## Appendix C: Answers

## Answers to Odd-Numbered Chapter Exercises

CHAPTER 1

1. a. Interval
b. Ratio
c. Nominal
d. Nominal
e. Ordinal
f. Ratio
2. Answers will vary.
3. Qualitative data is not numerical, whereas quantitative data is numerical. Examples will vary by student.
4. A discrete variable may assume only certain values. A continuous variable may assume an infinite number of values within a given range. The number of traffic citations issued each day during February in Garden City Beach, South Carolina, is a discrete variable. The weight of commercial trucks passing the weigh station at milepost 195 on Interstate 95 in North Carolina is a continuous variable.
5. a. Ordinal
b. Interval
c. The newer system provides information on the distance between exits.
6. If you were using this store as typical of all Barnes \& Noble stores, then it would be sample data. However, if you were considering it as the only store of interest, then the data would represent the population.
7. 

|  | Discrete Variable | Continuous Variable |
| :--- | :--- | :--- |
| Qualitative | b. Gender <br> d. Soft drink preference |  |
| Quantitative | f. SAT scores <br> g. Student rank in class <br> h. Rating of a finance <br> professor <br> i. Number of home <br> computers | a. Salary <br> c. Sales volume of <br> MP3 players <br> e. Temperature |


|  | Discrete | Continuous |
| :--- | :--- | :--- |
| Nominal | b. Gender |  |
| Ordinal | d. Soft drink preference <br> g. Student rank in class <br> h. Rating of a finance <br> professor |  |
| Interval | f. SAT scores | e. Temperature |
| Ratio | i. Number of home <br> computers | a. Salary <br> c. Sales volume of <br> MP3 players |

15. According to the sample information, $120 / 300$ or $40 \%$ would accept a job transfer.
16. a. Total sales increased by 106,041 , found by $1,255,337$ $1,149,296$, which is a $9.2 \%$ increase.
b. Market shares are:

|  | $\mathbf{2 0 1 0}$ | $\mathbf{2 0 0 9}$ |
| :--- | ---: | ---: |
| General Motors | $22.9 \%$ | $22.0 \%$ |
| Ford Motor | $19.9 \%$ | $16.2 \%$ |
| Chrysler | $11.3 \%$ | $12.7 \%$ |
| Toyota | $15.8 \%$ | $19.7 \%$ |
| American Honda | $11.8 \%$ | $12.4 \%$ |
| Nissan NA | $10.6 \%$ | $9.4 \%$ |
| Hyundai | $5.1 \%$ | $4.8 \%$ |
| Mazda | $2.6 \%$ | $2.8 \%$ |

Ford has gained 3.7\% and Toyota lost 3.9\% of their market shares.
c. Percentage changes are:

| General Motors | increase of $13.7 \%$ |
| :--- | :--- |
| Ford Motor | increase of $34.3 \%$ |
| Chrysler | decrease of $3.2 \%$ |
| Toyota | decrease of $12.4 \%$ |
| American Honda | increase of $3.9 \%$ |
| Nissan NA | increase of $22.8 \%$ |
| Hyundai | increase of $17.0 \%$ |
| Mazda |  |

Ford and Nissan had increases of more than 20\%. General Motors and Hyundai had increases of more than $10 \%$. Meanwhile, Toyota had a decrease of over 10\%.
19. Earnings increased each year over the previous year until a large peak in 2008. Then there was a rather large drop in 2009. Earnings increased again in 2010.
21. a. League is a qualitative variable; the others are quantitative.
b. League is a nominal-level variable; the others are ratiolevel variables.

CHAPTER 2
3.

25\% market share

| Season | Frequency | Relative Frequency |
| :--- | :---: | :---: |
| Winter | 100 | .10 |
| Spring | 300 | .30 |
| Summer | 400 | .40 |
| Fall | $\underline{200}$ | $\underline{.20}$ |
|  | 1,000 | 1.00 |

5. a. A frequency table.

| Color | Frequency | Relative Frequency |
| :--- | :---: | :---: |
| Bright White | 130 | 0.10 |
| Metallic Black | 104 | 0.08 |
| Magnetic Lime | 325 | 0.25 |
| Tangerine Orange | 455 | 0.35 |
| Fusion Red | $\underline{286}$ | $\underline{0.22}$ |
| Total | 1,300 | 1.00 |

b.

c.

d. 350,000 orange, 250,000 lime, 220,000 red, 100,000 white, and 80,000 black, found by multiplying relative frequency by $1,000,000$ production.
7. $2^{5}=32,2^{6}=64$, therefore, 6 classes
9. $2^{7}=128,2^{8}=256$, suggests 8 classes $i \geq \frac{\$ 567-\$ 235}{8}=41 \quad$ Class intervals of 45 or 50 would be acceptable.
11. a. $2^{4}=16$ Suggests 5 classes.
b. $i \geq \frac{31-25}{5}=1.2$ Use interval of 1.5 .
c. 24
d.

| Units | $\boldsymbol{f}$ | Relative Frequency |
| :---: | :---: | :---: |
| 24.0 up to 25.5 | 2 | 0.125 |
| 25.5 up to 27.0 | 4 | 0.250 |
| 27.0 up to 28.5 | 8 | 0.500 |
| 28.5 up to 30.0 | 0 | 0.000 |
| 30.0 up to 31.5 | $\frac{2}{16}$ | $\underline{0.125}$ |
| $\quad$ Total | $\mathbf{1 . 0 0 0}$ |  |

e. The largest concentration is in the 27.0 up to 28.5 class (8).
13.

a. \begin{tabular}{|cr|}

\hline | Number of |
| :---: |
| Visits | \& $\boldsymbol{f}$ <br>

\hline 0 up to 3 \& 9 <br>
3 up to 6 \& 21 <br>
6 up to 9 \& 13 <br>
9 up to 12 \& 4 <br>
12 up to 15 \& 3 <br>
15 up to 18 \& $\mathbf{1}$ <br>
Total \& 51 <br>
\hline
\end{tabular}

b. The largest group of shoppers (21) shop at the BiLo Supermarket 3, 4 , or 5 times during a month period. Some customers visit the store only 1 time during the month, but others shop as many as 15 times.
c.

| Number of <br> Visits | Percent <br> of Total |
| :---: | ---: |
| 0 up to 3 | 17.65 |
| 3 up to 6 | 41.18 |
| 6 up to 9 | 25.49 |
| 9 up to 12 | 7.84 |
| 12 up to 15 | 5.88 |
| 15 up to 18 | 1.96 |
| Total | 100.00 |

15. a. Histogram
b. 100
c. 5
d. 28
e. 0.28
f. 12.5
g. 13
16. a. 50
b. 1.5 thousand miles, or 1,500 miles.
c.

d. $X=1.5, Y=5$
e.

f. For the 50 employees, about half traveled between 6,000 and 9,000 miles. Five employees traveled less than 3,000 miles, and 2 traveled more than 12,000 miles.
17. a. 40
b. 5
c. 11 or 12
d. About $\$ 20 / \mathrm{hr}$
e. About $\$ 9 / \mathrm{hr}$
f. About $75 \%$
18. a. 5
b.

| Frequent <br> Flier Miles | $\boldsymbol{f}$ | $\mathbf{C F}$ |
| ---: | ---: | ---: |
| 0 up to 3 | 5 | 5 |
| 3 up to 6 | 12 | 17 |
| 6 up to 9 | 23 | 40 |
| 9 up to 12 | 8 | 48 |
| 12 up to 15 | 2 | 50 |


d. About 8.7 thousand miles
23. a. A qualitative variable uses either the nominal or ordinal scale of measurement. It is usually the result of counts. Quantitative variables are either discrete or continuous. There is a natural order to the results for a quantitative variable. Quantitative variables can use either the interval or ratio scale of measurement.
b. Both types of variables can be used for samples and populations.
25. a. Frequency table
b.


d. A pie chart would be better because it clearly shows that nearly half of the customers prefer no planned activities.
27. $2^{6}=64$ and $2^{7}=128$, suggest 7 classes
29. a. 5 , because $2^{4}=16<25$ and $2^{5}=32>25$
b. $i \geq \frac{48-16}{5}=6.4 \quad$ Use interval of 7 .
c. 15
d.

| Class | Frequency |  |
| :---: | :--- | ---: |
| 15 up to 22 | III | 3 |
| 22 up to 29 | HY III | 8 |
| 29 up to 36 | HY II | 7 |
| 36 up to 43 | HI | 5 |
| 43 up to 50 | II | $\underline{2}$ |
|  |  | 25 |

e. It is fairly symmetric, with most of the values between 22 and 36.
31. a. $2^{5}=32,2^{6}=64,6$ classes recommended.
b. $i=\frac{10-1}{6}=1.5$, use an interval of 2 .
c. 0
d.

| Class | Frequency |
| :---: | :---: |
| 0 up to | 2 |
| 2 up to | 4 |
| 4 up to | 6 |
| 6 up to | 8 |
| 8 up to 10 | 12 |
|  | 17 |

e. The distribution is fairly symmetric or bell-shaped with a large peak in the middle of the two classes of 4 up to 8 .

| Class | Frequency |
| :---: | :---: |
| 0 up to 200 | 19 |
| 200 up to 400 | 1 |
| 400 up to 600 | 4 |
| 600 up to 800 | 1 |
| 800 up to 1000 | 2 |

This distribution is positively skewed with a large "tail" to the right or positive values. Notice that the top 7 tunes account for 4,342 plays out of a total of 5,968 or about $73 \%$ of all plays.
35.
a. 56
b. 10 (found by $60-50$ )
c. 55
d. 17
37. a. $\$ 30.50$, found by $(\$ 265-\$ 82) / 6$
b. $\$ 35$
c.

| $\$ 70$ up to $\$ 105$ | 4 |  |
| ---: | ---: | ---: |
| 105 up to | 140 | 17 |
| 140 up to | 175 | 14 |
| 175 up to | 210 | 2 |
| 210 up to | 245 | 6 |
| 245 up to | 280 | 1 |

d. The purchases range from a low of about $\$ 70$ to a high of about $\$ 280$. The concentration is in the $\$ 105$ up to $\$ 140$ and $\$ 140$ up to $\$ 175$ classes.
39.

41.


| SC Income | Percent | Cumulative |
| :--- | :---: | :---: |
| Wages | 73 | 73 |
| Dividends | 11 | 84 |
| IRA | 8 | 92 |
| Pensions | 3 | 95 |
| Social Security | 2 | 97 |
| Other | 3 | 100 |

By far the largest part of income in South Carolina is wages. Almost three-fourths of the adjusted gross income comes from wages. Dividends and IRAs each contribute roughly another 10\%.
43. a. Since $2^{6}=64<70<128=2^{7}, 7$ classes are recommended. The interval should be at least $(1,002.2-3.3) / 7=$ 142.7. Use 150 as a convenient value.

| Frequency Distribution |  |
| :--- | ---: |
| 0 up to 150 | 28 |
| 150 up to 300 | 19 |
| 300 up to 450 | 15 |
| 450 up to 600 | 2 |
| 600 up to 750 | 4 |
| 750 up to 1050 | $\underline{1}$ |
| Total | 70 |

b.

45. a. Pie chart
b. 215 , found by $0.43 \times 500$
c. Seventy-eight percent are in either a house of worship (43\%) or outdoors (35\%).
47. a.

b. $0.42 ;(63.9+31.6) / 224.9$
c. $0.75 ;(63.9+31.6) / 127.0$
49.

| Color | Frequency |
| :--- | :---: |
| Brown | 130 |
| Yellow | 98 |
| Red | 96 |
| Blue | 52 |
| Orange | 35 |
| Green | $\underline{33}$ |
|  | 444 |



Brown, yellow, and red M\&M's make up almost 75 percent. The other 25 percent are blue, orange, and green.
51. $i \geq \frac{345.3-125.0}{7}=31.47$ Use interval of 35 .

| Selling Price | $\boldsymbol{f}$ | $\boldsymbol{C F}$ |
| :--- | ---: | ---: |
| 110 up to 145 | 3 | 3 |
| 145 up to 180 | 19 | 22 |
| 180 up to 215 | 31 | 53 |
| 215 up to 250 | 25 | 78 |
| 250 up to 285 | 14 | 92 |
| 285 up to 320 | 10 | 102 |
| 320 up to 355 | 3 | 105 |

a. Most homes ( $53 \%$ ) are in the 180 up to 250 range.
b. $\$ 127.5(110+17.5) ; \$ 337.5(320+17.5)$
c.


