars or other currency) are generally used as the tangible basis for evaluation. Thus, when there are several ways of accomplishing a stated objective, the alternative with the lowest overall cost or highest overall net income is selected.

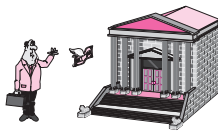
An *after-tax analysis* is performed during project evaluation, usually with only significant effects for asset depreciation and income taxes accounted for. Taxes imposed by local, state, federal, and international governments usually take the form of an income tax on revenues, value-added tax (VAT), import taxes, sales taxes, real estate taxes, and others. Taxes affect alternative estimates for cash flows; they tend to *improve* cash flow estimates for expenses, cost savings, and asset depreciation, while they *reduce* cash flow estimates for revenue and after-tax net income. This text delays the details of after-tax analysis until the fundamental tools and techniques of engineering economy are covered. Until then, it is assumed that all alternatives are taxed equally by prevailing tax laws. (If the effects of taxes must be considered earlier, it is recommended that Chapters 16 and 17 be covered after Chapter 6, 8 or 11.)

Now, we turn to some fundamentals of engineering economy that are applicable in the everyday life of engineering practice, as well as personal decision making.





Loan interest rate



Borrower

Bank

1.4 INTEREST RATE AND RATE OF RETURN

Interest is the manifestation of the time value of money. Computationally, interest is the difference between an ending amount of money and the beginning amount. If the difference is zero or negative, there is no interest. There are always two perspectives to an amount of interest—interest paid and interest earned. Interest is *paid* when a person or organization borrowed money (obtained a loan) and repays a larger amount. Interest is *earned* when a person or organization saved, invested, or lent money and obtains a return of a larger amount. It is shown below that the computations and numerical values are essentially the same for both perspectives, but there are different interpretations.

Interest paid on borrowed funds (a loan) is determined by using the relation

$$\text{Interest} = \text{amount owed now} - \text{original amount} \quad [1.1]$$

When interest paid over a *specific time unit* is expressed as a percentage of the original amount (principal), the result is called the *interest rate*.

$$\text{Interest rate (\%)} = \frac{\text{interest accrued per time unit}}{\text{original amount}} \times 100\% \quad [1.2]$$

The time unit of the rate is called the *interest period*. By far the most common interest period used to state an interest rate is 1 year. Shorter time periods can be used, such as, 1% per month. Thus, the interest period of the interest rate should always be included. If only the rate is stated, for example, 8.5%, a 1-year interest period is assumed.

EXAMPLE 1.3

An employee at LaserKinetics.com borrows \$10,000 on May 1 and must repay a total of \$10,700 exactly 1 year later. Determine the interest amount and the interest rate paid.

Solution

The perspective here is that of the borrower since \$10,700 repays a loan. Apply Equation [1.1] to determine the interest paid.

$$\text{Interest} = \$10,700 - 10,000 = \$700$$

Equation [1.2] determines the interest rate paid for 1 year.

$$\text{Percent interest rate} = \frac{\$700}{\$10,000} \times 100\% = 7\% \text{ per year}$$

EXAMPLE 1.4

Stereophonics, Inc., plans to borrow \$20,000 from a bank for 1 year at 9% interest for new recording equipment. (a) Compute the interest and the total amount due after 1 year. (b) Construct a column graph that shows the original loan amount and total amount due after 1 year used to compute the loan interest rate of 9% per year.

MASTER ①

SECTION 1.4

Interest Rate and Rate of Return

13

Solution

- (a) Compute the total interest accrued by solving Equation [1.2] for interest accrued.

$$\text{Interest} = \$20,000(0.09) = \$1,800$$

The total amount due is the sum of principal and interest.

$$\text{Total due} = \$20,000 + 1,800 = \$21,800$$

- (b) Figure 1–2 shows the values used in Equation [1.2]: \$1,800 interest, \$20,000 original loan principal, 1-year interest period.

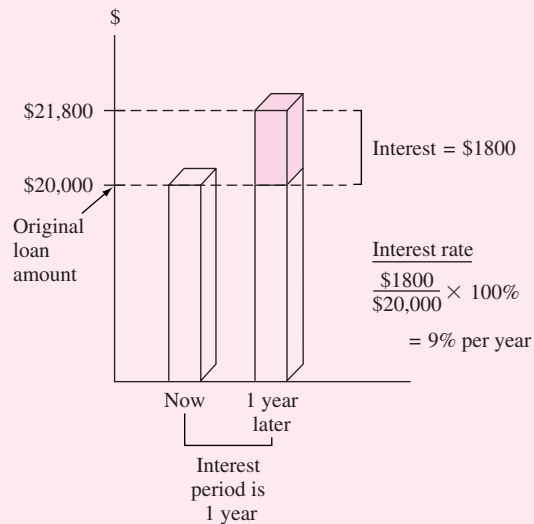


Figure 1–2

Values used to compute an interest rate of 9% per year, Example 1.4.

Comment

Note that in part (a), the total amount due may also be computed as

$$\text{Total due} = \text{principal}(1 + \text{interest rate}) = \$20,000(1.09) = \$21,800$$

Later we will use this method to determine future amounts for times longer than one interest period.

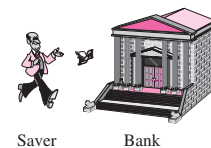
From the perspective of a saver, a lender, or an investor, interest earned is the final amount minus the initial amount, or principal.

$$\text{Interest earned} = \text{total amount now} - \text{original amount} \quad [1.3]$$

Interest earned over a specific period of time is expressed as a percentage of the original amount and is called *rate of return (ROR)*.

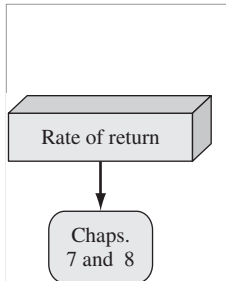
$$\text{Rate of return (\%)} = \frac{\text{interest accrued per time unit}}{\text{original amount}} \times 100\% \quad [1.4]$$

Investment rate of return



Saver

Bank



The time unit for rate of return is called the *interest period*, just as for the borrower's perspective. Again, the most common period is 1 year.

The term *return on investment (ROI)* is used equivalently with ROR in different industries and settings, especially where large capital funds are committed to engineering-oriented programs.

The numerical values in Equation [1.2] and Equation [1.4] are the same, but the term *interest rate paid* is more appropriate for the borrower's perspective, while the *rate of return earned* is better for the investor's perspective.

EXAMPLE 1.5

- (a) Calculate the amount deposited 1 year ago to have \$1000 now at an interest rate of 5% per year.
- (b) Calculate the amount of interest earned during this time period.

Solution

- (a) The total amount accrued (\$1000) is the sum of the original deposit and the earned interest. If X is the original deposit,

$$\text{Total accrued} = \text{original} + \text{original}(\text{interest rate})$$

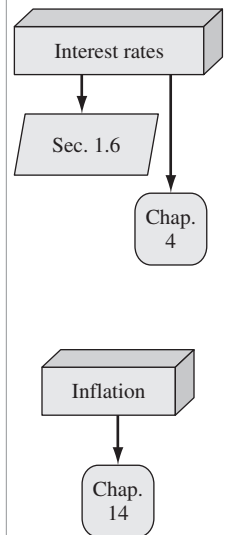
$$\$1000 = X + X(0.05) = X(1 + 0.05) = 1.05X$$

The original deposit is

$$X = \frac{1000}{1.05} = \$952.38$$

- (b) Apply Equation [1.3] to determine interest earned.

$$\text{Interest} = \$1000 - 952.38 = \$47.62$$



In Examples 1.3 to 1.5 the interest period was 1 year, and the interest amount was calculated at the end of one period. When more than one interest period is involved (e.g., if we wanted the amount of interest owed after 3 years in Example 1.4), it is necessary to state whether the interest is accrued on a *simple* or *compound* basis from one period to the next.

An additional economic consideration for any engineering economy study is *inflation*. Several comments about the fundamentals of inflation are warranted at this early stage. First, inflation represents a decrease in the value of a given currency. That is, \$1 now will not purchase the same number of apples (or most other things) as \$1 purchased 20 years ago. The changing value of the currency affects market interest rates. In simple terms, bank interest rates reflect two things: a so-called real rate of return *plus* the expected inflation rate. The real rate of return allows the investor to purchase more than he or she could have purchased before the investment. The safest investments (such as U.S. government bonds) typically have a 3% to 4% real rate of return built into their overall interest rates. Thus, an interest rate of, say, 9% per year on a U.S. government bond means that investors expect the inflation rate to be in the range of 5% to 6% per year. Clearly, then, inflation causes interest rates to rise.

From the borrower's perspective, the rate of inflation is simply another interest rate *tacked on to the real interest rate*. And, from the vantage point of the saver or investor in a fixed-interest account, inflation *reduces the real rate of return* on the investment. Inflation means that cost and revenue cash flow estimates increase over time. This increase is due to the changing value of money that is forced upon a country's currency by inflation, thus making a unit of currency (one dollar) worth less relative to its value at a previous time. We see the effect of inflation in that money purchases less now than it did at a previous time. Inflation contributes to

- A reduction in purchasing power of the currency.
- An increase in the CPI (consumer price index).
- An increase in the cost of equipment and its maintenance.
- An increase in the cost of salaried professionals and hourly employees.
- A reduction in the real rate of return on personal savings and certain corporate investments.

In other words, inflation can materially contribute to changes in corporate and personal economic analysis.

Commonly, engineering economy studies assume that inflation affects all estimated values equally. Accordingly, an interest rate or rate of return, such as 8% per year, is applied throughout the analysis without accounting for an additional inflation rate. However, if inflation were explicitly taken into account, and it was reducing the value of money at, say, an average of 4% per year, it would be necessary to perform the economic analysis using an inflated interest rate of 12.32% per year. (The relevant relations are derived in Chapter 14.) On the other hand, if the stated ROR on an investment is 8% with inflation included, the same inflation rate of 4% per year results in a real rate of return of only 3.85% per year!

