
PRACTICE SET

Questions

- Q6-1.** *Multiplexing* is the set of techniques that allows the simultaneous transmission of multiple signals across a single data link.
- Q6-3.** In *multiplexing*, the word *link* refers to the physical path. The word *channel* refers to the portion of a link that carries a transmission between a given pair of lines. One link can have many (n) channels.
- Q6-5.** To maximize the efficiency of their infrastructure, telephone companies have traditionally multiplexed analog signals from lower-bandwidth lines onto higher-bandwidth lines. The *analog hierarchy* uses voice channels (4 KHz), *groups* (48 KHz), *supergroups* (240 KHz), *master groups* (2.4 MHz), and *jumbo groups* (15.12 MHz).
- Q6-7.** WDM is common for multiplexing *optical signals* because it allows the multiplexing of signals with a very high frequency.
- Q6-9.** In *synchronous TDM*, each input has a reserved slot in the output frame. This can be inefficient if some input lines have no data to send. In *statistical TDM*, slots are dynamically allocated to improve bandwidth efficiency. Only when an input line has a slot's worth of data to send is it given a slot in the output frame.
- Q6-11** The *frequency hopping spread spectrum* (FHSS) technique uses M different carrier frequencies that are modulated by the source signal. At one moment, the signal modulates one carrier frequency; at the next moment, the signal modulates another carrier frequency.

Problems

- P6-1.** To multiplex 10 voice channels, we need nine guard bands. The required bandwidth is then $B = (4 \text{ KHz}) \times 10 + (500 \text{ Hz}) \times 9 = 44.5 \text{ KHz}$

P6-3.

- a. Group level: overhead = 48 KHz – (12 × 4 KHz) = 0 Hz.
- b. Supergroup level: overhead = 240 KHz – (5 × 48 KHz) = 0 Hz.
- c. Master group: overhead = 2520 KHz – (10 × 240 KHz) = 120 KHz.
- d. Jumbo Group: overhead = 16.984 MHz – (6 × 2.52 MHz) = 1.864 MHz.

P6-5.

- a. Each output frame carries 2 bits from each source plus one extra bit for synchronization. Frame size = $20 \times 2 + 1 = 41$ bits.
- b. Each frame carries 2 bit from each source. Frame rate = $100,000/2 = 50,000$ frames/s.
- c. Frame duration = $1 / (\text{frame rate}) = 1 / 50,000 = 20$ ms.
- d. Data rate = $(50,000 \text{ frames/s}) \times (41 \text{ bits/frame}) = 2.05$ Mbps. The output data rate here is slightly less than the one in Problem 4.
- e. In each frame 40 bits out of 41 are useful. Efficiency = $40/41 = 97.5\%$. Efficiency is better than the one in Problem 4.

P6-7. We combine six 200-kbps sources into three 400-kbps. Now we have seven 400-kbps channel.

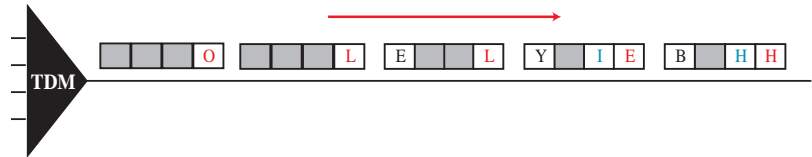
- a. Each output frame carries 1 bit from each of the seven 400-kbps line. Frame size = $7 \times 1 = 7$ bits.
- b. Each frame carries 1 bit from each 400-kbps source. Frame rate = 400,000 frames/s.
- c. Frame duration = $1 / (\text{frame rate}) = 1 / 400,000 = 2.5$ ms.
- d. Output data rate = $(400,000 \text{ frames/s}) \times (7 \text{ bits/frame}) = 2.8$ Mbps. We can also calculate the output data rate as the sum of input data rate because there is no synchronizing bits. Output data rate = $6 \times 200 + 4 \times 400 = 2.8$ Mbps.

P6-9. We need to add extra bits to the second source to make both rates = 190 kbps. Now we have two sources, each of 190 Kbps.

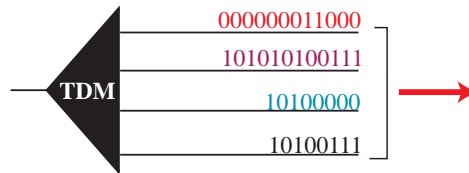
- a. The frame carries 1 bit from each source. Frame size = $1 + 1 = 2$ bits.
- b. Each frame carries 1 bit from each 190-kbps source. Frame rate = 190,000 frames/s.
- c. Frame duration = $1 / (\text{frame rate}) = 1 / 190,000 = 5.3$ ms.

- d. Output data rate = $(190,000 \text{ frames/s}) \times (2 \text{ bits/frame}) = 380 \text{ kbps}$. Here the output bit rate is greater than the sum of the input rates (370 kbps) because of extra bits added to the second source.

P6-11. See the following figure.



P6-13. See the following figure.



P6-15. The number of hops = $100 \text{ KHz} / 4 \text{ KHz} = 25$. So we need $\log_2 25 = 4.64 \approx 5$ bits

P6-17. Random numbers are 11, 13, 10, 6, 12, 3, 8, 9 as calculated below:

$$\begin{aligned}
 N_1 &= 11 \\
 N_2 &= (5 + 7 \times 11) \bmod 17 - 1 = 13 \\
 N_3 &= (5 + 7 \times 13) \bmod 17 - 1 = 10 \\
 N_4 &= (5 + 7 \times 10) \bmod 17 - 1 = 6 \\
 N_5 &= (5 + 7 \times 6) \bmod 17 - 1 = 12 \\
 N_6 &= (5 + 7 \times 12) \bmod 17 - 1 = 3 \\
 N_7 &= (5 + 7 \times 3) \bmod 17 - 1 = 8 \\
 N_8 &= (5 + 7 \times 8) \bmod 17 - 1 = 9
 \end{aligned}$$