About 42 homes sold for less than 200.
About 55\% of the homes sold for less than 220. So $45 \%$ sold for more. Less than $1 \%$ of the homes sold for less than 125.
d.


Townships 3 and 4 have more sales than the average and Townships 1 and 5 have somewhat less than the average.
53. Since $2^{6}=64<80<128=2^{7}$, use 7 classes. The interval should be at least $(1008-741) / 7=38.14$ miles. Use 40. The resulting frequency distribution is:

| Class | $\boldsymbol{f}$ |
| :--- | ---: |
| 730 up to 770 | 5 |
| 770 up to 810 | 17 |
| 810 up to 850 | 37 |
| 850 up to 890 | 18 |
| 890 up to 930 | 1 |
| 930 up to 970 | 0 |
| 970 up to 1010 | 2 |

a. The typical amount driven is 830 miles. The range is from 730 up to 1010 miles
b. The distribution is "bell shaped" around 830 . However, there are two outliers up around 1000 miles.
c.

Cumulative Frequency of Miles Driven per Month


Forty percent of the buses were driven fewer than 820 miles.
Fifty-nine buses were driven less than 850 miles.
d.

Pie Chart of Bus Type


Pie Chart of Seats


The first chart shows that about two-thirds of the buses are diesel. The second diagram shows that nearly three fourths of the buses have 55 seats.

## CHAPTER 3

1. $\mu=5.4$, found by $27 / 5$
2. a. $\bar{X}=7.0$, found by $28 / 4$
b. $(5-7)+(9-7)+(4-7)+(10-7)=0$
3. $\bar{X}=14.58$, found by $43.74 / 3$
4. a. 15.4 , found by $154 / 10$
b. Population parameter, since it includes all the salespeople at Midtown Ford
5. a. $\$ 54.55$, found by $\$ 1,091 / 20$
b. A sample statistic-assuming that the power company serves more than 20 customers
6. $\bar{X}=\frac{\sum X}{n}$ so
$\Sigma X=\bar{X} \cdot n=(\$ 5430)(30)=\$ 162,900$
7. $\$ 22.91$, found by $\frac{300(\$ 20)+400(\$ 25)+400(\$ 23)}{300+400+400}$
8. $\$ 17.75$, found by $(\$ 400+\$ 750+\$ 2,400) / 200$
9. a. No mode
b. The given value would be the mode.
c. 3 and 4 bimodal
10. a. Mean $=3.33$
b. Median = 5
c. Mode $=5$
11. a. Median $=2.9$
b. Mode $=2.9$
12. $\bar{X}=\frac{647}{11}=58.82$

Median $=58$, Mode $=58$
Any of the three measures would be satisfactory.
25. a. $\bar{X}=\frac{90.4}{12}=7.53$
b. Median $=7.45$. There are several modes: $6.5,7.3,7.8$, and 8.7.
c. $\bar{X}=\frac{33.8}{4}=8.45$,

Median $=8.7$
About 1 percentage point higher in Winter
27. a. 7 , found by $10-3$.
b. 6 , found by $30 / 5$.
c. 2.4 , found by $12 / 5$.
d. The difference between the highest number sold (10) and the smallest number sold (3) is 7 . On average, the number of HDTVs sold deviates by 2.4 from the mean of 6 .
29. a. 30 , found by $54-24$.
b. 38 , found by $380 / 10$.
c. 7.2 , found by $72 / 10$.
d. The difference of 54 and 24 is 30 . On average, the number of minutes required to install a door deviates 7.2 minutes from the mean of 38 minutes.
31.

| State | Mean | Median | Range |
| :--- | :---: | :---: | :---: |
| California | 33.10 | 34.0 | 32 |
| lowa | 24.50 | 25.0 | 19 |

The mean and median ratings were higher for California, but there was also more variation in California.
33. a. 5
b. 4.4 , found by
$\frac{(8-5)^{2}+(3-5)^{2}+(7-5)^{2}+(3-5)^{2}+(4-5)^{2}}{5}$
35. a. $\$ 2.77$
b. 1.26 , found by
$(2.68-2.77)^{2}+(1.03-2.77)^{2}+(2.26-2.77)^{2}$
$+(4.30-2.77)^{2}+(3.58-2.77)^{2}$ $\frac{+(4.30-2.77)^{2}+(3.58-2.77)^{2}}{5}$
37. a. Range: 7.3, found by $11.6-4.3$. Arithmetic mean: 6.94 , found by $34.7 / 5$. Variance: 6.5944 , found by $32.972 / 5$.
Standard deviation: 2.568, found by $\sqrt{6.5944}$.
b. Dennis has a higher mean return $(11.76>6.94)$. However, Dennis has greater spread in its returns on equity $(16.89>6.59)$.
39. a. $\bar{X}=4$

$$
s^{2}=\frac{(7-4)^{2}+\cdots+(3-4)^{2}}{5-1}=\frac{22}{5-1}=5.5
$$

b. $s=2.3452$
41. a. $\bar{X}=38$

$$
\begin{aligned}
& s^{2}=\frac{(28-38)^{2}+\cdots+(42-38)^{2}}{10-1}=82.667 \\
& s^{2}=\frac{744}{10-1}=82.667
\end{aligned}
$$

b. $s=9.0921$
43. a. $\bar{X}=\frac{951}{10}=95.1$

$$
\begin{aligned}
s^{2} & =\frac{(101-95.1)^{2}+\cdots+(88-95.1)^{2}}{10-1} \\
& =\frac{1,112.9}{9}=123.66
\end{aligned}
$$

b. $s=\sqrt{123.66}=11.12$
45. About $69 \%$, found by $1-1 /(1.8)^{2}$
47. a. About $95 \%$
b. $47.5 \%, 2.5 \%$
49. a. Mean $=5$, found by $(6+4+3+7+5) / 5$.

Median is 5 , found by rearranging the values and selecting the middle value.
b. Population, because all partners were included
c. $\Sigma(X-\mu)=(6-5)+(4-5)+(3-5)+(7-5)+$ $(5-5)=0$
51. $\bar{X}=\frac{545}{16}=34.06$

Median $=37.50$
53. The mean is 35.675 , found by $1427 / 40$.

The median is 36 , found by sorting the data and averaging the 20th and 21st observations.
55. $\bar{X}_{w}=\frac{\$ 5.00(270)+\$ 6.50(300)+\$ 8.00(100)}{270+300+100}=\$ 6.12$
$\begin{aligned} & \text { 57. } \\ & \text { 59. }\end{aligned} \bar{X}_{w}=\frac{[15,300(4.5)+10,400(3.0)+150,600(10.2)]}{176,300}=9.28$
59.
a. 55, found by $72-17$
b. 14.4 , found by $144 / 10$, where $\bar{X}=43.2$
c. 17.6245
61. a. There were 13 flights, so all items are considered.
b. $\mu=\frac{2,259}{13}=173.77$

Median $=195$
c. Range $=301-7=294$

$$
s=\sqrt{\frac{133,846}{13}}=101.47
$$

63. a. The mean is $\$ 717.20$, found by $\$ 17,930 / 25$. The median is $\$ 717.00$ and there are two modes, $\$ 710$ and $\$ 722$.
b. The range is $\$ 90$, found by $\$ 771-\$ 681$, and the standard deviation is $\$ 24.87$, found by the square root of $14,850 / 24$.
c. From $\$ 667.46$ up to $\$ 766.94$, found by $\$ 717.20$ $\pm 2(\$ 24.87)$.
64. a. Mean $=9.1$, found by $273 / 30$. Median is 9 , found by averaging the 15th and 16th values.
b. Range $=14$, found by $18-4$. Standard deviation $=$ 3.566 , found by the square root of (368.7/29).
65. a. The mean team payroll is $\$ 91,016,667$, rounded to $\$ 91.0$ million. The median is $\$ 84,300,000$, rounded to $\$ 84.3$ million. Since the distribution is positively skewed, the median is a better measure of location.
b. The range is $\$ 171,400,000$, or $\$ 171.4$ million. The standard deviation is $\$ 38,254,935$, or $\$ 38.3$ million. Using the data rounded to the nearest $\$ 0.1$ million, $75 \%$ of the team payrolls are between $\$ 14.4$ million and $\$ 167.6$ million.
c. The AL mean and standard deviation are $\$ 96,992,857$, or $\$ 98.0$ million, and $\$ 43,724,812$, or $\$ 43.7$ million. The NL mean and standard deviation are $\$ 85,787,500$, or $\$ 85.8$ million, and $\$ 33,314,739$, or $\$ 33.3$ million. The AL team payroll has a larger mean and more dispersion.

## CHAPTER 4

1. a. Dot plot
b. 15
c. 1,7
d. 2 and 3
2. Median $=53$, found by $(11+1)\left(\frac{1}{2}\right) \therefore 6$ th value in from lowest $Q_{1}=49$, found by $(11+1)\left(\frac{1}{4}\right) \therefore$ 3rd value in from lowest $Q_{3}=55$, found by $(11+1)\left(\frac{3}{4}\right) \therefore$ 9th value in from lowest
3. a. $Q_{1}=33.25, Q_{3}=50.25$
b. $D_{2}=27.8, D_{8}=52.6$
c. $P_{67}=47$
4. a. 350
b. $Q_{1}=175, Q_{3}=930$
c. $930-175=755$
d. Less than 0 , or more than about 2,060
e. There are no outliers.
f. The distribution is positively skewed.
5. 



The distribution is somewhat positively skewed. Note that the dashed line above 35 is longer than below 18.
11. a. The mean is 30.8 , found by $154 / 5$. The median is 31.0 , and the standard deviation is 3.96 , found by

$$
s=\sqrt{\frac{62.8}{4}}=3.96
$$

b. -0.15 , found by $\frac{3(30.8-31.0)}{3.96}$
c.

| Salary | $\left(\frac{(\boldsymbol{X}-\overline{\boldsymbol{X}})}{\boldsymbol{s}}\right)$ | $\left(\frac{(\boldsymbol{X}-\overline{\boldsymbol{X}})}{\boldsymbol{s}}\right)^{3}$ |
| :---: | ---: | ---: |
| 36 | 1.313131 | 2.264250504 |
| 26 | -1.212121 | -1.780894343 |
| 33 | 0.555556 | 0.171467764 |
| 28 | -0.707071 | -0.353499282 |
| 31 | 0.050505 | 0.000128826 |
|  |  | 0.301453469 |

0.125 , found by $[5 /(4 \times 3)] \times 0.301$
13. a. The mean is 21.93 , found by $328.9 / 15$. The median is 15.8 , and the standard deviation is 21.18 , found by

$$
s=\sqrt{\frac{6283}{14}}=21.18
$$

b. 0.868 , found by $[3(21.93-15.8)] / 21.18$
c. 2.444 , found by $[15 /(14 \times 13)] \times 29.658$
15.


There is a positive relationship between the variables.
17. a. Both variables are nominal scale.
b. Contingency table
c. Men are about twice as likely to order a dessert. From the table, $32 \%$ of the men ordered dessert, but only $15 \%$ of the women.
19. a. Dot plot
b. 15
c. 5
21. a. $L_{50}=(20+1) \frac{50}{100}=10.50$

Median $=\frac{83.7+85.6}{2}=84.65$
$L_{25}=(21)(.25)=5.25$
$Q_{1}=66.6+.25(72.9-66.6)=68.175$
$L_{75}=21(.75)=15.75$
$Q_{3}=87.1+.75(90.2-87.1)=89.425$
b. $L_{26}=21(.26)=5.46$
$P_{26}=66.6+.46(72.9-66.6)=69.498$
$L_{83}=21(.83)=17.43$
$P_{83}=93.3+.43(98.6-93.3)=95.579$
c.

23. a. $Q_{1}=26.25, Q_{3}=35.75$, Median $=31.50$
$\qquad$
b. $Q_{1}=33.25, Q_{3}=38.75$, Median $=37.50$

c. The median time for public transportation is about 6 minutes less. There is more variation in public
transportation. The difference between $Q_{1}$ and $Q_{3}$ is 9.5 minutes for public transportation and 5.5 minutes for private transportation.
25. The distribution is positively skewed. The first quartile is about $\$ 20$ and the third quartile is about $\$ 90$. There is one outlier located at $\$ 255$. The median is about $\$ 50$.
27. a.