1.5 EQUIVALENCE

Equivalent terms are used very often in the transfer from one scale to another. Some common equivalencies or conversions are as follows:

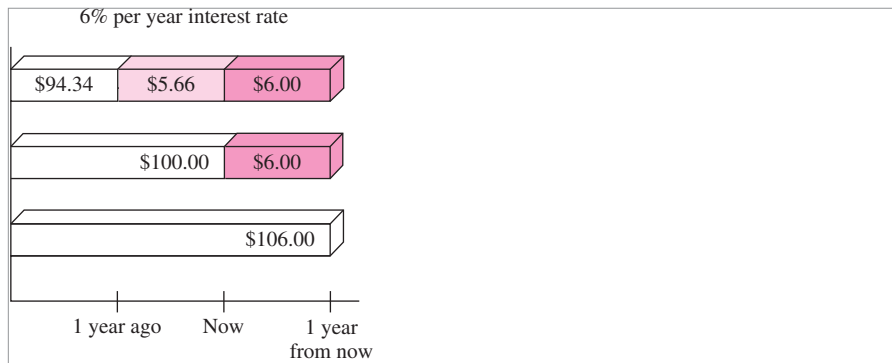
Length: 100 centimeters = 1 meter 1000 meters = 1 kilometer
 12 inches = 1 foot 3 feet = 1 yard 39.370 inches = 1 meter

Pressure: 1 atmosphere = 1 newton/meter²
 1 atmosphere = 10³ pascal = 1 kilopascal

Many equivalent measures are a combination of two or more scales. For example, 110 kilometers per hour (kph) is equivalent to 68 miles per hour (mph) or 1.133 miles per minute, based on the equivalence that 1 mile = 1.6093 kilometers and 1 hour = 60 minutes. We can further conclude that driving at approximately 68 mph for 2 hours is equivalent to traveling a total of about 220 kilometers, or 136 miles. Three scales—time in hours, length in miles, and length in kilometers—are combined to develop equivalent statements. An additional use of these equivalencies is to estimate driving time in hours between two cities using two maps, one indicating distance in miles, a second showing kilometers. Note that throughout these statements the fundamental relation 1 mile = 1.6093 kilometers is used. If this relation changes, then the other equivalencies are in error.

Figure 1-3

Equivalence of three amounts at a 6% per year interest rate.



When considered together, the time value of money and the interest rate help develop the concept of *economic equivalence*, which means that different sums of money at different times may be equal in economic value. For example, if the interest rate is 6% per year, \$100 today (present time) is equivalent to \$106 one year from today.

$$\text{Amount accrued} = 100 + 100(0.06) = 100(1 + 0.06) = \$106$$

So, if someone offered you a gift of \$100 today or \$106 one year from today, it would make no difference which offer you accepted. In either case you have \$106 one year from today. However, the two sums of money are equivalent to each other *only* when the interest rate is 6% per year. At a higher or lower interest rate, \$100 today is not equivalent to \$106 one year from today.

In addition to future equivalence, we can apply the same logic to determine equivalence for previous years. A total of \$100 now is equivalent to $\$100/1.06 = \94.34 one year ago at an interest rate of 6% per year. From these illustrations, we can state the following: \$94.34 last year, \$100 now, and \$106 one year from now are equivalent at an interest rate of 6% per year. The fact that these sums are equivalent can be verified by computing the two interest rates for 1-year interest periods.

$$\frac{\$6}{\$100} \times 100\% = 6\% \text{ per year}$$

and

$$\frac{\$5.66}{\$94.34} \times 100\% = 6\% \text{ per year}$$

Figure 1-3 indicates the amount of interest each year necessary to make these three different amounts equivalent at 6% per year.

EXAMPLE 1.6

AC-Delco makes auto batteries available to General Motors dealers through privately owned distributorships. In general, batteries are stored throughout the year, and a 5% cost increase is added each year to cover the inventory carrying charge for the distributorship owner. Assume you own the City Center Delco facility. Make the calculations

MASTER 1

necessary to show which of the following statements are true and which are false about battery costs.

- (a) The amount of \$98 now is equivalent to a cost of \$105.60 one year from now.
- (b) A truck battery cost of \$200 one year ago is equivalent to \$205 now.
- (c) A \$38 cost now is equivalent to \$39.90 one year from now.
- (d) A \$3000 cost now is equivalent to \$2887.14 one year ago.
- (e) The carrying charge accumulated in 1 year on an investment of \$2000 worth of batteries is \$100.

Solution

- (a) Total amount accrued = $98(1.05) = \$102.90 \neq \105.60 ; therefore, it is false. Another way to solve this is as follows: Required original cost is $105.60/1.05 = \$100.57 \neq \98 .
- (b) Required old cost is $205.00/1.05 = \$195.24 \neq \200 ; therefore, it is false.
- (c) The cost 1 year from now is $38(1.05) = \$39.90$; true
- (d) Cost now is $2887.14(1.05) = \$3031.50 \neq \3000 ; false.
- (e) The charge is 5% per year interest, or $2000(0.05) = \$100$; true.

1.6 SIMPLE AND COMPOUND INTEREST

The terms *interest*, *interest period*, and *interest rate* (introduced in Section 1.4) are useful in calculating equivalent sums of money for one interest period in the past and one period in the future. However, for more than one interest period, the terms *simple interest* and *compound interest* become important.

Simple interest is calculated using the principal only, ignoring any interest accrued in preceding interest periods. The total simple interest over several periods is computed as

$$\text{Interest} = (\text{principal})(\text{number of periods})(\text{interest rate}) \quad [1.5]$$

where the interest rate is expressed in decimal form.

EXAMPLE 1.7

Pacific Telephone Credit Union loaned money to an engineering staff member for a radio-controlled model airplane. The loan is for \$1000 for 3 years at 5% per year simple interest. How much money will the engineer repay at the end of 3 years? Tabulate the results.

Solution

The interest for each of the 3 years is

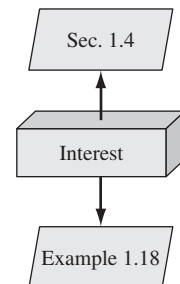
$$\text{Interest per year} = 1000(0.05) = \$50$$

Total interest for 3 years from Equation [1.5] is

$$\text{Total interest} = 1000(3)(0.05) = \$150$$

The amount due after 3 years is

$$\text{Total due} = \$1000 + 150 = \$1150$$



The \$50 interest accrued in the first year and the \$50 accrued in the second year do not earn interest. The interest due each year is calculated only on the \$1000 principal.

The details of this loan repayment are tabulated in Table 1–1 from the perspective of the borrower. The year zero represents the present, that is, when the money is borrowed. No payment is made until the end of year 3. The amount owed each year increases uniformly by \$50, since simple interest is figured on only the loan principal.

TABLE 1–1 Simple Interest Computations

(1) End of Year	(2) Amount Borrowed	(3) Interest	(4) Amount Owed	(5) Amount Paid
0	\$1000			
1	—	\$50	\$1050	\$ 0
2	—	50	1100	0
3	—	50	1150	1150

For *compound interest*, the interest accrued for each interest period is calculated on the *principal plus the total amount of interest accumulated in all previous periods*. Thus, compound interest means interest on top of interest. Compound interest reflects the effect of the time value of money on the interest also. Now the interest for one period is calculated as

$$\text{Interest} = (\text{principal} + \text{all accrued interest})(\text{interest rate}) \quad [1.6]$$

EXAMPLE 1.8

If an engineer borrows \$1000 from the company credit union at 5% per year compound interest, compute the total amount due after 3 years. Graph and compare the results of this and the previous example.

Solution

The interest and total amount due each year are computed separately using Equation [1.6].

Year 1 interest:	$\$1000(0.05) = \50.00
Total amount due after year 1:	$\$1000 + 50.00 = \1050.00
Year 2 interest:	$\$1050(0.05) = \52.50
Total amount due after year 2 :	$\$1050 + 52.50 = \1102.50
Year 3 interest:	$\$1102.50(0.05) = \55.13
Total amount due after year 3:	$\$1102.50 + 55.13 = \1157.63

MASTER 1

SECTION 1.6

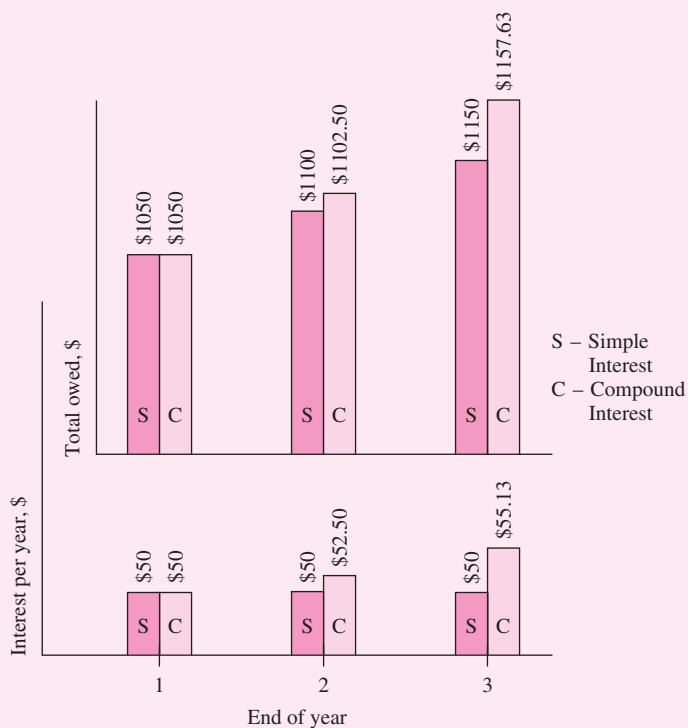
Simple and Compound Interest

TABLE 1-2 Compound Interest Computations, Example 1.8

(1) End of Year	(2) Amount Borrowed	(3) Interest	(4) Amount Owed	(5) Amount Paid
0	\$1000			
1	—	\$50.00	\$1050.00	\$ 0
2	—	52.50	1102.50	0
3	—	55.13	1157.63	1157.63

The details are shown in Table 1-2. The repayment plan is the same as that for the simple interest example—no payment until the principal plus accrued interest is due at the end of year 3.

Figure 1-4 shows the amount owed at the end of each year for 3 years. The difference due to the time value of money is recognized for the compound interest case. An extra $\$1157.63 - \$1150 = \$7.63$ of interest is paid compared with simple interest over the 3-year period.


Figure 1-4

Comparison of simple and compound interest calculations, Examples 1.7 and 1.8.

