

Assignment 12: Integration and Riemann Sums (4.1-4) Name _____
 Please provide a handwritten response.

1a. The \int command is used to find both indefinite and definite integrals. To find $\int (4x - 2\sqrt{x}) dx$ you enter $\int (4x - 2\sqrt{x}, x, c)$. Is the answer correct? Did the calculator record the $+C$?

1b. Next evaluate $F(x) = \int \frac{2x^3}{x^4 + 1} dx$ as $\int (2x^3 / (x^4 + 1), x, c)$ and record the results below.

1c. By definition of antiderivative, what should $F'(x)$ be? Differentiate your solution to **1b** using the $d()$ command (you can paste F' into this command as you did in **Assignment 10**) and record the result below. Is it correct?

2a. To approximate the area under the graph of $f(x) = \cos x$ on the interval $\left[0, \frac{\pi}{2}\right]$ graph $f(x)$ over $\left[0, \frac{\pi}{2}\right]$ and sketch the results below.



$$0 \leq x \leq \frac{\pi}{2}, 0 \leq y \leq 1$$

2b. Now use 50 rectangles to approximate the area under this curve. You will use the program **riemann()** to perform this approximation. You will need to place $y_1 = \cos x$ in your graphing menu. After exiting the graphing menu run the program by typing **riemann()**. You will need to enter $a = 0$, $b = \frac{\pi}{2}$, $n = 50$. Note that the program is using $\Delta x = \frac{b-a}{n}$. Record the value being used for Δx below.

2c. The Riemann sum for left-hand evaluation $\sum_{i=1}^n f(x_{i-1}) \Delta x$ can be found using **riemann()**. It is given as result **left sum** in the program **riemann()**. Is it a plausible approximation of the area? Record the result for left-hand evaluation below.

2d. The Riemann sum for right-hand evaluation $\sum_{i=1}^n f(x_i)\Delta x$ can be found using the same program. It is given as result **right sum** in the program. Run the program **riemann()** and record the result for right-hand evaluation below. Is your answer greater or less than your result in part **c**? Why should this be so?

2e. Likewise, the Riemann sum for midpoint evaluation $\sum_{i=1}^n f\left[\frac{1}{2}(x_{i-1} + x_i)\right]\Delta x$ can be found using the same program by pressing enter again. It is given as result **mid sum** in the program **riemann()**. Record the result for midpoint evaluation below.

2f. Now approximate the area using 100 rectangles. To rerun the program after you quit, press **ENTER** with **riemann()** in the entry line (you should not have to retype it) and the program will again prompt you to enter **a**, **b**, and **n**. This time enter **n=100** and record the three results below. Do the three approximations in parts **c-e** become more spread out or closer together? Is this what you would expect?¹

3. The exact value of the area you approximated can be found using the definite integral $\int_0^{\pi/2} \cos x \, dx$. The definite integral is found using the \int command. Execute $\int(\cos(x), x, 0, \pi / 2)$ and record the results below. Based on the evidence you have already gathered, is this answer plausible?

¹ The Trapezoidal Rule and Simpson's rule for Assignment 13 are included in this program. Bypass them by pressing ENTER twice and use 2nd QUIT to exit the program.