Median is 3733 . First quartile is 1478 . Third quartile is 6141 . So prices over $13,135.5$, found by $6141+1.5$ (6141-1478), are outliers. There are three ( 13,925 , 20,413, and 44,312).
b.


Median is 0.84 . First quartile is 0.515 . Third quartile is 1.12. So sizes over 2.0275, found by $1.12+1.5$ (1.12 $0.515)$, are outliers. There are three $(2.03,2.35$, and 5.03).
c.


There is a direct association between them. The first observation is larger on both scales.
d.

| Shapel <br> Cut | Average | Good | Ideal | Premium | Ultra <br> Ideal | All |
| :--- | :---: | :---: | :---: | :---: | :---: | ---: |
| Emerald | 0 | 0 | 1 | 0 | 0 | 1 |
| Marquise | 0 | 2 | 0 | 1 | 0 | 3 |
| Oval | 0 | 0 | 0 | 1 | 0 | 1 |
| Princess | 1 | 0 | 2 | 2 | 0 | 5 |
| Round | $\frac{1}{2}$ | $\frac{3}{3}$ | $\frac{3}{2}$ | $\frac{13}{17}$ | $\frac{3}{3}$ | $\frac{23}{33}$ |
| $\quad$ Total | $\frac{2}{5}$ | 5 | $\frac{1}{6}$ |  | 3 |  |

The majority of the diamonds are round (23). Premium cut is most common (17). The Round Premium combination occurs most often (13).
29. $s k=0.065$ or $s k=\frac{3(7.7143-8.0)}{3.9036}=-0.22$
31.

Scatterplot of Accidents versus Age


As age increases, the number of accidents decreases.
33. a. 139,340,000
b. $5.4 \%$ unemployed, found by $(7523 / 139,340) 100$
c. $\mathrm{Men}=5.64 \%$

Women = 5.12\%
35. a.


There are five outliers. There is a group of three around 50 years (Angels, Athletics, and Dodgers) and a group of two close to 100 years old (Cubs and Red Sox).
b.


Using equation 4-1 (if using Excel, see software commands) and rounding to the nearest $\$ 0.1$ million, the first quartile is $\$ 61.4$ million, the third quartile is $\$ 105.8$ million. The distribution is positively skewed, with the New York Yankees a definite outlier.
c.

## Scatter Diagram of Wins vs. Payroll



Higher payrolls lead to more wins.
d.


The distribution is fairly uniform between 57 and 97 .

CHAPTER 5

1. |  | Person |  |
| :---: | :---: | :---: |
|  | Outcome | $\mathbf{1}$ |
| $\mathbf{2}$ |  |  |
| 1 | A | A |
| 2 | A | F |
| 3 | F | A |
| 4 | F | F |
2. a. .176, found by $\frac{6}{34} \quad$ b. Empirical
3. a. Empirical
b. Classical
c. Classical
d. Empirical, based on seismological data
4. a. The survey of 40 people about environmental issues
b. 26 or more respond yes, for example.
c. $10 / 40=.25$
d. Empirical
e. The events are not equally likely, but they are mutually exclusive.
5. a. Answers will vary. Here are some possibilities: $123,124,125,999$
b. $(1 / 10)^{3}$
c. Classical
6. $P(A$ or $B)=P(A)+P(B)=.30+.20=.50$ $P($ neither $)=1-.50=.50$.
7. a. $102 / 200=.51$
b. .49 , found by $61 / 200+37 / 200=.305+.185$.

Special rule of addition.
15. $P($ above $C)=.25+.50=.75$
17. $P(A$ or $B)=P(A)+P(B)-P(A$ and $B)$

$$
=.20+.30-.15=.35
$$

19. When two events are mutually exclusive, it means that if one occurs, the other event cannot occur. Therefore, the probability of their joint occurrence is zero.
20. a. $P(P$ and $F)=0.20$
b. $P(P$ and $D)=0.30$
c. No
d. Joint probability
e. $P(P$ or $D$ or $F)=1-P(P$ and $D$ and $F)$

$$
=1-.10=.90
$$

23. $P(A$ and $B)=P(A) \times P(B \mid A)=.40 \times .30=.12$
24. . 90 , found by $(.80+.60)-.5$.
.10 , found by ( $1-.90$ ).
25. a. $P\left(A_{1}\right)=3 / 10=.30$
b. $P\left(B_{1} \mid A_{2}\right)=1 / 3=.33$
c. $P\left(B_{2}\right.$ and $\left.A_{3}\right)=1 / 10=.10$
26. a. A contingency table
b. .27 , found by $300 / 500 \times 135 / 300$
c. The tree diagram would appear as:

27. a. Contingency table
b. 0.842 , found by $32 / 38$
c. Independence requires that $P(A \mid B)=P(A)$. One possibility is: $P($ Good I 20 up to 30 yards $)=P($ Good $)$. Does $12 / 12=32 / 38$ ? No, the two variables are not independent.
d. 0.895 , found by $12 / 38+32 / 38-10 / 38$
e. 0.026 , found by $1 / 38$
28. a. $78,960,960$
b. 840 , found by $(7)(6)(5)(4)$. That is $7!/ 3$ !
c. 10 , found by $5!/ 3!2$ !
29. 210 , found by (10)(9)(8)(7)/(4)(3)(2)
30. 120 , found by 5 !
31. $10,897,286,400$, found by ${ }_{15} P_{10}=(15)(14)(13)(12)(11)(10)(9)(8)(7)(6)$
32. a. Asking teenagers to compare their reactions to a newly developed soft drink.
b. Answers will vary. One possibility is more than half of the respondents like it.
33. Subjective
34. a. $4 / 9$, found by $(2 / 3) \cdot(2 / 3)$.
b. $3 / 4$, because $(3 / 4) \cdot(2 / 3)=0.5$.
35. a. .8145 , found by $(.95)^{4}$
b. Special rule of multiplication
c. $P(A$ and $B$ and $C$ and $D)=P(A) \times P(B) \times P(C) \times P(D)$
36. a. .08 , found by $.80 \times .10$
b. No; $90 \%$ of females attended college, $78 \%$ of males c.

d. Yes, because all the possible outcomes are shown on the tree diagram.
37. a. 0.57 , found by $57 / 100$
b. 0.97 , found by $(57 / 100)+(40 / 100)$
c. Yes, because an employee cannot be both.
d. 0.03 , found by $1-0.97$
38. a. $1 / 2$, found by $(2 / 3)(3 / 4)$
b. $1 / 12$, found by $(1 / 3)(1 / 4)$
c. $11 / 12$, found by $1-1 / 12$
39. a. 0.9039 , found by $(0.98)^{5}$
b. 0.0961 , found by $1-0.9039$
40. a. 0.0333 , found by $(4 / 10)(3 / 9)(2 / 8)$
b. 0.1667 , found by $(6 / 10)(5 / 9)(4 / 8)$
c. 0.8333 , found by $1-0.1667$
d. Dependent
41. a. 0.3818 , found by $(9 / 12)(8 / 11)(7 / 10)$
b. 0.6182 , found by $1-0.3818$
42. a. $P(\mathrm{~S}) \cdot P(\mathrm{R} \mid \mathrm{S})=.60(.85)=0.51$
b. $P(\mathrm{~S}) \cdot P(\mathrm{PR} \mid \mathrm{S})=.60(1-.85)=0.09$
43. a. $P($ not perfect $)=P$ (bad sector) $+P$ (defective)

$$
=\frac{112}{1,000}+\frac{31}{1,000}=.143
$$

b. $P($ defective $\mid$ not perfect $)=\frac{.031}{.143}=.217$
65. a. $P(P$ or D$)=(1 / 50)(9 / 10)+(49 / 50)(1 / 10)=0.116$
b. $P(\mathrm{No})=(49 / 50)(9 / 10)=0.882$
c. $P($ No on 3$)=(0.882)^{3}=0.686$
d. $P($ at least one prize $)=1-0.686=0.314$
67. Yes, 256 is found by $2^{8}$.
69. .9744, found by $1-(.40)^{4}$
71. a. .185, found by (.15)(.95) + (.05)(.85)
b. 0075 , found by (.15)(.05)
73. a. $P(F$ and $>60)=.25$, found by solving with the general rule of multiplication:
$P(F) \cdot P(>60 \mid F)=(.5)(.5)$
b. 0
c. 3333 , found by $1 / 3$
75. $26^{4}=456,976$
77. 0.512 , found by $(0.8)^{3}$
79. .525, found by $1-(.78)^{3}$
81. a.

| Winning | Attendance |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| Season | Low | Moderate | High | Total |
| No | 6 | 5 | 3 | 14 |
| Yes | $\frac{3}{9}$ | $\frac{7}{12}$ | $\frac{6}{9}$ | $\frac{16}{30}$ |
| Total | 9 |  |  |  |

1. 0.5333 , found by $16 / 30$
2. 0.6333 , found by $16 / 30+9 / 30-6 / 30=19 / 30$
3. 0.6777 , found by $6 / 9$
4. 0.1000 , found by $3 / 30$
b.

|  | Losing <br> Season | Winning <br> Season | Total |
| :--- | :---: | :---: | :---: |
| New | 7 | 8 | 15 |
| Old | $\frac{7}{14}$ | $\frac{8}{16}$ | $\frac{15}{30}$ |
| Total |  |  |  |

1. 0.5333 , found by $16 / 30$
2. 0.2667 , found by $8 / 30$
3. 0.7667 , found by $16 / 30+15 / 30-8 / 30$

## CHAPTER 6

1. Mean $=1.3$, variance $=.81$, found by:

$$
\begin{aligned}
\mu= & 0(.20)+1(.40)+2(.30)+3(.10)=1.3 \\
\sigma^{2}= & (0-1.3)^{2}(.2)+(1-1.3)^{2}(.4) \\
& +(2-1.3)^{2}(.3)+(3-1.3)^{2}(.1) \\
= & .81
\end{aligned}
$$

3. Mean $=14.5$, variance $=27.25$, found by:

$$
\begin{aligned}
\mu= & 5(.1)+10(.3)+15(.2)+20(.4)=14.5 \\
\sigma^{2}= & (5-14.5)^{2}(.1)+(10-14.5)^{2}(.3) \\
& +(15-14.5)^{2}(.2)+(20-14.5)^{2}(.4) \\
= & 27.25
\end{aligned}
$$

5. a.

| Calls, <br> $\boldsymbol{x}$ | Frequency | $\boldsymbol{P}(\boldsymbol{x})$ | $\boldsymbol{x} \boldsymbol{P}(\boldsymbol{x})$ | $(\boldsymbol{x}-\boldsymbol{\mu})^{\mathbf{2}}$ <br> $\boldsymbol{P}(\boldsymbol{x})$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 8 | .16 | 0 | .4624 |
| 1 | 10 | .20 | .20 | .0980 |
| 2 | 22 | .44 | .88 | .0396 |
| 3 | 9 | .18 | .54 | .3042 |
| 4 | $\frac{1}{50}$ | .02 | $\underline{.08}$ | $\underline{.1058}$ |
|  | 50 |  | 1.70 | 1.0100 |

b. Discrete distribution, because only certain outcomes are possible.
c. $\mu=\Sigma x \cdot P(x)=1.70$
d. $\sigma=\sqrt{1.01}=1.005$
7.

| Amount | $\boldsymbol{P}(\boldsymbol{x})$ | $\boldsymbol{x P}(\boldsymbol{x})$ | $(\boldsymbol{x}-\boldsymbol{\mu})^{2} \boldsymbol{P}(\boldsymbol{x})$ |
| :---: | :---: | :---: | :---: |
| 10 | .50 | 5 | 60.50 |
| 25 | .40 | 10 | 6.40 |
| 50 | .08 | 4 | 67.28 |
| 100 | .02 | $\underline{2}$ | $\underline{124.82}$ |
|  |  | $\underline{21}$ | 259.00 |

a. $\mu=\Sigma x P(x)=21$
b. $\sigma^{2}=\Sigma(x-\mu)^{2} P(x)=259$
$\sigma=\sqrt{259}=16.093$
9. a. $P(2)=\frac{4!}{2!(4-2)!}(.25)^{2}(.75)^{4-2}=.2109$
b. $P(3)=\frac{4!}{3!(4-3)!}(.25)^{3}(.75)^{4-3}=.0469$
11. a.