Comment

The difference between simple and compound interest grows each year. If the computations are continued for more years, for example, 10 years, the difference is \$128.90; after 20 years compound interest is \$653.30 more than simple interest.

If \$7.63 does not seem like a significant difference in only 3 years, remember that the beginning amount here is \$1000. If we make these same calculations for an initial amount of \$100,000 or \$1 million, multiply the difference by 100 or 1000, and we are talking real money. This indicates that the power of compounding is vitally important in all economics-based analyses.

Another and shorter way to calculate the total amount due after 3 years in Example 1.8 is to combine calculations rather than perform them on a year-by-year basis. The total due each year is as follows:

$$\text{Year 1: } \$1000(1.05)^1 = \$1050.00$$

$$\text{Year 2: } \$1000(1.05)^2 = \$1102.50$$

$$\text{Year 3: } \$1000(1.05)^3 = \$1157.63$$

The year 3 total is calculated directly; it does not require the year 2 total. In general formula form

$$\text{Total due after a number of years} = \text{principal}(1 + \text{interest rate})^{\text{number of years}}$$

This fundamental relation is used many times in upcoming chapters.

We combine the concepts of interest rate, simple interest, compound interest, and equivalence to demonstrate that different loan repayment plans may be equivalent, but differ substantially in monetary amounts from one year to another. This also shows that there are many ways to take into account the time value of money. The following example illustrates equivalence for five different loan repayment plans.

EXAMPLE 1.9

(a) Demonstrate the concept of equivalence using the different loan repayment plans described below. Each plan repays a \$5000 loan in 5 years at 8% interest per year.

- **Plan 1: Simple interest, pay all at end.** No interest or principal is paid until the end of year 5. Interest accumulates each year on the principal only.
- **Plan 2: Compound interest, pay all at end.** No interest or principal is paid until the end of year 5. Interest accumulates each year on the total of principal and all accrued interest.
- **Plan 3: Simple interest paid annually, principal repaid at end.** The accrued interest is paid each year, and the entire principal is repaid at the end of year 5.
- **Plan 4: Compound interest and portion of principal repaid annually.** The accrued interest and one-fifth of the principal (or \$1000) is repaid each

MASTER ①

SECTION 1.6 Simple and Compound Interest

21

year. The outstanding loan balance decreases each year, so the interest for each year decreases.

- **Plan 5: Equal payments of compound interest and principal made annually.** Equal payments are made each year with a portion going toward principal repayment and the remainder covering the accrued interest. Since the loan balance decreases at a rate slower than that in plan 4 due to the equal end-of-year payments, the interest decreases, but at a slower rate.

- (b) Make a statement about the equivalence of each plan at 8% simple or compound interest, as appropriate.

Solution

- (a) Table 1–3 presents the interest, payment amount, total owed at the end of each year, and total amount paid over the 5-year period (column 4 totals).

TABLE 1–3 Different Repayment Schedules Over 5 Years for \$5000 at 8% Per Year Interest

(1) End of Year	(2) Interest Owed for Year	(3) Total Owed at End of Year	(4) End-of-Year Payment	(5) Total Owed after Payment
<i>Plan 1: Simple Interest, Pay All at End</i>				
0				\$5000.00
1	\$400.00	\$5400.00	—	5400.00
2	400.00	5800.00	—	5800.00
3	400.00	6200.00	—	6200.00
4	400.00	6600.00	—	6600.00
5	400.00	7000.00	<u>\$7000.00</u>	
Totals			\$7000.00	
<i>Plan 2: Compound Interest, Pay All at End</i>				
0				\$5000.00
1	\$400.00	\$5400.00	—	5400.00
2	432.00	5832.00	—	5832.00
3	466.56	6298.56	—	6298.56
4	503.88	6802.44	—	6802.44
5	544.20	7346.64	<u>\$7346.64</u>	
Totals			\$7346.64	
<i>Plan 3: Simple Interest Paid Annually; Principal Repaid at End</i>				
0				\$5000.00
1	\$400.00	\$5400.00	\$400.00	5000.00
2	400.00	5400.00	400.00	5000.00
3	400.00	5400.00	400.00	5000.00
4	400.00	5400.00	400.00	5000.00
5	400.00	5400.00	<u>5400.00</u>	
Totals			\$7000.00	

TABLE 1-3 (Continued)

(1) End of Year	(2) Interest Owed for Year	(3) Total Owed at End of Year	(4) End-of-Year Payment	(5) Total Owed after Payment
<i>Plan 4: Compound Interest and Portion of Principal Repaid Annually</i>				
0				\$5000.00
1	\$400.00	\$5400.00	\$1400.00	4000.00
2	320.00	4320.00	1320.00	3000.00
3	240.00	3240.00	1240.00	2000.00
4	160.00	2160.00	1160.00	1000.00
5	80.00	1080.00	1080.00	
Totals			\$6200.00	
<i>Plan 5: Equal Annual Payments of Compound Interest and Principal</i>				
0				\$5000.00
1	\$400.00	\$5400.00	\$1252.28	4147.72
2	331.82	4479.54	1252.28	3227.25
3	258.18	3485.43	1252.28	2233.15
4	178.65	2411.80	1252.28	1159.52
5	92.76	1252.28	1252.28	
Totals			\$6261.41	

The amounts of interest (column 2) are determined as follows:

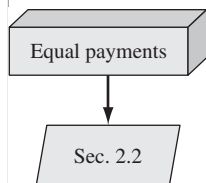
- Plan 1** Simple interest = (original principal)(0.08)
- Plan 2** Compound interest = (total owed previous year)(0.08)
- Plan 3** Simple interest = (original principal)(0.08)
- Plan 4** Compound interest = (total owed previous year)(0.08)
- Plan 5** Compound interest = (total owed previous year)(0.08)

Note that the amounts of the annual payments are different for each repayment schedule and that the total amounts repaid for most plans are different, even though each repayment plan requires exactly 5 years. The difference in the total amounts repaid can be explained (1) by the time value of money, (2) by simple or compound interest, and (3) by the partial repayment of principal prior to year 5.

(b) Table 1-3 shows that \$5000 at time 0 is equivalent to each of the following:

- Plan 1** \$7000 at the end of year 5 at 8% simple interest.
- Plan 2** \$7346.64 at the end of year 5 at 8% compound interest.
- Plan 3** \$400 per year for 4 years and \$5400 at the end of year 5 at 8% simple interest.
- Plan 4** Decreasing payments of interest and partial principal in years 1 (\$1400) through 5 (\$1080) at 8% compound interest.
- Plan 5** \$1252.28 per year for 5 years at 8% compound interest.

An engineering economy study uses plan 5; interest is compounded, and a constant amount is paid each period. This amount covers accrued interest and a partial amount of principal repayment.



MASTER ①**1.7 TERMINOLOGY AND SYMBOLS**

The equations and procedures of engineering economy utilize the following terms and symbols. Sample units are indicated.

P = value or amount of money at a time designated as the present or time 0. Also P is referred to as present worth (PW), present value (PV), net present value (NPV), discounted cash flow (DCF), and capitalized cost (CC); dollars

F = value or amount of money at some future time. Also F is called future worth (FW) and future value (FV); dollars

A = series of consecutive, equal, end-of-period amounts of money. Also A is called the annual worth (AW) and equivalent uniform annual worth (EUAW); dollars per year, dollars per month

n = number of interest periods; years, months, days

i = interest rate or rate of return per time period; percent per year, percent per month

t = time, stated in periods; years, months, days

The symbols P and F represent one-time occurrences; A occurs with the same value once each interest period for a specified number of periods. It should be clear that a present value P represents a single sum of money at some time prior to a future value F or prior to the first occurrence of an equivalent series amount A .

It is important to note that the symbol A always represents a uniform amount (i.e., the same amount each period) that extends through *consecutive* interest periods. Both conditions must exist before the series can be represented by A .

The interest rate i is assumed to be a compound rate, unless specifically stated as simple interest. The rate i is expressed in percent per interest period, for example, 12% per year. Unless stated otherwise, assume that the rate applies throughout the entire n years or interest periods. The decimal equivalent for i is always used in engineering economy computations.

All engineering economy problems involve the element of time n and interest rate i . In general, every problem will involve at least four of the symbols P , F , A , n , and i , with at least three of them estimated or known.

EXAMPLE 1.10

A new college graduate has a job with Boeing Aerospace. She plans to borrow \$10,000 now to help in buying a car. She has arranged to repay the entire principal plus 8% per year interest after 5 years. Identify the engineering economy symbols involved and their values for the total owed after 5 years.

Solution

In this case, P and F are involved, since all amounts are single payments, as well as n and i . Time is expressed in years.

$$P = \$10,000 \quad i = 8\% \text{ per year} \quad n = 5 \text{ years} \quad F = ?$$

The future amount F is unknown.

EXAMPLE 1.11

Assume you borrow \$2000 now at 7% per year for 10 years and must repay the loan in equal yearly payments. Determine the symbols involved and their values.

Solution

Time is in years.

$$P = \$2000$$

$$A = ? \text{ per year for 10 years}$$

$$i = 7\% \text{ per year}$$

$$n = 10 \text{ years}$$

In Examples 1.10 and 1.11, the P value is a receipt to the borrower, and F or A is a disbursement from the borrower. It is equally correct to use these symbols in the reverse roles.

EXAMPLE 1.12

On July 1, 2002, your new employer Ford Motor Company deposits \$5000 into your money market account, as part of your employment bonus. The account pays interest at 5% per year. You expect to withdraw an equal annual amount for the following 10 years. Identify the symbols and their values.

Solution

Time is in years.

$$P = \$5000$$

$$A = ? \text{ per year}$$

$$i = 5\% \text{ per year}$$

$$n = 10 \text{ years}$$

MASTER 1**EXAMPLE 1.13**

You plan to make a lump-sum deposit of \$5000 now into an investment account that pays 6% per year, and you plan to withdraw an equal end-of-year amount of \$1000 for 5 years, starting next year. At the end of the sixth year, you plan to close your account by withdrawing the remaining money. Define the engineering economy symbols involved.

Solution

Time is expressed in years.

$$P = \$5000$$

$$A = \$1000 \text{ per year for 5 years}$$

$$F = ? \text{ at end of year 6}$$

$$i = 6\% \text{ per year}$$

$$n = 5 \text{ years for the } A \text{ series and 6 for the } F \text{ value}$$

EXAMPLE 1.14

Last year Jane's grandmother offered to put enough money into a savings account to generate \$1000 this year to help pay Jane's expenses at college. (a) Identify the symbols, and (b) calculate the amount that had to be deposited exactly 1 year ago to earn \$1000 in interest now, if the rate of return is 6% per year.

Solution

(a) Time is in years.

$$P = ?$$

$$i = 6\% \text{ per year}$$

$$n = 1 \text{ year}$$

$$F = P + \text{interest}$$

$$= ? + \$1000$$

(b) Refer to Equations [1.3] and [1.4]. Let F = total amount now and P = original amount. We know that $F - P = \$1000$ is the accrued interest. Now we can determine P for Jane and her grandmother.

$$F = P + P(\text{interest rate})$$

The \$1000 interest can be expressed as

$$\text{Interest} = F - P = [P + P(\text{interest rate})] - P$$

$$= P(\text{interest rate})$$

$$\$1000 = P(0.06)$$

$$P = \frac{1000}{0.06} = \$16,666.67$$

1.8 INTRODUCTION TO SOLUTION BY COMPUTER

The functions on a computer spreadsheet can greatly reduce the amount of hand and calculator work for equivalency computations involving *compound interest* and the terms P , F , A , i , and n . The power of the electronic spreadsheet often makes it possible to enter a predefined spreadsheet function into one cell and obtain the final answer immediately. Any spreadsheet system can be used—one off the shelf, such as Microsoft Excel®, or one specially developed with built-in financial functions and operators. Excel is used throughout this book because it is readily available and easy to use.

Appendix A is a primer on using spreadsheets and Excel. The functions used in engineering economy are described there in detail, with explanations of all the parameters (also called arguments) placed between parentheses after the function identifier. The Excel online help function provides similar information. Appendix A also includes a section on spreadsheet layout that is useful when the economic analysis is presented to someone else—a coworker, a boss, or a professor.

A total of six Excel functions can perform most of the fundamental engineering economy calculations. However, these functions are no substitute for knowing how the time value of money and compound interest work. The functions are great supplemental tools, but they do not replace the understanding of engineering economy relations, assumptions, and techniques.

Using the symbols P , F , A , i , and n exactly as defined in the previous section, the Excel functions most used in engineering economic analysis are formulated as follows.

To find the present value P : $PV(i\%,n,A,F)$

To find the future value F : $FV(i\%,n,A,P)$

To find the equal, periodic value A : $PMT(i\%,n,P,F)$

To find the number of periods n : $NPER(i\%,A,P,F)$

To find the compound interest rate i : $RATE(n,A,P,F)$

To find the compound interest rate i : $IRR(\text{first_cell}:\text{last_cell})$

To find the present value P of any series: $NPV(i\%, \text{second_cell}:\text{last_cell}) + \text{first_cell}$

If some of the parameters don't apply to a particular problem, they can be omitted and zero is assumed. If the parameter omitted is an interior one, the comma must be entered. The last two functions require that a series of numbers be entered into contiguous spreadsheet cells, but the first five can be used with no supporting data. In all cases, the function must be preceded by an equals sign (=) in the cell where the answer is to be displayed.

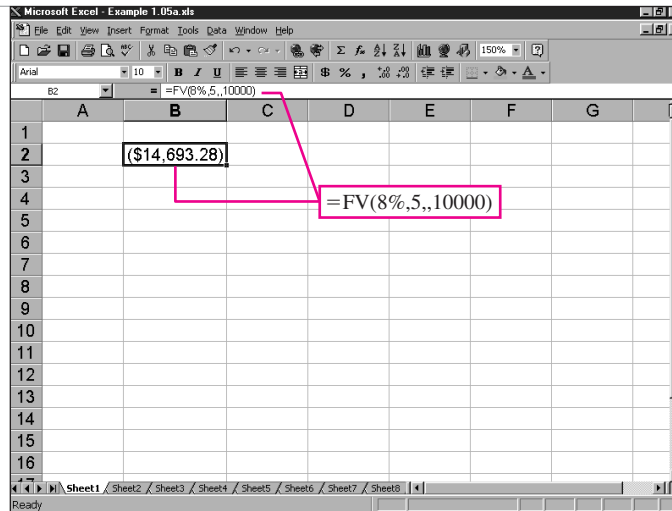
Each of these functions will be introduced and illustrated at the point in this text where they are most useful. However, to get an idea of how they work, look back at Examples 1.10 and 1.11. In Example 1.10, the future amount F is unknown, as indicated by $F = ?$ in the solution. In the next chapter, we will learn how the time value of money is used to find F , given P , i , and n . To find F in this example using a spreadsheet, simply enter the FV function preceded by an equals

MASTER 1

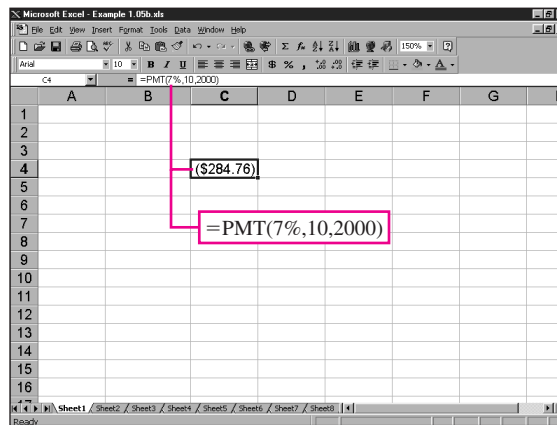
SECTION 1.8

Introduction to Solution by Computer

27



(a)



(b)

Figure 1-5

Excel spreadsheet functions for (a) Example 1.10 and (b) Example 1.11.

sign into any cell. The format is $=FV(i\%,n,,P)$ or $=FV(8\%,5,,10000)$. The comma is entered because there is no A involved. Figure 1-5a is a screen image of the Excel spreadsheet with the FV function entered into cell B2. The answer of $\$-14,693.28$ is displayed. The answer is in red on the actual Excel screen to indicate a negative amount from the borrower's perspective to repay the loan after 5 years. The FV function is shown in the formula bar above the worksheet itself. Also, we have added a cell tag to show the format of the FV function.

In Example 1.11, the uniform annual amount A is sought, and P , i , and n are known. Find A , using the function $PMT(i\%,n,P)$ or, in this example, $PMT(7\%,10,2000)$. Figure 1-5b shows the result in cell C4. The format of the FV function is shown in the formula bar and the cell tag.



Because these functions can be used so easily and rapidly, we will detail them in many of the examples throughout the book. A special checkered-flag icon, with *Q-Solv* (for quick solution) printed on it, is placed in the margin when just one function is needed to get an answer. In the introductory chapters of Level One, the entire spreadsheet and detailed functions are shown. In succeeding chapters, the Q-Solv icon is shown in the margin, and the spreadsheet function is contained within the solution of the example.

When the power of the computer is used to solve a more complex problem utilizing several functions and possibly an Excel chart (graph), the icon in the margin is a lightning bolt with the term *E-Solve* printed. These spreadsheets are more complex and contain much more information and computation, especially when sensitivity analysis is performed. The Solution by Computer answer to an example is always presented after the Solution by Hand. As mentioned earlier, the spreadsheet function is not a replacement for the correct understanding and application of the engineering economy relations. Therefore, the hand and computer solutions complement each other.

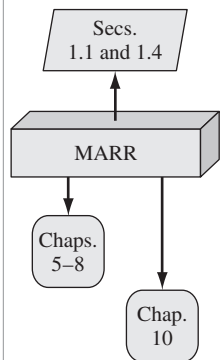
1.9 MINIMUM ATTRACTIVE RATE OF RETURN

For any investment to be profitable, the investor (corporate or individual) expects to receive more money than the amount invested. In other words, a fair *rate of return*, or *return on investment*, must be realizable. The definition of ROR in Equation [1.4] is used in this discussion, that is, amount earned divided by the original amount.

Engineering alternatives are evaluated upon the prognosis that a reasonable ROR can be expected. Therefore, some reasonable rate must be established for the selection criteria phase of the engineering economy study (Figure 1–1). The reasonable rate is called the *Minimum Attractive Rate of Return (MARR)* and is higher than the rate expected from a bank or some safe investment that involves minimal investment risk. Figure 1–6 indicates the relations between different rate of return values. In the United States, the current U.S. Treasury bill return is sometimes used as the benchmark safe rate.

The MARR is also referred to as the *hurdle rate* for projects; that is, to be considered financially viable the expected ROR must meet or exceed the MARR or hurdle rate. Note that the MARR is not a rate that is calculated like a ROR. The MARR is established by (financial) managers and used as a criterion against which an alternative's ROR is measured, when making the accept/reject decision.

To develop a foundation-level understanding of how a MARR value is established and used, we must return to the term *capital* introduced in Section 1.1. Capital is also referred to as *capital funds* and *capital investment money*. It always costs money in the form of interest to raise capital. The interest, stated as a percentage rate, is called the *cost of capital*. For example, if you want to purchase a new music system, but don't have sufficient money (capital), you could obtain a credit union loan at some interest rate, say, 9% per year and use that cash to the merchant now. Or, you could use your (newly acquired) credit card and