| $\boldsymbol{X}$ | $\boldsymbol{P}(\boldsymbol{X})$ |
| :--- | :--- |
| 0 | .064 |
| 1 | .288 |
| 2 | .432 |
| 3 | .216 |

b. $\quad \mu=1.8$
$\sigma^{2}=0.72$
$\sigma=\sqrt{0.72}=.8485$
13. a. .2668, found by $P(2)=\frac{9!}{(9-2)!2!}(.3)^{2}(.7)^{7}$
b. . 1715 , found by $P(4)=\frac{9!}{(9-4)!4!}(.3)^{4}(.7)^{5}$
c. . 0404 , found by $P(0)=\frac{9!}{(9-0)!0!}(.3)^{0}(.7)^{9}$
15. a. . 2824 , found by $P(0)=\frac{12!}{(12-0)!0!}(.10)^{0}(.9)^{12}$
b. . 3765 , found by $P(1)=\frac{12!}{(12-1)!1!}(.10)^{1}(.9)^{11}$
c. .2301, found by $P(2)=\frac{12!}{(12-2)!2!}(.10)^{2}(.9)^{10}$
d. $\mu=1.2$, found by $12(.10)$
$\sigma=1.0392$, found by $\sqrt{1.08}$
17. a. 0.1858 , found by $\frac{15!}{2!13!}(0.23)^{2}(0.77)^{13}$
b. 0.1416 , found by $\frac{15!}{5!10!}(0.23)^{5}(0.77)^{10}$
c. 3.45 , found by $(0.23)(15)$
19. a. 0.296 , found by using Appendix B. 9 with $n$ of $8, \pi$ of 0.30 , and $x$ of 2
b. $P(x \leq 2)=0.058+0.198+0.296=0.552$
c. 0.448 , found by $P(x \geq 3)=1-P(x \leq 2)=1-0.552$
21. a. 0.387 , found from Appendix $B .9$ with $n$ of $9, \pi$ of 0.90 , and $x$ of 9
b. $P(X<5)=0.001$
c. 0.992 , found by $1-0.008$
d. 0.947 , found by $1-0.053$
23. a. $\mu=10.5$, found by $15(0.7)$ and $\sigma=\sqrt{15(0.7)(0.3)}=$ 1.7748
b. 0.2061 , found by $\frac{15!}{10!5!}(0.7)^{10}(0.3)^{5}$
c. 0.4247 , found by $0.2061+0.2186$
d. 0.5154 , found by $0.2186+0.1700+0.0916+0.0305+0.0047$
25. a. . 6703
b. .3297
27. a. . 0613
b. .0803
29. $\mu=6$
$P(X \geq 5)=1-(.0025+.0149+.0446+.0892+.1339)$ $=.7149$
31. A random variable is a quantitative or qualitative outcome that results from a chance experiment. A probability distribution also includes the likelihood of each possible outcome.
33. $\mu=\$ 1,000(.25)+\$ 2,000(.60)+\$ 5,000(.15)=\$ 2,200$ $\sigma^{2}=(1,000-2,200)^{2} .25+(\$ 2,000-\$ 2,200)^{2} .60+$ $(5,000-2,200)^{2} .15$
$=1,560,000$
35. $\mu=12(.25)+\cdots+15(.1)=13.2$
$\sigma^{2}=(12-13.2)^{2} .25+\cdots+(15-13.2)^{2} .10=0.86$ $\sigma=\sqrt{0.86}=.927$
37. a. $\mu=10(.35)=3.5$
b. $P(X=4)={ }_{10} C_{4}(.35)^{4}(.65)^{6}=210(.0150)(.0754)=.2375$
c. $P(X \geq 4)={ }_{10} C_{x}(.35)^{X}(.65)^{10-X}$

$$
=.2375+.1536+\cdots+.0000=.4862
$$

39. a. 6 , found by $0.4 \times 15$
b. 0.0245 , found by $\frac{15!}{10!5!}(0.4)^{10}(0.6)^{5}$
c. 0.0338 , found by $0.0245+0.0074+0.0016+0.0003+0.0000$
d. 0.0093 , found by $0.0338-0.0245$
40. a. $\mu=20(0.075)=1.5$
$\sigma=\sqrt{20(0.075)(0.925)}=1.1779$
b. 0.2103 , found by $\frac{20!}{0!20!}(0.075)^{0}(0.925)^{20}$
c. 0.7897 , found by $1-0.2103$
41. a. 0.1311 , found by $\frac{16!}{4!12!}(0.15)^{4}(0.85)^{12}$
b. 2.4, found by (0.15)(16)
c. 0.2100 , found by

$$
1-0.0743-0.2097-0.2775-0.2285
$$

45. 0.279
46. $\mu=4.0$, from Appendix B. 5
a. . 0183
b. . 1954
c. . 6289
d. . 5665
47. a. 0.1733 , found by $\frac{(3.1)^{4} e^{-3.1}}{4!}$
b. 0.0450 , found by $\frac{(3.1)^{0} e^{-3.1}}{0!}$
c. 0.9550 , found by $1-0.0450$
48. $\mu=n \pi=23\left(\frac{2}{113}\right)=.407$
$P(2)=\frac{(.407)^{2} e^{-.407}}{2!}=0.0551$
$P(0)=\frac{(.407)^{0} e^{-.407}}{0!}=0.6656$
49. a. $\mu=n \pi=15(.67)=10.05$

$$
\sigma=\sqrt{n \pi(1-\pi)}=\sqrt{15(.67)(.33)}=1.8211
$$

b. $P(8)={ }_{15} C_{8}(.67)^{8}(.33)^{7}=6435(.0406)(.000426)=.1114$
c. $P(x \geq 8)=.1114+.1759+\cdots+.0025=.9163$
55. The mean number of home runs per game is 1.89835 , found by $4613 /(15 \times 162)$.
a. $P(0)=\frac{1.89835^{\circ} e^{-1.89835}}{0!}=0.14982$
b. $P(2)=\frac{1.89835^{2} e^{-1.89835}}{2!}=0.26995$
c. $P(X>=4)=0.1250=1-(0.1498+0.2844$

$$
+0.2700+0.1708)
$$

## CHAPTER 7

1. a. $b=10, a=6$
b. $\mu=\frac{6+10}{2}=8$
c. $\sigma=\sqrt{\frac{(10-6)^{2}}{12}}=1.1547$
d. Area $=\frac{1}{(10-6)} \cdot \frac{(10-6)}{1}=1$
e. $P(X>7)=\frac{1}{(10-6)} \cdot \frac{10-7}{1}=\frac{3}{4}=.75$
f. $P(7 \leq x \leq 9)=\frac{1}{(10-6)} \cdot \frac{(9-7)}{1}=\frac{2}{4}=.50$
2. a. 0.30 , found by $(30-27) /(30-20)$
b. 0.40 , found by $(24-20) /(30-20)$
3. a. $a=0.5, b=3.00$
b. $\mu=\frac{0.5+3.00}{2}=1.75$

$$
\sigma=\sqrt{\frac{(3.00-.50)^{2}}{12}}=.72
$$

c. $P(x<1)=\frac{1}{(3.0-0.5)} \cdot \frac{1-.5}{1}=\frac{.5}{2.5}=0.2$
d. 0 , found by $\frac{1}{(3.0-0.5)} \frac{(1.0-1.0)}{1}$
e. $P(x>1.5)=\frac{1}{(3.0-0.5)} \cdot \frac{3.0-1.5}{1}=\frac{1.5}{2.5}=0.6$
7. The actual shape of a normal distribution depends on its mean and standard deviation. Thus, there is a normal distribution, and an accompanying normal curve, for a mean of 7 and a standard deviation of 2 . There is another normal curve for a mean of $\$ 25,000$ and a standard deviation of $\$ 1,742$, and so on.
9. a. 490 and 510 , found by $500 \pm 1$ (10)
b. 480 and 520 , found by $500 \pm 2(10)$
c. 470 and 530 , found by $500 \pm 3(10)$
11. $Z_{\text {Rob }}=\frac{\$ 50,000-\$ 60,000}{\$ 5,000}=-2$

$$
Z_{\text {Rachel }}=\frac{\$ 50,000-\$ 35,000}{\$ 8,000}=1.875
$$

Adjusting for their industries, Rob is well below average and Rachel well above.
13. a. 1.25 , found by $z=\frac{25-20}{4.0}=1.25$
b. 0.3944 , found in Appendix B. 1
c. 0.3085 , found by $z=\frac{18-20}{2.5}=-0.5$

Find 0.1915 in Appendix B. 1 for $z=-0.5$, then $0.5000-0.1915=0.3085$
15. a. 0.3413 , found by $z=\frac{\$ 24-\$ 20.50}{\$ 3.50}=1.00$,
then find 0.3413 in Appendix B. 1 for $z=1$
b. 0.1587 , found by $0.5000-0.3413=0.1587$
c. 0.3336 , found by $z=\frac{\$ 19.00-\$ 20.50}{\$ 3.50}=-0.43$

Find 0.1664 in Appendix B.1, for $z=-0.43$, then $0.5000-0.1664=0.3336$
17. a. 0.8276 : First find $z=-1.5$, found by $(44-50) / 4$ and $z=1.25=(55-50) / 4$. The area between -1.5 and 0 is 0.4332 and the area between 0 and 1.25 is 0.3944 , both from Appendix B.1. Then adding the two areas we find that $0.4332+0.3944=0.8276$.
b. 0.1056 , found by $0.5000-.3944$, where $z=1.25$
c. 0.2029 : Recall that the area for $z=1.25$ is 0.3944 , and the area for $z=0.5$, found by $(52-50) / 4$, is 0.1915 . Then subtract $0.3944-0.1915$ and find 0.2029 .
19. a. 0.4052 , where $z=[(3100-3000) / 410]=0.24$; leads to $0.5-0.0948=0.4052$.
b. 0.2940 ; the $z$ value for $\$ 3,500$ is 1.22 , found by [(3500-3000)/410], and the corresponding area is 0.3888. Leads to $0.3888-0.0948=0.2940$
c. 0.8552 ; the $z$ value for $\$ 2,250$ is -1.83 , found by [(2250-3000)/410], and the corresponding area is 0.4664 . Then, $0.4664+0.3888=0.8552$
21. a. 0.0764 , found by $z=(20-15) / 3.5=1.43$, then $0.5000-0.4236=0.0764$
b. 0.9236 , found by $0.5000+0.4236$, where $z=1.43$
c. 0.1185 , found by $z=(12-15) / 3.5=-0.86$. The area under the curve is 0.3051 , then $z=(10-15) / 3.5=-1.43$. The area is 0.4236 . Finally, $0.4236-0.3051=0.1185$.
23. $X=56.60$, found by adding 0.5000 (the area left of the mean) and then finding a $z$ value that forces $45 \%$ of the data to fall inside the curve. Solving for $X: 1.65=(X-50) / 4=56.60$.
25. $\$ 1,630$, found by $\$ 2,100-1.88(\$ 250)$
27. a. 214.8 hours: Find $a z$ value where 0.4900 of area is between 0 and $z$. That value is $z=2.33$. Then solve for $X: 2.33=(X-195) / 8.5$, so $X=214.8$ hours.
b. 270.2 hours: Find a $z$ value where 0.4900 of area is between 0 and $(-z)$. That value is $z=-2.33$. Then solve for $X$ : $-2.33=(X-290) / 8.5$, so $X=270.2$ hours.
29. $41.7 \%$, found by $12+1.65(18)$
31. a. $\mu=\frac{11.96+12.05}{2}=12.005$
b. $\sigma=\sqrt{\frac{(12.05-11.96)^{2}}{12}}=.0260$
c. $P(X<12)=\frac{1}{(12.05-11.96)} \frac{12.00-11.96}{1}=\frac{.04}{.09}=.44$
d. $P(X>11.98)=\frac{1}{(12.05-11.96)}\left(\frac{12.05-11.98}{1}\right)$