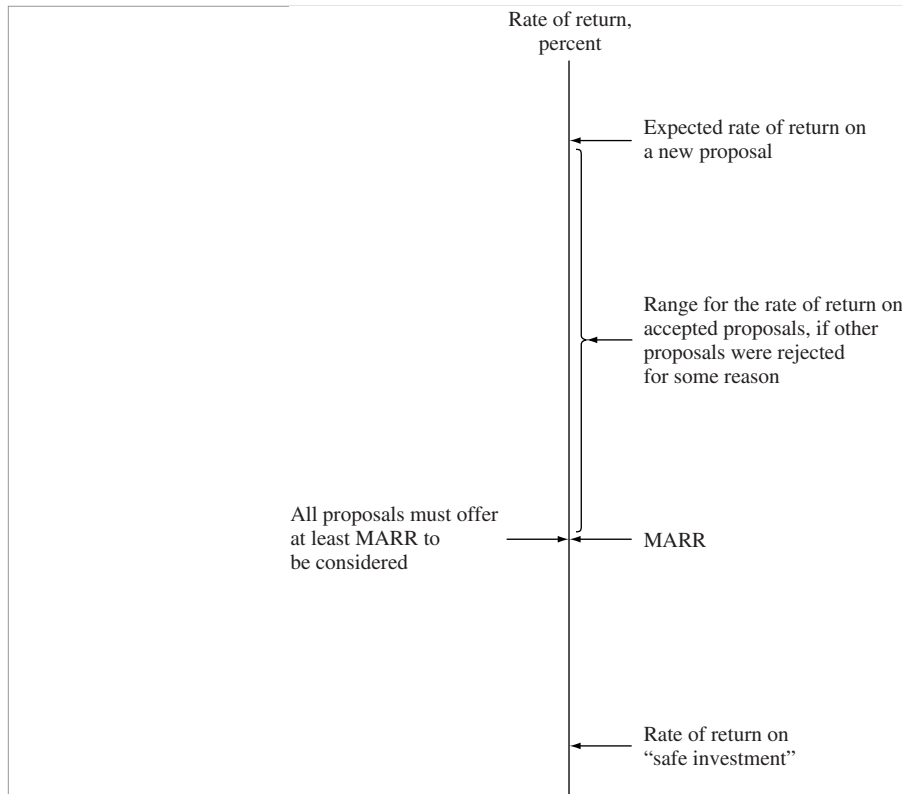


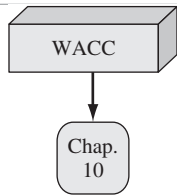
Figure 1-6
Size of MARR relative to other rate of return values.

pay off the balance on a monthly basis. This approach will probably cost you at least 18% per year. Or, you could use funds from your savings account that earns 5% per year and pay cash. The 9%, 18%, and 5% rates are your cost of capital estimates to raise the capital for the system by different methods of capital financing. In analogous ways, corporations estimate the cost of capital from different sources to raise funds for engineering projects and other types of projects.

In general, capital is developed in two ways—equity financing and debt financing. A combination of these two is very common for most projects. Chapter 10 covers these in greater detail, but a snapshot description follows.

Equity financing. The corporation uses its own funds from cash on hand, stock sales, or retained earnings. Individuals can use their own cash, savings, or investments. In the example above, using money from the 5% savings account is equity financing.

Debt financing. The corporation borrows from outside sources and repays the principal and interest according to some schedule, much like the plans in Table 1-3. Sources of debt capital may be bonds, loans, mortgages, venture capital pools, and many others. Individuals, too, can utilize debt sources, such as the credit card and credit union options described in the music system example.



Combinations of debt-equity financing mean that a weighted average cost of capital (WACC) results. If the music system is purchased with 40% credit card money at 18% per year and 60% savings account funds earning 5% per year, the weighted average cost of capital is $0.4(18) + 0.6(5) = 10.2\%$ per year.

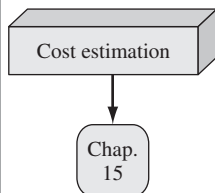
For a corporation, the *established MARR* used as a criterion to accept or reject an alternative will always be *higher than the weighted average cost of capital* that the corporation must bear to obtain the necessary capital funds. So the inequality

$$\text{ROR} \geq \text{MARR} > \text{cost of capital} \quad [1.7]$$

must be correct for an accepted project. Exceptions may be government-regulated requirements (safety, security, environmental, legal, etc.), economically lucrative ventures expected to lead to other opportunities, etc. Value-added engineering projects usually follow Equation [1.7].

Often there are many alternatives that are expected to yield a ROR that exceeds the MARR as indicated in Figure 1–6, but there may not be sufficient capital available for all, or the project's risk may be estimated as too high to take the investment chance. Therefore, new projects that are undertaken are usually those projects that have an expected return at least as great as the return on another alternative not yet funded. Such a selected new project would be a proposal represented by the top ROR arrow in Figure 1–6. For example, assume $\text{MARR} = 12\%$ and proposal 1 with an expected $\text{ROR} = 13\%$ cannot be funded due to a lack of capital funds. Meanwhile, proposal 2 has a $\text{ROR} = 14.5\%$ and is funded from available capital. Since proposal 1 is not undertaken due to the lack of capital, its estimated ROR of 13% is referred to as the *opportunity cost*; that is, the opportunity to make an additional 13% return is forgone.

1.10 CASH FLOWS: THEIR ESTIMATION AND DIAGRAMMING



In Section 1.3 cash flows are described as the inflows and outflows of money. These cash flows may be estimates or observed values. Every person or company has cash receipts—revenue and income (inflows); and cash disbursements—expenses, and costs (outflows). These receipts and disbursements are the cash flows, with a plus sign representing cash inflows and a minus sign representing cash outflows. Cash flows occur during specified periods of time, such as 1 month or 1 year.

Of all the elements of the engineering economy study approach (Figure 1–1), cash flow estimation is likely the most difficult and inexact. Cash flow estimates are just that—estimates about an uncertain future. Once estimated, the techniques of this book guide the decision making process. But the time-proven accuracy of an alternative's estimated cash inflows and outflows clearly dictates the quality of the economic analysis and conclusion.

Cash inflows, or receipts, may be comprised of the following, depending upon the nature of the proposed activity and the type of business involved.

MASTER ①

Samples of Cash Inflow Estimates

Revenues (usually *incremental* resulting from an alternative).
 Operating cost reductions (resulting from an alternative).
 Asset salvage value.
 Receipt of loan principal.
 Income tax savings.
 Receipts from stock and bond sales.
 Construction and facility cost savings.
 Saving or return of corporate capital funds.

Cash outflows, or disbursements, may be comprised of the following, again depending upon the nature of the activity and type of business.

Samples of Cash Outflow Estimates

First cost of assets.
 Engineering design costs.
 Operating costs (annual and incremental).
 Periodic maintenance and rebuild costs.
 Loan interest and principal payments.
 Major expected/unexpected upgrade costs.
 Income taxes.
 Expenditure of corporate capital funds.

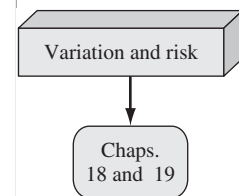
Background information for estimates may be available in departments such as accounting, finance, marketing, sales, engineering, design, manufacturing, production, field services, and computer services. The accuracy of estimates is largely dependent upon the experiences of the person making the estimate with similar situations. Usually *point estimates* are made; that is, a single-value estimate is developed for each economic element of an alternative. If a statistical approach to the engineering economy study is undertaken, a *range estimate* or *distribution estimate* may be developed. Though more involved computationally, a statistical study provides more complete results when key estimates are expected to vary widely. We will use point estimates throughout most of this book. Final chapters discuss decision making under risk.

Once the cash inflow and outflow estimates are developed, the net cash flow can be determined.

$$\begin{aligned} \text{Net cash flow} &= \text{receipts} - \text{disbursements} \\ &= \text{cash inflows} - \text{cash outflows} \quad [1.8] \end{aligned}$$

Since cash flows normally take place at varying times within an interest period, a simplifying assumption is made.

The *end-of-period convention* means that all cash flows are assumed to occur at the end of an interest period. When several receipts and disbursements occur within a given interest period, the *net* cash flow is assumed to occur at the *end* of the interest period.



However, it should be understood that, although F or A amounts are located at the end of the interest period by convention, the end of the period is not necessarily December 31. In Example 1.12 the deposit took place on July 1, 2002, and the withdrawals will take place on July 1 of each succeeding year for 10 years. Thus, *end of the period means end of interest period, not end of calendar year.*

The *cash flow diagram* is a very important tool in an economic analysis, especially when the cash flow series is complex. It is a graphical representation of cash flows drawn on a time scale. The diagram includes what is known, what is estimated, and what is needed. That is, once the cash flow diagram is complete, another person should be able to work the problem by looking at the diagram.

Cash flow diagram time $t = 0$ is the present, and $t = 1$ is the end of time period 1. We assume that the periods are in years for now. The time scale of Figure 1-7 is set up for 5 years. Since the end-of-year convention places cash flows at the end of years, the “1” marks the end of year 1.

While it is not necessary to use an exact scale on the cash flow diagram, you will probably avoid errors if you make a neat diagram to approximate scale for both time and relative cash flow magnitudes.

The direction of the arrows on the cash flow diagram is important. A vertical arrow pointing up indicates a positive cash flow. Conversely, an arrow pointing down indicates a negative cash flow. Figure 1-8 illustrates a receipt (cash inflow) at the end of year 1 and equal disbursements (cash outflows) at the end of years 2 and 3.

The perspective or vantage point must be determined prior to placing a sign on each cash flow and diagramming it. As an illustration, if you borrow \$2500 to buy a \$2000 used Harley-Davidson for cash, and you use the remaining \$500 for a new paint job, there may be several different perspectives taken. Possible

Figure 1-7
A typical cash flow time scale for 5 years.

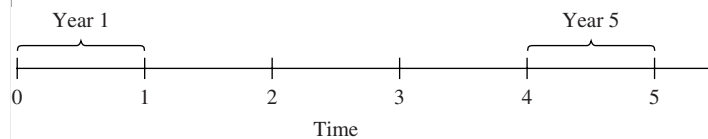
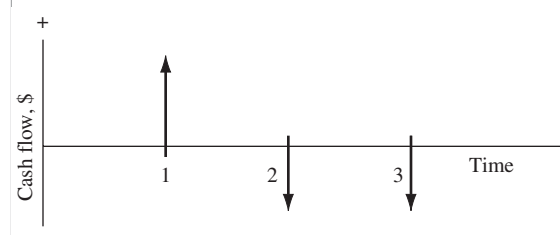


Figure 1-8
Example of positive and negative cash flows.



MASTER 1

SECTION 1.10

Cash Flows: Their Estimation and Diagramming

33

perspectives, cash flow signs, and amounts are as follows.

Perspective	Cash Flow, \$
Credit union	-2500
You as borrower	+2500
You as purchaser, and as paint customer	-2000 -500
Used cycle dealer	+2000
Paint shop owner	+500

EXAMPLE 1.15

Reread Example 1.10, where $P = \$10,000$ is borrowed at 8% per year and F is sought after 5 years. Construct the cash flow diagram.

Solution

Figure 1-9 presents the cash flow diagram from the vantage point of the borrower. The present sum P is a cash inflow of the loan principal at year 0, and the future sum F is the cash outflow of the repayment at the end of year 5. The interest rate should be indicated on the diagram.

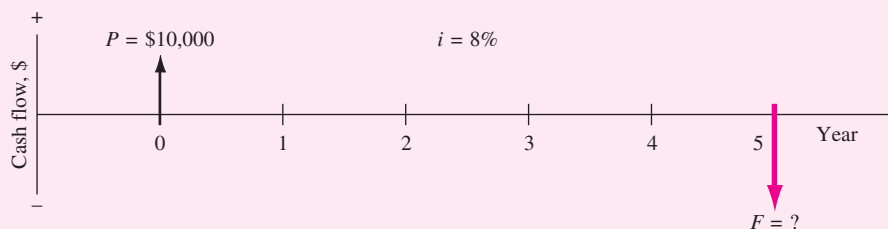


Figure 1-9
Cash flow diagram, Example 1.15.

EXAMPLE 1.16

Each year Exxon-Mobil expends large amounts of funds for mechanical safety features throughout its worldwide operations. Carla Ramos, a lead engineer for Mexico and Central American operations, plans expenditures of \$1 million now and each of the next 4 years just for the improvement of field-based pressure-release valves. Construct the cash flow diagram to find the equivalent value of these expenditures at the end of year 4, using a cost of capital estimate for safety-related funds of 12% per year.

Solution

Figure 1-10 indicates the uniform and negative cash flow series (expenditures) for five periods, and the unknown F value (positive cash flow equivalent) at exactly the same

time as the fifth expenditure. Since the expenditures start immediately, the first \$1 million is shown at time 0, not time 1. Therefore, the last negative cash flow occurs at the end of the fourth year, when F also occurs. To make this diagram appear similar to that of Figure 1–9 with a full 5 years on the time scale, the addition of the year -1 prior to year 0 completes the diagram for a full 5 years. This addition demonstrates that year 0 is the end-of-period point for the year -1 .

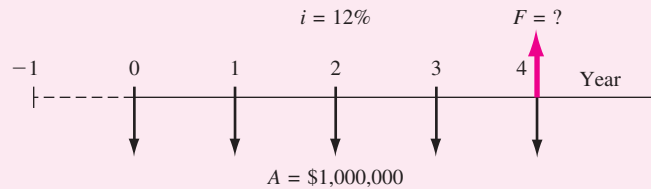


Figure 1–10
Cash flow diagram, Example 1.16.

EXAMPLE 1.17

A father wants to deposit an unknown lump-sum amount into an investment opportunity 2 years from now that is large enough to withdraw \$4000 per year for state university tuition for 5 years starting 3 years from now. If the rate of return is estimated to be 15.5% per year, construct the cash flow diagram.

Solution

Figure 1–11 presents the cash flows from the father's perspective. The present value P is a cash outflow 2 years hence and is to be determined ($P = ?$). Note that this present value does not occur at time $t = 0$, but it does occur one period prior to the first A value of \$4000, which is the cash inflow to the father.

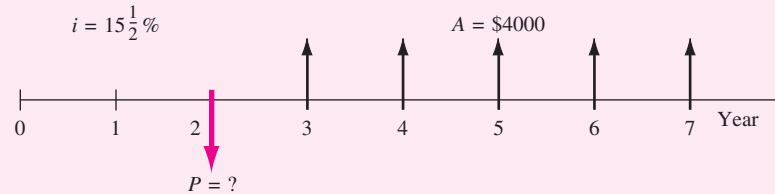


Figure 1–11
Cash flow diagram, Example 1.17.

Additional Examples 1.19 and 1.20.

MASTER ①

SECTION 1.11

Rule of 72: Estimating Doubling Time and Interest Rate

35

1.11 RULE OF 72: ESTIMATING DOUBLING TIME AND INTEREST RATE

Sometimes it is helpful to estimate the number of years n or the rate of return i required for a single cash flow amount to double in size. The *rule of 72* for compound interest rates can be used to estimate i or n , given the other value. The estimation is simple; the time required for an initial single amount to double in size with compound interest is approximately equal to 72 divided by the rate of return in percent.

$$\text{Estimated } n = \frac{72}{i} \quad [1.9]$$

For example, at a rate of 5% per year, it would take approximately $72/5 = 14.4$ years for a current amount to double. (The actual time required is 14.3 years, as will be shown in Chapter 2.) Table 1–4 compares the times estimated from the rule of 72 to the actual times required for doubling at several compounded rates. As you can see, very good estimates are obtained.

Alternatively, the compound rate i in percent required for money to double in a specified period of time n can be estimated by dividing 72 by the specified n value.

$$\text{Estimated } i = \frac{72}{n} \quad [1.10]$$

In order for money to double in a time period of 12 years, for example, a compound rate of return of approximately $72/12 = 6\%$ per year would be required. The exact answer is 5.946% per year.

If the interest is simple, a rule of 100 may be used in the same way. In this case the answers obtained will always be exactly correct. As illustrations, money doubles in exactly 12 years at $100/12 = 8.33\%$ simple interest. Or, at 5% simple interest it takes exactly $100/5 = 20$ years to double.

TABLE 1–4 Doubling Time Estimates Using the Rule of 72 and the Actual Time Using Compound Interest Calculations

Rate of Return, % per Year	Doubling Time, Years	
	Rule-of-72 Estimate	Actual Years
1	72	70
2	36	35.3
5	14.4	14.3
10	7.2	7.5
20	3.6	3.9
40	1.8	2.0



1.12 SPREADSHEET APPLICATION—SIMPLE AND COMPOUND INTEREST, AND CHANGING CASH FLOW ESTIMATES

The example below demonstrates how an Excel spreadsheet can be used to obtain equivalent future values. A key feature is the use of mathematical relations developed in the cells to perform sensitivity analysis for changing cash flow estimates and the interest rate. To answer these basic questions using hand solution can be time-consuming; the spreadsheet makes it much easier.

EXAMPLE 1.18

A Japan-based architectural firm has asked a United States-based software engineering group to infuse GIS (geographical information system) sensing capability via satellite into monitoring software for high-rise structures in order to detect greater-than-expected horizontal movements. This software could be very beneficial as an advance warning of serious tremors in earthquake-prone areas in Japan and the United States. The inclusion of accurate GIS data is estimated to increase annual revenue over that for the current software system by \$200,000 for each of the next 2 years, and by \$300,000 for each of years 3 and 4. The planning horizon is only 4 years due to the rapid advances made internationally in building-monitoring software. Develop spreadsheets to answer the questions below.

- Determine the equivalent future value in year 4 of the increased cash flows, using an 8% per year rate of return. Obtain answers for both simple and compound interest.
- Rework part (a) if the cash flow estimates in years 3 and 4 increase from \$300,000 to \$600,000.
- The financial manager of the U.S. company wants to consider the effects of 4% per year inflation in the analysis of part (a). As mentioned in Section 1.4, inflation reduces the real rate of return. For the 8% rate of return, an inflation rate of 4% per year compounded each year reduces the return to 3.85% per year.

Solution by Computer

Refer to Figure 1–12a to c for the solutions. All three spreadsheets contain the same information, but the cell values are altered as required by the question. (Actually, all the questions posed here can be answered on one spreadsheet by simply changing the numbers. Three spreadsheets are shown here for explanation purposes only.)

The Excel functions are constructed with reference to the cells, not the values themselves, so that sensitivity analysis can be performed without function changes. This approach treats the value in a cell as a *global variable* for the spreadsheet. For example, the 8% (simple or compound interest) rate in cell B4 will be referenced in all functions as B4, not 8%. Thus, a change in the rate requires only one alteration in the cell B4 entry, not in every spreadsheet relation and function where 8% is used. Key Excel relations are detailed in the cell tags.

- 8% simple interest.* Refer to Figure 1–12a, columns C and D, for the answers. Simple interest earned each year (column C) incorporates Equation [1.5] one year

MASTER 1

SECTION 1.12

Spreadsheet Application—Simple and Compound Interest

Microsoft Excel - Example 1.18(a-c)

File Edit View Insert Format Tools Data Window Help

Example 1.18 (contains 3 worksheets)
Part (a) - Find F in year 4

Rate of return 8.00%

End of year (EOY)	Cash flow	Simple interest		Compound interest	
		Interest earned during year	Cumulative equivalent EOY cash flow	Interest earned during year	Cumulative equivalent EOY cash flow
0	\$ -				
1	\$ 200,000	\$ -	\$ 200,000	\$ -	\$ 200,000
2	\$ 200,000	\$ 16,000	\$ 416,000	\$ 16,000	\$ 416,000
3	\$ 300,000	\$ 32,000	\$ 748,000	\$ 33,280	\$ 749,280
4	\$ 300,000	\$ 56,000	\$ 1,104,000	\$ 59,942	\$ 1,109,222
Total	\$ 1,000,000	\$ 104,000		\$ 109,222	

Formulas shown in pink boxes:

- $=B15+E15+F14$
- $=B12*B4$
- $=C14+B14*B4$
- $=SUM(B15:C15)+D14$
- $=F14*B4$

(a)

Microsoft Excel - Example 1.18(a-c)

File Edit View Insert Format Tools Data Window Help

(b) Find F with increased cash flow estimates

Rate of return 8.00%

End of year (EOY)	Cash flow	Simple interest		Compound interest	
		Interest earned during year	Cumulative equivalent EOY cash flow	Interest earned during year	Cumulative equivalent EOY cash flow
0	\$ -				
1	\$ 200,000	\$ -	\$ 200,000	\$ -	\$ 200,000
2	\$ 200,000	\$ 16,000	\$ 416,000	\$ 16,000	\$ 416,000
3	\$ 600,000	\$ 32,000	\$ 1,048,000	\$ 33,280	\$ 1,049,280
4	\$ 600,000	\$ 80,000	\$ 1,728,000	\$ 83,942	\$ 1,733,222
Total	\$ 1,800,000	\$ 128,000		\$ 133,222	

(b)