$$
=\frac{.07}{.09}=.78
$$

e. All cans have more than 11.00 ounces, so the probability is $100 \%$.
33. a. $\mu=\frac{4+10}{2}=7$
b. $\sigma=\sqrt{\frac{(10-4)^{2}}{12}}=1.732$
c. $P(X<6)=\frac{1}{(10-4)} \cdot\left(\frac{6-4}{1}\right)=\frac{2}{6}=.33$
d. $P(X>5)=\frac{1}{(10-4)} \cdot\left(\frac{10-5}{1}\right)=\frac{5}{6}=.83$
35. a. -0.4 for net sales, found by $(170-180) / 25$. 2.92 for employees, found by $(1,850-1,500) / 120$.
b. Net sales are 0.4 standard deviations below the mean. Employees is 2.92 standard deviations above the mean.
c. 65.54 percent of the aluminum fabricators have greater net sales compared with Clarion, found by $0.1554+$ 0.5000 . Only $0.18 \%$ have more employees than Clarion, found by $0.5000-0.4982$.
37. a. 0.5000 , because $z=\frac{30-490}{90}=-5.11$
b. 0.2514 , found by $0.5000-0.2486$
c. 0.6374 , found by $0.2486+0.3888$
d. 0.3450 , found by $0.3888-0.0438$
39. a. 0.3015 , found by $0.5000-0.1985$
b. 0.2579 , found by $0.4564-0.1985$
c. 0.0011 , found by $0.5000-0.4989$
d. 1,818 , found by $1,280+1.28(420)$
41. a. $90.82 \%$ : First find $z=1.33$, found by $(40-34) / 4.5$. The area between 0 and 1.33 is 0.4082 . Then add 0.5000 and 0.4082 and find 0.9082 or $90.82 \%$.
b. $78.23 \%$ : First find $z=-0.78$ found by $(25-29) / 5.1$. The area between 0 and $(-0.78)$ is 0.2823 . Then add 0.5000 and 0.2823 and find 0.7823 or $78.23 \%$.
c. 44.5 hours/week for women: Find a $z$ value where 0.4900 of the area is between 0 and $z$. That value is 2.33. Then solve for $X: 2.33=(X-34) / 4.5$, so $X=44.5$ hours/week. 40.9 hours/week for men: $2.33=(X-29) / 5.1$, so $X=40.9$ hours/week.
43. About 4,099 units, found by solving for $X$.
$1.65=(X-4,000) / 60$
45. a. $15.39 \%$, found by $(8-10.3) / 2.25=-1.02$, then $0.5000-0.3461=0.1539$.
b. $17.31 \%$, found by: $z=(12-10.3) / 2.25=0.76$. Area is 0.2764 . $z=(14-10.3) / 2.25=1.64$. Area is 0.4495 . The area between 12 and 14 is 0.1731 , found by $0.4495-0.2764$.
c. Yes, but it is rather remote. Reasoning: On 99.73\% of the days, returns are between 3.55 and 17.05 , found by $10.3 \pm 3(2.25)$. Thus, the chance of less than 3.55 returns is rather remote.
47. a. $21.19 \%$ found by $z=(9.00-9.20) / 0.25=-0.80$, so $0.5000-0.2881=0.2119$
b. Increase the mean. $z=(9.00-9.25) / 0.25=-1.00$, $P=0.5000-0.3413=0.1587$.
Reduce the standard deviation. $z=(9.00-9.20) /$ $0.15=-1.33 ; P=0.5000-0.4082=0.0918$.
Reducing the standard deviation is better because a smaller percent of the hams will be below the limit.
49. a. $z=(60-52) / 5=1.60$, so $0.5000-0.4452=0.0548$
b. Let $z=0.67$, so $0.67=(X-52) / 5$ and $X=55.35$, set mileage at 55,350
c. $z=(45-52) / 5=-1.40$, so $0.5000-0.4192=0.0808$
51. $\frac{470-\mu}{\sigma}=0.25 \quad \frac{500-\mu}{\sigma}=1.28 \quad \sigma=29,126$ and $\mu=462,718$
53. a. $1.65=(45-\mu) / 5 \quad \mu=36.75$
b. $1.65=(45-\mu) / 10 \quad \mu=28.5$
c. $z=(30-28.5) / 10=0.15$,
then $0.5000+0.0596=0.5596$
55. a. Estimate is 2.043, rounding up to $3 ; z=(3.5-2.436)$ / $0.713=1.49$; leads to $0.5000-0.4319=0.0681$. 2.043 teams is $(30)(0.0681)$, rounding up to 3 . There were actually 3 teams that exceeded 3.5 million. Estimate is fairly accurate.
b. Estimate is 25.7, or 26 teams. $z=(50-91.020) /$ $38.258=-1.07$; leads to $0.3577+0.5000=0.8577$. 25.7 teams is 0.8577 (30). There were actually 28 teams that exceeded $\$ 50$ million in payroll. Estimate is fairly accurate.

## CHAPTER 8

1. a. 303 Louisiana, 5155 S. Main, 3501 Monroe, 2652 W. Central
b. Answers will vary.
c. 630 Dixie Hwy, 835 S. McCord Rd, 4624 Woodville Rd
d. Answers will vary.
2. a. Bob Schmidt Chevrolet Great Lakes Ford Nissan Grogan Towne Chrysler Southside Lincoln Mercury Rouen Chrysler Jeep Eagle
b. Answers will vary.
c. Yark Automotive

Thayer Chevrolet Toyota
Franklin Park Lincoln Mercury
Mathews Ford Oregon Inc.
Valiton Chrysler
5. a.

| Sample | Values | Sum | Mean |
| :---: | :---: | :---: | :---: |
| 1 | 12,12 | 24 | 12 |
| 2 | 12,14 | 26 | 13 |
| 3 | 12,16 | 28 | 14 |
| 4 | 12,14 | 26 | 13 |
| 5 | 12,16 | 28 | 14 |
| 6 | 14,16 | 30 | 15 |

b. $\mu_{\bar{x}}=(12+13+14+13+14+15) / 6=13.5$ $\mu=(12+12+14+16) / 4=13.5$
c. More dispersion with population data compared to the sample means. The sample means vary from 12 to 15, whereas the population varies from 12 to 16.
7. a.

| Sample | Values | Sum | Mean |
| :---: | :---: | :---: | :---: |
| 1 | $12,12,14$ | 38 | 12.66 |
| 2 | $12,12,15$ | 39 | 13.00 |
| 3 | $12,12,20$ | 44 | 14.66 |
| 4 | $14,15,20$ | 49 | 16.33 |
| 5 | $12,14,15$ | 41 | 13.66 |
| 6 | $12,14,15$ | 41 | 13.66 |
| 7 | $12,15,20$ | 47 | 15.66 |
| 8 | $12,15,20$ | 47 | 15.66 |
| 9 | $12,14,20$ | 46 | 15.33 |
| 10 | $12,14,20$ | 46 | 15.33 |

b. $\mu_{\bar{x}}=\frac{(12.66+\cdots+15.33+15.33)}{10}=14.6$ $\mu=(12+12+14+15+20) / 5=14.6$
c. The dispersion of the population is greater than that of the sample means. The sample means vary from 12.66 to 16.33, whereas the population varies from 12 to 20.
9. a. 20 , found by ${ }_{6} C_{3}$
b.

| Sample | Cases | Sum | Mean |
| :--- | :---: | :---: | :---: |
| Ruud, Wu, Sass | $3,6,3$ | 12 | 4.00 |
| Ruud, Sass, Flores | $3,3,3$ | 9 | 3.00 |
| $\vdots$ | $\vdots$ | $\vdots$ | $\vdots$ |
| Sass, Flores, Schueller | $3,3,1$ | 7 | 2.33 |

c. $\mu_{\bar{x}}=2.67$, found by $\frac{53.33}{20}$.
$\mu=2.67$, found by $(3+6+3+3+0+1) / 6$.
They are equal.
d.


Distribution of Sample Means


| Sample Mean | Number of Means | Probability |
| :---: | :---: | :---: |
| 1.33 | 3 | .1500 |
| 2.00 | 3 | .1500 |
| 2.33 | 4 | .2000 |
| 3.00 | 4 | .2000 |
| 3.33 | 3 | .1500 |
| 4.00 | $\underline{3}$ | $\underline{.1500}$ |
|  | 20 | 1.0000 |

The population has more dispersion than the sample means. The sample means vary from 1.33 to 4.0. The population varies from 0 to 6 .
11. a.

b.

| Sample | Sum | $\overline{\boldsymbol{X}}$ |  | Sample | Sum | $\overline{\boldsymbol{X}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 11 | 2.2 |  | 6 | 20 | 4.0 |
| 2 | 31 | 6.2 |  | 7 | 23 | 4.6 |
| 3 | 21 | 4.2 |  | 8 | 29 | 5.8 |
| 4 | 24 | 4.8 |  | 9 | 35 | 7.0 |
| 5 | 21 | 4.2 |  | 10 | 27 | 5.4 |



The mean of the 10 sample means is 4.84 , which is close to the population mean of 4.5 . The sample means range from 2.2 to 7.0 , whereas the population values range from 0 to 9 . From the above graph, the sample means tend to cluster between 4 and 5 .
13. a.-c. Answers will vary depending on the coins in your possession.
15. a. $z=\frac{63-60}{12 / \sqrt{9}}=0.75$
$P=.2266$, found by $.5000-.2734$
b. $z=\frac{56-60}{12 / \sqrt{9}}=-1.00$
$P=.1587$, found by $.5000-.3413$
c. $P=.6147$, found by $0.3413+0.2734$
17. $z=\frac{1,950-2,200}{250 / \sqrt{50}}=-7.07 \quad P=1$, or virtually certain
19. a. Formal Man, Summit Stationers, Bootleggers, Leather Ltd, Petries
b. Answers may vary.
c. Elder-Beerman, Frederick's of Hollywood, Summit Stationers, Lion Store, Leather Ltd., Things Remembered, County Seat, Coach House Gifts, Regis Hairstylists
21. a.

| Samples | Mean | Deviation from <br> Mean | Square of <br> Deviation |
| :---: | :---: | :---: | :---: |
| 1,1 | 1.0 | -1.0 | 1.0 |
| 1,2 | 1.5 | -0.5 | 0.25 |
| 1,3 | 2.0 | 0.0 | 0.0 |
| 2,1 | 1.5 | -0.5 | 0.25 |
| 2,2 | 2.0 | 0.0 | 0.0 |
| 2,3 | 2.5 | 0.5 | 0.25 |
| 3,1 | 2.0 | 0.0 | 0.0 |
| 3,2 | 2.5 | 0.5 | 0.25 |
| 3,3 | 3.0 | 1.0 | 1.0 |

b. Mean of sample means is $(1.0+1.5+2.0+\cdots+$ $3.0) / 9=18 / 9=2.0$. The population mean is $(1+2+$ $3) / 3=6 / 3=2$. They are the same value.
c. Variance of sample means is $(1.0+0.25+0.0+\cdots+$ $1.0) / 9=3 / 9=1 / 3$. Variance of the population values is $(1+0+1) / 3=2 / 3$. The variance of the population is twice as large as that of the sample means.
d. Sample means follow a triangular shape peaking at 2 . The population is uniform between 1 and 3 .
23. Larger samples provide narrower estimates of a population mean. So the company with 200 sampled customers can provide more precise estimates. In addition, they are selected consumers who are familiar with laptop computers and may be better able to evaluate the new computer.
25. a. We selected 60, 104, 75, 72, and 48. Answers will vary.
b. We selected the third observation. So the sample consists of 75, 72, 68, 82, 48. Answers will vary.
c. Number the first 20 motels from 00 to 19. Randomly select three numbers. Then number the last five numbers 20 to 24 . Randomly select two numbers from that group.
27. a. 15 , found by ${ }_{6} C_{2}$
b.

| Sample | Value | Sum | Mean |
| :---: | :---: | :---: | :---: |
| 1 | 79,64 | 143 | 71.5 |
| 2 | 79,84 | 163 | 81.5 |
| $\vdots$ | $\vdots$ | $\vdots$ | $\vdots$ |
| 15 | 92,77 | 169 | $\frac{84.5}{1,195.0}$ |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

c. $\mu_{\bar{x}}=79.67$, found by $1,195 / 15$.
$\mu=79.67$, found by $478 / 6$.
They are equal.
d. No. The student is not graded on all available information. He/she is as likely to get a lower grade based on the sample as a higher grade.
29. a. 10, found by ${ }_{5} \mathrm{C}_{2}$
b.