		Simple interest		Compound interest	
		Interest earned	Cumulative	Interest earned	Cumulative
End of year		during year	equivalent	during year	equivalent
(EOY)	Cash flow		EOY cash flow		EOY cash flow
0	\$ -				
1	\$ 200,000	\$ -	\$ 200,000	\$ -	\$ 200,000
2	\$ 200,000	\$ 7,700	\$ 407,700	\$ 7,700	\$ 407,700
3	\$ 300,000	\$ 15,400	\$ 723,100	\$ 15,696	\$ 723,396
4	\$ 300,000	\$ 26,950	\$ 1,050,050	\$ 27,851	\$ 1,051,247
Total	\$ 1,000,000	\$ 50,050		\$ 51,247	

(c)

Figure 1-12

Spreadsheet solution including sensitivity analysis, Example 1.18(a)-(c).

at a time into the interest relation by using only the end-of-year (EOY) cash flow amounts (\$200,000 or \$300,000) to determine interest for the next year. This interest is added to the interest from all previous years. In \$1000 units,

$$\text{Year 2: } C13 = B12 * B4 = \$200(0.08) = \$16 \quad (\text{see the cell tag})$$

$$\text{Year 3: } C14 = C13 + B13 * B4 = \$16 + 200(0.08) = \$32$$

$$\text{Year 4: } C15 = C14 + B14 * B4 = \$32 + 300(0.08) = \$56 \quad (\text{see the cell tag})$$

Remember, an = sign must precede each relation in the spreadsheet. Cell C16 contains the function SUM(C12:C15) to display the total simple interest of \$104,000 over the 4 years. The future value is in D15. It is $F = \$1,104,000$ which includes the cumulative amount of all cash flows and all simple interest. In \$1000 units, example functions are

$$\text{Year 2: } D13 = \text{SUM}(B13:C13) + D12 = (\$200 + 16) + 200 = \$416$$

$$\text{Year 4: } D15 = \text{SUM}(B15:C15) + D14 = (\$300 + 56) + 748 = \$1104$$

8% compound interest. See Figure 1-12a, columns E and F. The spreadsheet structure is the same, except that Equation [1.6] is incorporated into the compound interest values in column E, thus adding interest on top of earned interest.

MASTER 1

SECTION 1.12

Spreadsheet Application—Simple and Compound Interest

39

Interest at 8% is based on the accumulated cash flow at the end of the previous year. In \$1000 units,

$$\text{Year 2 interest: } E13 = F12 * B4 = \$200(0.08) = \$16$$

$$\text{Cumulative cash flow: } F13 = B13 + E13 + F12 = \$200 + 16 + 200 = \$416$$

$$\text{Year 4 interest: } E15 = F14 * B4 = \$749.28(0.08) = \$59.942$$

(see the cell tag)

$$\text{Cumulative cash flow: } F15 = B15 + E15 + F14$$

$$= \$300 + 59.942 + 749.280 = \$1109.222$$

The equivalent future value is in cell F15, where $F = \$1,109,222$ is shown.

The cash flows are equivalent to \$1,104,000 at a simple 8% interest rate, and \$1,109,222 at a compound 8% interest rate. Using a compound interest rate increases the F value by \$5222.

Note that it is not possible to use the FV function in this case because the A values are not the same for all 4 years. We will learn how to use all the basic functions in more versatile ways in the next few chapters.

- (b) Refer to Figure 1–12*b*. In order to initialize the spreadsheet with the two increased cash flow estimates, replace the \$300,000 values in B14 and B15 with \$600,000. All spreadsheet relations are identical, and the new interest and accumulated cash flow values are shown immediately. The equivalent fourth-year F values have increased for both the 8% simple and compound interest rates (D15 and F15, respectively).
- (c) Figure 1–12*c* is identical to the spreadsheet in Figure 1–12*a*, except the cell B4 now contains the rate of 3.85%. The corresponding F value for compound interest in F15 has decreased to \$1,051,247 from the \$1,109,222 at 8%. This represents an effect of inflation of \$57,975 in only four years. It is no surprise that governments, corporations, engineers, and all individuals are concerned when inflation rises and the currency is worth less over time.

Comment

When working with an Excel spreadsheet, it is possible to display all of the entries and functions on the screen by simultaneously touching the <Ctrl> and <> keys, which may be in the upper left of the keyboard on the key with <~>. Additionally, it may be necessary to widen some columns in order to display the entire function statement.

ADDITIONAL EXAMPLES**EXAMPLE 1.19****CASH FLOW DIAGRAMS**

A rental company spent \$2500 on a new air compressor 7 years ago. The annual rental income from the compressor has been \$750. Additionally, the \$100 spent on maintenance during the first year has increased each year by \$25. The company plans to sell the compressor at the end of next year for \$150. Construct the cash flow diagram from the company's perspective.

Solution

Use now as time $t = 0$. The incomes and costs for years -7 through 1 (next year) are tabulated below with net cash flow computed using Equation [1.8]. The net cash flows (one negative, eight positive) are diagrammed in Figure 1-13.

End of year	Income	Cost	Net Cash Flow
-7	\$ 0	\$2500	\$-2500
-6	750	100	650
-5	750	125	625
-4	750	150	600
-3	750	175	575
-2	750	200	550
-1	750	225	525
0	750	250	500
1	750 + 150	275	625

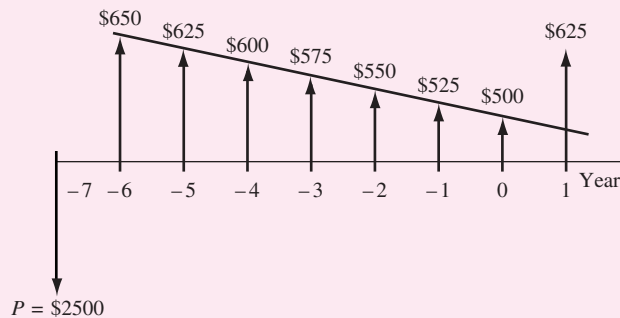


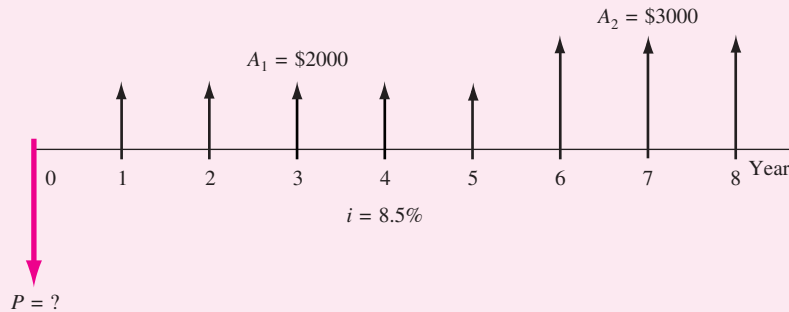
Figure 1.13
Cash flow diagram, Example 1.19.

EXAMPLE 1.20**CASH FLOW DIAGRAMS**

An electrical engineer wants to deposit an amount P now such that she can withdraw an equal annual amount of $A_1 = \$2000$ per year for the first 5 years starting 1 year after the deposit, and a different annual withdrawal of $A_2 = \$3000$ per year for the following 3 years. How would the cash flow diagram appear if $i = 8.5\%$ per year?

Solution

The cash flows are shown in Figure 1–14. The negative cash outflow P occurs now. The first withdrawal (positive cash inflow) for the A_1 series occurs at the end of year 1, and A_2 occurs in years 6 through 8.

**Figure 1–14**

Cash flow diagram with two different A series, Example 1.20.

CHAPTER SUMMARY

Engineering economy is the application of economic factors and criteria to evaluate alternatives, considering the time value of money. The engineering economy study involves computing a specific economic measure of worth for estimated cash flows over a specific period of time.

The concept of *equivalence* helps in understanding how different sums of money at different times are equal in economic terms. The differences between simple interest (based on principal only) and compound interest (based on principal and interest upon interest) have been described in formulas, tables, and graphs. This power of compounding is very noticeable, especially over long periods of time, as is the effect of inflation, introduced here.

The MARR is a reasonable rate of return established as a hurdle rate to determine if an alternative is economically viable. The MARR is always higher than the return from a safe investment.

Also, we learned about cash flows:

- Difficulties with their estimation.
- Difference between estimated and actual value.
- End-of-year convention for cash flow location.
- Net cash flow computation.
- Different perspectives in determining the cash flow sign.
- Construction of a cash flow diagram.

PROBLEMS

Basic Concepts

- 1.1 What is meant by the term *time value of money*?
- 1.2 List three intangible factors.
- 1.3 (a) What is meant by evaluation criterion?
(b) What is the primary evaluation criterion used in economic analysis?
- 1.4 List three evaluation criteria besides the economic one for selecting the best restaurant.
- 1.5 Discuss the importance of *identifying* alternatives in the engineering economic process.
- 1.6 What is the difference between simple and compound interest?
- 1.7 What is meant by minimum attractive rate of return?
- 1.8 What is the difference between debt and equity financing? Give an example of each.

Interest Rate and Rate of Return

- 1.9 Trucking giant Yellow Corp agreed to purchase rival Roadway for \$966 million in order to reduce so-called back-office costs (e.g., payroll and insurance) by \$45 million per year. If the savings were realized as planned, what would be the rate of return on the investment?
- 1.10 If Ford Motor Company's profits increased from 22 cents per share to 29 cents per share in the April–June quarter compared to the previous quarter, what was the rate of increase in profits for that quarter?
- 1.11 A broadband service company borrowed \$2 million for new equipment and repaid the principal of the loan plus \$275,000

interest after 1 year. What was the interest rate on the loan?

- 1.12 A design-build engineering firm completed a pipeline project wherein the company realized a profit of \$2.3 million in 1 year. If the amount of money the company had invested was \$6 million, what was the rate of return on the investment?
- 1.13 US Filter received a contract for a small water desalting plant whereby the company expected to make a 28% rate of return on its investment. If the company invested \$8 million in equipment the first year, what was the amount of the profit in that year?
- 1.14 A publicly traded construction company reported that it just paid off a loan that it received 1 year earlier. If the total amount of money the company paid was \$1.6 million and the interest rate on the loan was 10% per year, how much money did the company borrow 1 year ago?
- 1.15 A start-up chemical company has established a goal of making at least a 35% per year rate of return on its investment. If the company acquired \$50 million in venture capital, how much did it have to earn in the first year?

Equivalence

- 1.16 At an interest rate of 8% per year, \$10,000 today is equivalent to how much (a) 1 year from now and (b) 1 year ago?
- 1.17 A medium-size consulting engineering firm is trying to decide whether it should replace its office furniture now or wait and do it 1 year from now. If it waits 1 year, the cost is expected to be \$16,000. At an interest rate of 10% per year, what would be the equivalent cost now?

MASTER 1

PROBLEMS

43

1.18 An investment of \$40,000 one year ago and \$50,000 now are equivalent at what interest rate?

1.19 At what interest rate would \$100,000 now be equivalent to \$80,000 one year ago?

Simple and Compound Interest

1.20 Certain certificates of deposit accumulate interest at 10% per year simple interest. If a company invests \$240,000 now in these certificates for the purchase of a new machine 3 years from now, how much will the company have at the end of the 3-year period?

1.21 A local bank is offering to pay compound interest of 7% per year on new savings accounts. An e-bank is offering 7.5% per year simple interest on a 5-year certificate of deposit. Which offer is more attractive to a company that wants to set aside \$1,000,000 now for a plant expansion 5 years from now?

1.22 Badger Pump Company invested \$500,000 five years ago in a new product line that is now worth \$1,000,000. What rate of return did the company earn (a) on a simple interest basis and (b) on a compound interest basis?

1.23 How long will it take for an investment to double at 5% per year (a) simple interest and (b) compound interest?

1.24 A company that manufactures regenerative thermal oxidizers made an investment 10 years ago that is now worth \$1,300,000. How much was the initial investment at an interest rate of 15% per year (a) simple interest and (b) compound interest?

1.25 Companies frequently borrow money under an arrangement that requires them to make periodic payments of only interest and then pay the principal of the loan all at

once. A company that manufactures odor control chemicals borrowed \$400,000 for 3 years at 10% per year compound interest under such an arrangement. What is the difference in the *total amount paid* between this arrangement (identified as plan 1) and plan 2, in which the company makes no interest payments until the loan is due and then pays it off in one lump sum?

1.26 A company that manufactures in-line mixers for bulk manufacturing is considering borrowing \$1.75 million to update a production line. If it borrows the money now, it can do so at an interest rate of 7.5% per year simple interest for 5 years. If it borrows next year, the interest rate will be 8% per year compound interest, but it will be for only 4 years. (a) How much interest (total) will be paid under each scenario, and (b) should the company borrow now or 1 year from now? Assume the total amount due will be paid when the loan is due in either case.

Symbols and Spreadsheets

1.27 Define the symbols involved when a construction company wants to know how much money it can spend 3 years from now in lieu of spending \$50,000 now to purchase a new truck, when the compound interest rate is 15% per year.

1.28 State the purpose for each of the following built-in Excel functions.

(a) $FV(i\%,n,A,P)$

(b) $IRR(\text{first_cell}:\text{last_cell})$

(c) $PMT(i\%,n,P,F)$

(d) $PV(i\%,n,A,F)$

1.29 What are the values of the engineering economy symbols P , F , A , i , and n in the following Excel functions? Use a ? for the symbol that is to be determined.

(a) $FV(7\%,10,2000,9000)$

(b) $PMT(11\%,20,14000)$

(c) $PV(8\%,15,1000,800)$

1.30 Write the engineering economy symbol that corresponds to each of the following Excel functions.

- (a) PV
- (b) PMT
- (c) NPER
- (d) IRR
- (e) FV

1.31 In a built-in Excel function, if a certain parameter does not apply, under what circumstances can it be left blank? When must a comma be entered in its place?

MARR and Cost of Capital

1.32 Identify each of the following as either a safe investment or a risky one.

- (a) New restaurant business
- (b) Savings account in a bank
- (c) Certificate of deposit
- (d) Government bond
- (e) Relative's "get-rich-quick" idea

1.33 Identify each of the following as either equity or debt financing.

- (a) Money from savings
- (b) Money from a certificate of deposit
- (c) Money from a relative who is a partner in the business
- (d) Bank loan
- (e) Credit card

1.34 Rank the following from highest to lowest rate of return or interest rate: government bond, corporate bond, credit card, bank loan to new business, interest on checking account.

1.35 Rank the following from highest to lowest interest rate: cost of capital, acceptable rate of return on a risky investment, minimum attractive rate of return, rate of return on a safe investment, interest on checking account, interest on savings account.

1.36 Five separate projects have calculated rates of return of 8, 11, 12.4, 14, and 19%

per year. An engineer wants to know which projects to accept on the basis of rate of return. She learns from the finance department that company funds, which have a cost of capital of 18% per year, are commonly used to fund 25% of all capital projects. Later, she is told that borrowed money is currently costing 10% per year. If the MARR is established at exactly the weighted average cost of capital, which projects should she accept?

Cash Flows

1.37 What is meant by the end-of-period convention?

1.38 Identify the following as cash inflows or outflows to Daimler-Chrysler: income taxes, loan interest, salvage value, rebates to dealers, sales revenues, accounting services, cost reductions.

1.39 Construct a cash flow diagram for the following cash flows: \$10,000 outflow at time zero, \$3000 per year outflow in years 1 through 3 and \$9000 inflow in years 4 through 8 at an interest rate of 10% per year, and an unknown future amount in year 8.

1.40 Construct a cash flow diagram to find the present worth of a future outflow of \$40,000 in year 5 at an interest rate of 15% per year.

Doubling the Value

1.41 Use the rule of 72 to estimate the time it would take for an initial investment of \$10,000 to accumulate to \$20,000 at a compound rate of 8% per year.

1.42 Estimate the time it would take (according to the rule of 72) for money to quadruple in value at a compound interest rate of 9% per year.

MASTER 1

EXTENDED EXERCISE

45

- 1.43 Use the rule of 72 to estimate the interest that would be required for \$5000 to accumulate to \$10,000 in 4 years.
- 1.44 If you now have \$62,500 in your retirement account and you want to retire when the account is worth \$2 million, estimate the rate of return that the account must earn if you want to retire in 20 years without adding any more money to the account.

FE REVIEW PROBLEMS

- 1.45 An example of an intangible factor is
- (a) Taxes
 - (b) Cost of materials
 - (c) Morale
 - (d) Rent
- 1.46 The time it would take for money to double at a simple interest rate of 5% per year is closest to
- (a) 10 years
 - (b) 12 years
 - (c) 15 years
 - (d) 20 years
- 1.47 At a compound interest rate of 10% per year, \$10,000 one year ago is now equivalent to
- (a) \$8264
 - (b) \$9091
 - (c) \$11,000
 - (d) \$12,100
- 1.48 An investment of \$10,000 nine years ago has accumulated to \$20,000 now. The compound rate of return earned on the investment is closest to
- (a) 6%
 - (b) 8%
 - (c) 10%
 - (d) 12%
- 1.49 In most engineering economy studies, the best alternative is the one that
- (a) Will last the longest time
 - (b) Is easiest to implement
 - (c) Costs the least
 - (d) Is most politically correct
- 1.50 The cost of tuition at a certain public university was \$160 per credit-hour 5 years ago. The cost today (exactly 5 years later) is \$235. The annual rate of increase is closest to
- (a) 4%
 - (b) 6%
 - (c) 8%
 - (d) 10%

EXTENDED EXERCISE**EFFECTS OF COMPOUND INTEREST**

In an effort to maintain compliance with noise emission standards on the processing floor, National Semiconductors requires the use of noise-measuring instruments. The company plans to purchase new portable systems at the end of next year at a cost of \$9000 each. National estimates the maintenance cost to be \$500 per year for 3 years, after which they will be salvaged for \$2000 each.



Questions

1. Construct the cash flow diagram. For a compound interest rate of 8% per year, find the equivalent F value after 4 years, using calculations by hand.
2. Find the F value in question 1, using a spreadsheet.
3. Find the F value if the maintenance costs are \$300, \$500, and \$1000 for each of the 3 years. By how much has the F value changed?
4. Find the F value in question 1 in terms of dollars needed in the future with an adjustment for inflation of 4% per year. This increases the interest rate from 8% to 12.32% per year.

CASE STUDY

DESCRIBING ALTERNATIVES FOR PRODUCING REFRIGERATOR SHELLS

Background

Large refrigerator manufacturers like Whirlpool, General Electric, Frigidaire, and others may subcontract the molding of their plastic liners and door panels. One prime national subcontractor is Innovations Plastics. It is expected that in about 2 years improvements in mechanical properties will allow the molded plastic to sustain increased vertical and horizontal loading, thus significantly reducing the need for attached metal anchors for some shelving. However, improved molding equipment will be needed to enter this market. The company president wants a recommendation on whether Innovations should plan on offering the new technology to the major manufacturers and an estimate of the necessary capital investment to enter this market early.

You work as an engineer for Innovations. At this stage, you are not expected to perform a complete engineering economic analysis, for not enough information is available. You are asked to formulate reasonable alternatives, determine what data and estimates are needed for each one, and ascertain what criteria (economic and noneconomic) should be utilized to make the final decision.

Information

Some information useful at this time is as follows:

- The technology and equipment are expected to last about 10 years before new methods are developed.
- Inflation and income taxes will not be considered in the analysis.
- The expected returns on capital investment used for the last three new technology projects were compound rates of 15, 5, and 18%. The 5% rate was the criterion for enhancing an employee-safety system on an existing chemical-mixing process.
- Equity capital financing beyond \$5 million is not possible. The amount of debt financing and its cost are unknown.
- Annual operating costs have been averaging 8% of first cost for major equipment.
- Increased annual training costs and salary requirements for handling the new plastics and operating new equipment can range from \$800,000 to \$1.2 million.

There are two manufacturers working on the new-generation equipment. You label these options as alternatives A and B.

Case Study Exercises

1. Use the first four steps of the decision-making process to generally describe the alternatives and identify what economic-related estimates you will need to complete an engineering economy analysis for the president.
2. Identify any noneconomic factors and criteria to be considered in making the alternative selection.
3. During your inquiries about alternative B from its manufacturer, you learn that this company has already produced a prototype molding machine and has sold it to a company in Germany for

\$3 million (U.S. dollars). Upon inquiry, you further discover that the German company already has unused capacity on the equipment for manufacturing plastic shells. The company is willing to sell time on the equipment to Innovations immediately to produce its own shells for U.S. delivery. This could allow an earlier market entry into the United States. Consider this as alternative C, and develop the estimates necessary to evaluate C at the same time as alternatives A and B.