| Number of <br> Shutdowns | Mean | Number of <br> Shutdowns | Mean |
| :---: | :---: | :---: | :---: |
| 4,3 | 3.5 | 3,3 | 3.0 |
| 4,5 | 4.5 | 3,2 | 2.5 |
| 4,3 | 3.5 | 5,3 | 4.0 |
| 4,2 | 3.0 | 5,2 | 3.5 |
| 3,5 | 4.0 | 3,2 | 2.5 |


| Sample <br> Mean | Frequency | Probability |
| :---: | :---: | :---: |
| 2.5 | 2 | .20 |
| 3.0 | 2 | .20 |
| 3.5 | 3 | .30 |
| 4.0 | 2 | .20 |
| 4.5 | $\frac{1}{10}$ | $\overline{.10}$ |
|  |  | 1.00 |

c. $\mu_{\bar{x}}=(3.5+4.5+\cdots+2.5) / 10=3.4$
$\mu=(4+3+5+3+2) / 5=3.4$
The two means are equal.
d. The population values are relatively uniform in shape. The distribution of sample means tends toward normality.
31. a. The distribution will be normal.
b. $\sigma_{\bar{X}}=\frac{5.5}{\sqrt{25}}=1.1$
c. $z=\frac{36-35}{5.5 / \sqrt{25}}=0.91$
$P=0.1814$, found by $0.5000-0.3186$
d. $z=\frac{34.5-35}{5.5 / \sqrt{25}}=-0.45$
$P=0.6736$, found by $0.5000+0.1736$
e. 0.4922 , found by $0.3186+0.1736$
33. $z=\frac{\$ 335-\$ 350}{\$ 45 / \sqrt{40}}=-2.11$
$P=0.9826$, found by $0.5000+0.4826$
35. $z=\frac{25.1-24.8}{2.5 / \sqrt{60}}=0.93$
$P=0.8238$, found by $0.5000+0.3238$
37. Between 5,954 and 6,046 , found by $6,000 \pm 1.96(150 / \sqrt{40})$
39. $z=\frac{900-947}{205 / \sqrt{60}}=-1.78$
$P=0.0375$, found by $0.5000-0.4625$
41. a. Alaska, Connecticut, Georgia, Kansas, Nebraska, South Carolina, Virginia, Utah
b. Arizona, Florida, Iowa, Massachusetts, Nebraska, North Carolina, Rhode Island, Vermont
43. a. $z=\frac{600-510}{14.28 / \sqrt{10}}=19.9, P=0.00$, or virtually never
b. $z=\frac{500-510}{14.28 / \sqrt{10}}=-2.21$,

$$
P=0.4864+0.5000=0.9864
$$

c. $z=\frac{500-510}{14.28 / \sqrt{10}}=-2.21$,

$$
P=0.5000-0.4864=0.0136
$$

45. a. $\sigma_{\bar{X}}=\frac{2.1}{\sqrt{81}}=0.23$
b. $z=\frac{7.0-6.5}{2.1 / \sqrt{81}}=2.14, z=\frac{6.0-6.5}{2.1 / \sqrt{81}}=-2.14$, $P=.4838+.4838=.9676$
c. $z=\frac{6.75-6.5}{2.1 / \sqrt{81}}=1.07, z=\frac{6.25-6.5}{2.1 / \sqrt{81}}=-1.07$, $P=.3577+.3577=.7154$
d. .0162 found by $.5000-.4838$
46. Mean 2010 attendance is 2.436 million. Likelihood of a sample mean this large or larger is 0.0721 , found by 0.5000 0.4279 . The $z$ value is 1.46 .

## CHAPTER 9

1. 51.32 and 58.68 , found by $55 \pm 2.576(10 / \sqrt{49})$
2. a. 1.581 , found by $\sigma_{\bar{x}}=25 / \sqrt{250}$
b. The population is normally distributed and the population variance is known.
c. 16.901 and 23.099 , found by $20 \pm 3.099$
3. a. $\$ 20$. It is our best estimate of the population mean.
b. $\$ 18.60$ and $\$ 21.40$, found by $\$ 20 \pm 1.96(\$ 5 / \sqrt{49})$. About 95\% of the intervals similarly constructed will include the population mean.
4. a. 8.60 gallons.
b. 7.84 and 9.36 , found by $8.60 \pm 2.576(2.30 / \sqrt{60})$
c. If 100 such intervals were determined, the population mean would be included in about 99 intervals.
5. a. 2.201
b. 1.729
c. 3.499
6. a. The population mean is unknown, but the best estimate is 20 , the sample mean.
b. Use the $t$ distribution since the standard deviation is unknown. However, assume the population is normally distributed.
c. 2.093
d. Between 19.06 and 20.94 , found by $20 \pm 2.093(2 / \sqrt{20})$
e. Neither value is reasonable, because they are not inside the interval.
7. Between 95.39 and 101.81 , found by $98.6 \pm 1.833(5.54 / \sqrt{10})$
8. a. 0.8 , found by $80 / 100$
b. Between 0.72 and 0.88 , found by $0.8 \pm 1.96\left(\sqrt{\frac{0.8(1-0.8)}{100}}\right)$
c. We are reasonably sure the population proportion is between $72 \%$ and $88 \%$.
9. a. 0.625 , found by $250 / 400$
b. Between 0.563 and 0.687 , found by
$0.625 \pm 2.576\left(\sqrt{\frac{0.625(1-0.625)}{400}}\right)$
c. We are reasonably sure the population proportion is between $56 \%$ and $69 \%$.
10. 97 , found by $n=\left(\frac{1.96 \times 10}{2}\right)^{2}=96.04$
11. 196, found by $n=0.15(0.85)\left(\frac{1.96}{0.05}\right)^{2}=195.9216$
12. 554 , found by $n=\left(\frac{1.96 \times 3}{0.25}\right)^{2}=553.19$
13. a. 577 , found by $n=0.60(0.40)\left(\frac{1.96}{0.04}\right)^{2}=576.24$
b. 601, found by $n=0.50(0.50)\left(\frac{1.96}{0.04}\right)^{2}=600.25$
14. 6.13 years to 6.87 years, found by $6.5 \pm 1.989(1.7 / \sqrt{85})$
15. a. Between $\$ 313.41$ and 332.59 , found by
$323 \pm 2.426\left(\frac{25}{\sqrt{40}}\right)$.
b. $\$ 350$ is not reasonable, because it is outside of the confidence interval.
16. a. The population mean is unknown.
b. Between 7.50 and 9.14 , found by $8.32 \pm 1.685(3.07 / \sqrt{40})$
c. 10 is not reasonable because it is outside the confidence interval.
17. a. 65.49 up to 71.71 hours, found by $68.6 \pm 2.680(8.2 / \sqrt{50})$
b. The value suggested by the NCAA is included in the confidence interval. Therefore, it is reasonable.
c. Changing the confidence interval to 95 would reduce the width of the interval. The value of 2.680 would change to 2.010 .
18. 61, found by $1.96(16 / \sqrt{n})=4$
19. Between $\$ 13,734$ up to $\$ 15,028$, found by $14,381 \pm 1.711(1,892 / \sqrt{25}) \cdot 15,000$ is reasonable because it is inside the confidence interval.
20. a. $\$ 62.583$, found by $\$ 751 / 12$
b. Between $\$ 60.54$ and $\$ 64.63$, found by $62.583 \pm 1.796(3.94 / \sqrt{12})$
c. $\$ 60$ is not reasonable, because it is outside the confidence interval.
21. a. 89.4667 , found by $1,342 / 15$
b. Between 84.99 and 93.94 , found by $89.4667 \pm 2.145(8.08 / \sqrt{15})$
c. Yes, because even the lower limit of the confidence interval is above 80 .
22. The confidence interval is between 0.011 and 0.059 , found by $0.035 \pm 2.576\left(\sqrt{\frac{0.035(1-0.035)}{400}}\right)$. It would not be reasonable to conclude that fewer than $5 \%$ of the employees are now failing the test, because 0.05 is inside the confidence interval.
23. Between .65 and .75 , found by $.7 \pm 2.576 \sqrt{(.7)(.3) / 500}$. Yes, she will be reelected. She will receive more than $50 \%$ of the vote.
24. 369, found by $n=0.60(1-0.60)(1.96 / 0.05)^{2}$
25. 97 , found by $[(1.96 \times 500) / 100]^{2}$
26. a. Between 7,849 and 8,151 , found by
$8,000 \pm 2.756(300 / \sqrt{30})$
b. 554 , found by $n=\left(\frac{(1.96)(300)}{25}\right)^{2}$
27. a. Between 75.44 and 80.56 , found by $78 \pm 2.010(9 / \sqrt{50})$
b. 220 , found by $n=\left(\frac{(1.645)(9)}{1.0}\right)^{2}$
28. a. 30 , found by $180 / \sqrt{36}$
b. $\$ 355.10$ and $\$ 476.90$, found by $\$ 416 \pm 2.030\left(\frac{\$ 180}{\sqrt{36}}\right)$
c. About 1,245 , found by $\left(\frac{1.96(180)}{10}\right)^{2}$
29. a. 708.13 , rounded up to 709 , found by $0.21(1-0.21)(1.96 / 0.03)^{2}$
b. 1,068 , found by $0.50(0.50)(1.96 / 0.03)^{2}$
30. a. Between 0.156 and 0.184 , found by

$$
0.17 \pm 1.96 \sqrt{\frac{(0.17)(1-0.17)}{2700}}
$$

b. Yes, because $18 \%$ is inside the confidence interval.
c. 21,682 ; found by $0.17(1-0.17)[1.96 / 0.005]^{2}$
61. Between 12.69 and 14.11 , found by $13.4 \pm 1.96(6.8 / \sqrt{352})$
63. a. For selling price: 211.99 up to 230.22 , found by $221.1 \pm(1.983)(47.11 / \sqrt{105})=221.1 \pm 9.12$
b. For distance: 13.685 up to 15.572 , found by $14.629 \pm(1.983)(4.874 / \sqrt{105})=14.629 \pm 0.943$
c. For garage: 0.5867 up to 0.7657 , found by $0.6762 \pm$ $(1.96) \sqrt{\frac{0.6762(1-0.6762)}{105}}=0.6762 \pm 0.0895$
d. Answers may vary.
65. a. Between $\$ 438.34$ and 462.24 , found by $450.29 \pm 1.99\left(\frac{53.69}{\sqrt{80}}\right)$
b. Between 820.72 and 839.50 , found by $830.11 \pm 1.99\left(\frac{42.19}{\sqrt{80}}\right)$
c. Answers will vary.

## CHAPTER 10

1. a. Two-tailed
b. Reject $H_{0}$ when $z$ does not fall in the region between -1.96 and 1.96 .
c. -1.2 , found by $z=(49-50) /(5 / \sqrt{36})=-1.2$
d. Fail to reject $H_{0}$.
e. $p=.2302$, found by $2(.5000-.3849)$. A $23.02 \%$ chance of finding a $z$ value this large when $H_{0}$ is true.
2. a. One-tailed
b. Reject $H_{0}$ when $z>1.645$.
c. 1.2 , found by $z=(21-20) /(5 / \sqrt{36})=1.2$
d. Fail to reject $H_{0}$ at the .05 significance level
e. $p=.1151$, found by $.5000-.3849$. An $11.51 \%$ chance of finding a $z$ value this large or larger when the null hypothesis is true.
3. a. $H_{0}: \mu=60,000 \quad H_{1}: \mu \neq 60,000$
b. Reject $H_{0}$ if $z<-1.96$ or $z>1.96$.
c. -0.69 , found by:

$$
z=\frac{59,500-60,000}{(5,000 / \sqrt{48})}=-0.69
$$

d. Do not reject $H_{0}$.
e. $p=.4902$, found by $2(.5000-.2549$ ). Crosset's experience is not different from that claimed by the manufacturer. If $H_{0}$ is true, the probability of finding a value more extreme than this is .4902 .
7. a. $H_{0}: \mu \geq 6.8 \quad H_{1}: \mu<6.8$
b. Reject $H_{0}$ if $z<-1.645$
c. $z=\frac{6.2-6.8}{0.5 / \sqrt{36}}=-7.2$
d. $H_{0}$ is rejected.
e. $p=0$. The mean number of DVDs watched is less than 6.8 per month. If $H_{0}$ is true, there is virtually no chance of getting a statistic this small.
9. a. Reject $H_{0}$ when $t>1.833$.
b. $t=\frac{12-10}{(3 / \sqrt{10})}=2.108$
c. Reject $H_{0}$. The mean is greater than 10 .
11. $H_{0}: \mu \leq 40 \quad H_{1}: \mu>40$

Reject $H_{0}$ if $t>1.703$.

$$
t=\frac{42-40}{(2.1 / \sqrt{28})}=5.040
$$

Reject $H_{0}$ and conclude that the mean number of calls is greater than 40 per week.
13. $H_{0}: \mu \leq 40,000 \quad H_{1}: \mu>40,000$

Reject $H_{0}$ if $t>1.833$.

$$
t=\frac{50,000-40,000}{10,000 / \sqrt{10}}=3.16
$$

Reject $H_{0}$ and conclude that the mean income in Wilmington is greater than $\$ 40,000$.
15. a. Reject $H_{0}$ if $t<-3.747$.
b. $\bar{X}=17$ and $s=\sqrt{\frac{50}{5-1}}=3.536$

$$
t=\frac{17-20}{(3.536 / \sqrt{5})}=-1.90
$$

c. Do not reject $H_{0}$. We cannot conclude the population mean is less than 20.
d. Between .05 and .10 , about .065
17. $H_{0}: \mu \leq 1.4 \quad H_{1}: \mu>1.4$

Reject $H_{0}$ if $t>2.821$.

$$
t=\frac{1.6-1.4}{0.216 / \sqrt{10}}=2.93
$$

Reject $H_{0}$ and conclude that the drug has increased the amount of water consumption. The $p$-value is between 0.01 and 0.005 .
There is a slight probability (between one chance in 100 and one chance in 200) this rise could have arisen by chance.
19. $H_{0}: \mu \leq 50 \quad H_{1}: \mu>50$

Reject $H_{0}$ if $t>1.796$.

$$
t=\frac{82.5-50}{59.5 / \sqrt{12}}=1.89
$$

Reject $H_{0}$ and conclude that the mean number of text messages is greater than 50 . The $p$-value is less than 0.05 . There is a slight probability (less than one chance in 20) this could happen by chance.
21. a. $H_{0}$ is rejected if $z>1.645$.
b. 1.09 , found by $z=(0.75-0.70) / \sqrt{(0.70 \times 0.30) / 100}$
c. $H_{0}$ is not rejected.
23. a. $H_{0}: \pi \leq 0.52 \quad H_{1}: \pi>0.52$
b. $H_{0}$ is rejected if $z>2.326$.
c. 1.62 , found by $z=(.5667-.52) / \sqrt{(0.52 \times 0.48) / 300}$
d. $H_{0}$ is not rejected. We cannot conclude that the proportion of men driving on the Ohio Turnpike is larger than 0.52 .
25. a. $H_{0}: \pi \geq 0.90 \quad H_{1}: \pi<0.90$
b. $H_{0}$ is rejected if $z<-1.282$.
c. -2.67 , found by $z=(0.82-0.90) / \sqrt{(0.90 \times 0.10) / 100}$
d. $H_{0}$ is rejected. Fewer than $90 \%$ of the customers receive their orders in less than 10 minutes.
27. $H_{0}: \mu=\$ 45,000 \quad H_{1}: \mu \neq \$ 45,000$

Reject $H_{0}$ if $z<-1.645$ or $z>1.645$.

$$
z=\frac{45,500-45,000}{\$ 3,000 / \sqrt{120}}=1.83
$$

Reject $H_{0}$. We can conclude that the mean salary is not $\$ 45,000$. $p$-value 0.0672 , found by $2(0.5000-0.4664$ ).
29. $H_{0}: \mu \geq 10 \quad H_{1}: \mu<10$

Reject $H_{0}$ if $z<-1.645$.

$$
z=\frac{9.0-10.0}{2.8 / \sqrt{50}}=-2.53
$$

Reject $H_{0}$. The mean weight loss is less than 10 pounds. $p$-value $=0.5000-0.4943=0.0057$
31. $H_{0}: \mu \geq 7.0 \quad H_{1}: \mu<7.0$

Assuming a $5 \%$ significance level, reject $H_{0}$ if $t<-1.677$.

$$
t=\frac{6.8-7.0}{0.9 / \sqrt{50}}=-1.57
$$

Do not reject $H_{0}$. West Virginia students are not sleeping less than 6 hours. $p$-value is between .05 and .10 .
33. $H_{0}: \mu \geq 3.13 \quad H_{1}: \mu<3.13$

Reject $H_{0}$ if $t<-1.711$

$$
t=\frac{2.86-3.13}{1.20 / \sqrt{25}}=-1.13
$$

We fail to reject $H_{0}$ and conclude that the mean number of residents is not necessarily less than 3.13.
35. $H_{0}: \mu \leq 14 \quad H_{1}: \mu>14$

Reject $H_{0}$ if $t>2.821$.
$\bar{X}=15.66 \quad s=1.544$

$$
t=\frac{15.66-14.00}{1.544 / \sqrt{10}}=3.400
$$

Reject $H_{0}$. The average rate is greater than $14 \%$.
37. $H_{0}: \mu=3.1 \quad H_{1}: \mu \neq 3.1$ Assume a normal population. Reject $H_{0}$ if $t<-2.201$ or $t>2.201$.

$$
\begin{aligned}
\bar{X} & =\frac{41.1}{12}=3.425 \\
s & =\sqrt{\frac{4.0625}{12-1}}=.6077 \\
t & =\frac{3.425-3.1}{.6077 / \sqrt{12}}=1.853
\end{aligned}
$$

Do not reject $H_{0}$. Cannot show a difference between senior citizens and the national average. $p$-value is about 0.09 .
39. $H_{0}: \mu \geq 6.5 \quad H_{1}: \mu<6.5$ Assume a normal population. Reject $H_{0}$ if $t<-2.718$.
$\bar{X}=5.1667 \quad s=3.1575$

$$
t=\frac{5.1667-6.5}{3.1575 / \sqrt{12}}=-1.463
$$

Do not reject $H_{0}$. The $p$-value is greater than 0.05 .
41. $H_{0}: \mu=0 \quad H_{1}: \mu \neq 0$

Reject $H_{0}$ if $t<-2.110$ or $t>2.110$.

$$
\begin{array}{ll}
\bar{X}=-0.2322 & s=0.3120 \\
t & =\frac{-0.2322-0}{0.3120 / \sqrt{18}}=-3.158
\end{array}
$$

Reject $H_{0}$. The mean gain or loss does not equal 0 .
The $p$-value is less than 0.01 , but greater than 0.001 .
43. $H_{0}: \mu \leq 100 \quad H_{1}: \mu>100$ Assume a normal population. Reject $H_{0}$ if $t>1.761$.

$$
\begin{aligned}
\bar{X} & =\frac{1,641}{15}=109.4 \\
s & =\sqrt{\frac{1,389.6}{15-1}}=9.9628 \\
t & =\frac{109.4-100}{9.9628 / \sqrt{15}}=3.654
\end{aligned}
$$

Reject $H_{0}$. The mean number with the scanner is greater than 100. $p$-value is 0.001 .
45. $H_{0}: \mu=1.5 \quad H_{1}: \mu \neq 1.5$

Reject $H_{0}$ if $t>3.250$ or $t<-3.250$.

$$
t=\frac{1.3-1.5}{0.9 / \sqrt{10}}=-0.703
$$

Do not reject $H_{0}$.
47. a. This is a binomial situation with both the mean number of successes and failures equal to 22.5 , found by $0.5 \times 45$.
b. $H_{0}: \pi=0.50 \quad H_{1}: \pi \neq 0.50$
c.

Distribution Plot
Normal, Mean $=0$, StDev $=1$


Reject $H_{0}$ if $z$ is not between -2.576 and 2.576.
d. $z=\frac{\left(\frac{31}{45}\right)-0.50}{\sqrt{0.50(1-0.50) / 45}}=2.534$ We do not reject the null hypothesis. These data do not prove the coin flip is biased.
e. The $p$-value is 0.0114 , found by $2 \times(0.5000-0.4943)$. A value this extreme will happen about once out of fifty times with a fair coin.
49. $H_{0}: \pi \leq 0.60 \quad H_{1}: \pi>0.60$
$H_{0}$ is rejected if $z>2.326$.

$$
z=\frac{.70-.60}{\sqrt{\frac{.60(.40)}{200}}}=2.89
$$

$H_{0}$ is rejected. Ms. Dennis is correct. More than 60\% of the accounts are more than three months old.
51. $H_{0}: \pi \leq 0.44 \quad H_{1}: \pi>0.44$
$H_{0}$ is rejected if $z>1.645$.

$$
z=\frac{0.480-0.44}{\sqrt{(0.44 \times 0.56) / 1,000}}=2.55
$$

$H_{0}$ is rejected. We conclude that there has been an increase in the proportion of people wanting to go to Europe.
53. $H_{0}: \pi \leq 0.20 \quad H_{1}: \pi>0.20$
$H_{0}$ is rejected if $z>2.326$

$$
z=\frac{(56 / 200)-0.20}{\sqrt{(0.20 \times 0.80) / 200}}=2.83
$$

$H_{0}$ is rejected. More than $20 \%$ of the owners move during a particular year. $p$-value $=0.5000-0.4977=0.0023$.
55. $H_{0}: \pi \leq 0.40 \quad H_{1}: \pi>0.40$

Reject $H_{0}$ if $z$ is greater than 2.326.

$$
z=\frac{(16 / 30)-0.40}{\sqrt{[0.40(1-0.40) / 30]}}=1.49
$$

Do not reject the null hypothesis. These data do not show that college students are more likely to skip breakfast.
57. $H_{0}: \pi \geq 0.0008 \quad H_{1}: \pi<0.0008$
$H_{0}$ is rejected if $z<-1.645$.
$z=\frac{0.0006-0.0008}{\sqrt{\frac{0.0008(0.9992)}{10,000}}}=-0.707 H_{0}$ is not rejected.
These data do not prove there is a reduced fatality rate.
59. $H_{0}: \mu \geq 8 \quad H_{1}: \mu<8$

Reject $H_{0}$ if $t<-1.714$.

$$
t=\frac{7.5-8}{3.2 / \sqrt{24}}=-0.77
$$

Do not reject the null hypothesis. The time is not less.
61. a. $H_{0}: \mu=80 \quad H_{1}: \mu \neq 80$

Reject $H_{0}$ if $t$ is not between -2.045 and 2.045.
$t=\frac{91.02-80}{38.26 / \sqrt{30}}=1.578 \quad$ Do not reject the null.
The mean payroll could be $\$ 80.0$ million.
b. $H_{0}: \mu \leq 2,000,000 \quad H_{1}: \mu>2,000,000$

Reject $H_{0}$ if $t$ is $>1.699$.
$t=\frac{2,436,000-2,000,000}{713,000 / \sqrt{30}}=3.349$
Reject the null. The mean attendance was more than 2,000,000.

## CHAPTER 11

1. a. Two-tailed test
b. Reject $H_{0}$ if $z<-2.05$ or $z>2.05$
c. $z=\frac{102-99}{\sqrt{\frac{5^{2}}{40}+\frac{6^{2}}{50}}}=2.59$
d. Reject $H_{0}$
e. $p$-value $=.0096$, found by $2(.5000-.4952)$
2. Step $1 H_{0}: \mu_{1} \geq \mu_{2} \quad H_{1}: \mu_{1}<\mu_{2}$

Step 2 The . 05 significance level was chosen.
Step 3 Reject $H_{0}$ if $z<-1.645$.
Step $4-0.94$, found by:

$$
z=\frac{7.6-8.1}{\sqrt{\frac{(2.3)^{2}}{40}}+\frac{(2.9)^{2}}{55}}=-0.94
$$

Step 5 Do not reject $H_{0}$. Babies using the Gibbs brand did not gain less weight. $p$-value $=.1736$, found by $.5000-.3264$.
5. $H_{0}: \mu_{1} \leq \mu_{2} \quad H_{1}: \mu_{1}>\mu_{2}$ If $z>1.645$, reject $H_{0}$.

$$
z=\frac{61.4-60.6}{\sqrt{\frac{(1.2)^{2}}{45}+\frac{(1.1)^{2}}{39}}}=3.187
$$

Reject the null. It is reasonable to conclude that those who had a Caesarean section are shorter.
The $p$-value is virtually zero. That much of a difference could almost never be due to sampling error.
7. a. $H_{0}$ is rejected if $z>1.645$.
b. 0.64 , found by $p_{c}=\frac{70+90}{100+150}$
c. 1.61 , found by

$$
z=\frac{0.70-0.60}{\sqrt{[(0.64 \times 0.36) / 100]+[(0.64 \times 0.36) / 150]}}
$$

d. $H_{0}$ is not rejected.
9. a. $H_{0}: \pi_{1}=\pi_{2} \quad H_{1}: \pi_{1} \neq \pi_{2}$
b. $H_{0}$ is rejected if $z<-1.96$ or $z>1.96$.
c. $p_{c}=\frac{24+40}{400+400}=0.08$
d. -2.09 , found by

$$
z=\frac{0.06-0.10}{\sqrt{[(0.08 \times 0.92) / 400]+[(0.08 \times 0.92) / 400]}}
$$

e. $H_{0}$ is rejected. The proportion infested is not the same in the two fields.
11. $H_{0}: \pi_{d} \leq \pi_{r} \quad H_{1}: \pi_{d}>\pi_{r}$
$H_{0}$ is rejected if $z>2.05$.

$$
\begin{aligned}
p_{c} & =\frac{168+200}{800+1,000}=0.2044 \\
z & =\frac{0.21-0.20}{\sqrt{\frac{(0.2044)(0.7956)}{800}+\frac{(0.2044)(0.7956)}{1,000}}}=0.52
\end{aligned}
$$

$H_{0}$ is not rejected. We cannot conclude that a larger proportion of Democrats favor lowering the standards. $p$-value $=0.3015$.
13. a. Reject $H_{0}$ if $t>2.120$ or $t<-2.120$.
$d f=10+8-2=16$
b. $s_{p}^{2}=\frac{(10-1)(4)^{2}+(8-1)(5)^{2}}{10+8-2}=19.9375$
c. $t=\frac{23-26}{\sqrt{19.9375\left(\frac{1}{10}+\frac{1}{8}\right)}}=-1.416$
d. Do not reject $H_{0}$.
e. $p$-value is greater than 0.10 and less than 0.20 .
15. $H_{0}: \mu_{1}=\mu_{2} \quad H_{1}: \mu_{1} \neq \mu_{2}$
$d f=n_{1}+n_{2}-2=16+14-2=28$
Reject $H_{0}$ if $t>2.376$ or $t<-2.376$.
$s_{p}^{2}=\frac{(16-1)(9380.646)^{2}+(14-1)(7547.931)^{2}}{16+14-2}=73,591,939.53$

$$
t=\frac{5906-7500}{\sqrt{73,791,939.53\left(\frac{1}{16}+\frac{1}{14}\right)}}=-0.5075
$$

Do not reject $H_{0}$. The data do not suggest any statistical difference between the average salaries of pitchers versus position players.
17. $H_{0}: \mu_{s} \leq \mu_{a} \quad H_{1}: \mu_{s}>\mu_{a}$
$d f=6+7-2=11$
Reject $H_{0}$ if $t>1.363$.

$$
\begin{aligned}
s_{p}^{2} & =\frac{(6-1)(12.2)^{2}+(7-1)(15.8)^{2}}{6+7-2}=203.82 \\
t & =\frac{142.5-130.3}{\sqrt{203.82\left(\frac{1}{6}+\frac{1}{7}\right)}}=1.536
\end{aligned}
$$

Reject $H_{0}$. The mean daily expenses are greater for the sales staff. The $p$-value is between 0.05 and 0.10 .
19. a. Reject $H_{0}$ if $t>2.353$.
b. $\bar{d}=\frac{12}{4}=3.00 \quad s_{d}=\sqrt{\frac{2}{3}}=0.816$
c. $t=\frac{3.00}{0.816 / \sqrt{4}}=7.35$
d. Reject $H_{0}$. There are more defective parts produced on the day shift.
e. $p$-value is less than 0.005 , but greater than 0.0005 .
21. $H_{0}: \mu_{d} \leq 0 \quad H_{1}: \mu_{d}>0$
$\bar{d}=25.917$
$s_{d}=40.791$
Reject $H_{0}$ if $t>1.796$

$$
t=\frac{25.917}{40.791 / \sqrt{12}}=2.20
$$

Reject $H_{0}$. The incentive plan resulted in an increase in weekly income. The $p$-value is about . 025 .
23. $H_{0}: \mu_{m}=\mu_{w} \quad H_{1}: \mu_{m} \neq \mu_{w}$

Reject $H_{0}$ if $z>2.576$ or $t<-2.576$.

$$
z=\frac{24.51-22.69}{\sqrt{\left(\frac{4.48^{2}}{35}+\frac{3.86^{2}}{40}\right)}}=1.871
$$

Do not reject $H_{0}$. The $p$-value is 0.0614 , found by $2(0.5000-$ 0.4693).
25. $H_{0}: \mu_{1}=\mu_{2} ; \quad H_{1}: \mu_{1} \neq \mu_{2}$

Reject $H_{0}$ if $z<-1.96$ or $z>1.96$.

$$
z=\frac{4.77-5.02}{\sqrt{\frac{(1.05)^{2}}{40}+\frac{(1.23)^{2}}{50}}}=-1.04
$$

$H_{0}$. is not rejected. There is no difference in the mean number of calls. $p$-value $=2(0.5000-$ $0.3508)=0.2984$.
27. $H_{0}: \mu_{B} \leq \mu_{A} \quad H_{1}: \mu_{B}>\mu_{A}$. $d f=n_{\mathrm{B}}+n_{\mathrm{A}}-2=30+40-2=68$ Reject $H_{0}$ if $t>1.668$

$$
\begin{aligned}
s_{p}^{2} & =\frac{(30-1)(7100)^{2}+(40-1)(9200)^{2}}{30+40-2}=70,041,911.76 \\
t & =\frac{61,000-57,000}{\sqrt{70,041,911.76\left(\frac{1}{30}+\frac{1}{40}\right)}}=1.979
\end{aligned}
$$

Reject $H_{0}$. The mean income of Plan $B$ subscribers is greater than that of Plan A subscribers. The $p$-value is between 0.025 and 0.010 .
29. $H_{0}: \pi_{1} \leq \pi_{2} \quad H_{1}: \pi_{1}>\pi_{2}$ Reject $H_{0}$ if $z>1.645$.

$$
\begin{aligned}
p_{c} & =\frac{180+261}{200+300}=0.882 \\
z & =\frac{0.90-0.87}{\sqrt{\frac{0.882(0.118)}{200}+\frac{0.882(0.118)}{300}}}=1.019
\end{aligned}
$$

$H_{0}$ is not rejected. There is no difference in the proportions that found relief with the new and the old drugs.
31. $H_{0}: \pi_{1} \leq \pi_{2} \quad H_{1}: \pi_{1}>\pi_{2}$

If $z>2.326$, reject $H_{0}$.

$$
\begin{aligned}
p_{c} & =\frac{990+970}{1,500+1,600}=0.63 \\
z & =\frac{.6600-.60625}{\sqrt{\frac{.63(.37)}{1,500}+\frac{.63(.37)}{1,600}}}=3.10
\end{aligned}
$$

Reject the null hypothesis. We can conclude the proportion of men who believe the division is fair is greater. The $p$-value is less than 0.001 .
33. $H_{0}: \pi_{1} \leq \pi_{2} \quad H_{1}: \pi_{1}>\pi_{2} \quad H_{0}$ is rejected if $z>1.645$.

$$
\begin{aligned}
p_{c} & =\frac{.091+.085}{2}=.088 \\
z & =\frac{0.091-0.085}{\sqrt{\frac{(0.088)(0.912)}{5000}+\frac{(0.088)(0.912)}{5000}}}=1.059
\end{aligned}
$$

$H_{0}$ is not rejected. There has not been an increase in the proportion calling conditions "good." The $p$-value is 0.1446 , found by $0.5000-0.3554$. The increase in the percentages will happen by chance in one out of every seven cases.
35. $H_{0}: \pi_{1}=\pi_{2} \quad H_{1}: \pi_{1} \neq \pi_{2}$
$H_{0}$ is rejected if $z$ is not between -1.96 and 1.96.
$p_{c}=\frac{100+36}{300+200}=.272$
$z=\frac{\frac{100}{300}-\frac{36}{200}}{\sqrt{\frac{(0.272)(0.728)}{300}+\frac{(0.272)(0.728)}{200}}}=3.775$
$H_{0}$ is rejected. There is a difference in the replies of the sexes.
37. $H_{0}: \mu_{1} \leq \mu_{2} \quad H_{1}: \mu_{1}>\mu_{2} \quad$ Reject $H_{0}$ if $t>2.650$.
$\bar{X}_{1}=125.125 \quad s_{1}=15.094$
$\bar{X}_{2}=117.714 \quad s_{2}=19.914$

$$
s_{p}^{2}=\frac{(8-1)(15.094)^{2}+(7-1)(19.914)^{2}}{8+7-2}=305.708
$$

$$
t=\frac{125.125-117.714}{\sqrt{305.708\left(\frac{1}{8}+\frac{1}{7}\right)}}=0.819
$$

$H_{0}$ is not rejected. There is no difference in the mean number sold at the regular price and the mean number sold at the reduced price.
39. $\underline{H}_{0}: \mu_{d} \leq 0 \quad H_{1}: \mu_{d}>0 \quad$ Reject $H_{0}$ if $t>1.895$.
$\bar{d}=1.75 \quad s_{d}=2.9155$
$t=\frac{1.75}{2.9155 / \sqrt{8}}=1.698$
Do not reject $H_{0}$. There is no difference in the mean number of absences. The $p$-value is greater than 0.05 but less than .10.
41. $H_{0}: \mu_{1}=\mu_{2} \quad H_{1}: \mu_{1} \neq \mu_{2}$

Reject $H_{0}$ if $t<-2.024$ or $t>2.204$.

$$
\begin{gathered}
s_{p}^{2}=\frac{(15-1)(40)^{2}+(25-1)(30)^{2}}{15+25-2}=1157.89 \\
t=\frac{150-180}{\sqrt{1157.89\left(\frac{1}{15}+\frac{1}{25}\right)}}=-2.699
\end{gathered}
$$

Reject the null hypothesis. The population means are different.
43. $H_{0}: \mu_{d} \leq 0 \quad H_{1}: \mu_{d}>0$

Reject $H_{0}$ if $t>1.895$.
$\bar{d}=3.11 \quad s_{d}=2.91$

$$
t=\frac{3.11}{2.91 / \sqrt{8}}=3.02
$$

Reject $H_{0}$. The mean is lower.
45. $H_{0}: \mu_{0}=\mu_{R} \quad H_{1}: \mu_{0} \neq \mu_{R}$
$d f=25+28-2=51$
Reject $H_{0}$ if $t<-2.008$ or $t>2.008$.
$\bar{X}_{O}=86.24, s_{O}=23.43$
$X_{R}=92.04, s_{R}=24.12$

$$
\begin{aligned}
s_{p}^{2} & =\frac{(25-1)(23.43)^{2}+(28-1)(24.12)^{2}}{25+28-2}=566.335 \\
t & =\frac{86.24-92.04}{\sqrt{566.335\left(\frac{1}{25}+\frac{1}{28}\right)}}=-0.886
\end{aligned}
$$

Do not reject $H_{0}$. There is no difference in the mean number of cars in the two lots.
47. Defining $d=($ Count at US $17-$ Count at SC 707)
$H_{0}: \mu_{d} \leq 0 \quad H_{1}: \mu_{d}>0 \quad d f=n-1=25-1=24$
Reject $H_{0}$ if $t>1.711$.

$$
\begin{aligned}
\bar{d} & =2.8 ; \quad S_{d}=6.589 \\
t & =\frac{2.8}{6.589 / \sqrt{25}}=2.125
\end{aligned}
$$

Reject $H_{0} ; p$-value $=0.022$. Based on automobile counts, the US 17 store has more business volume than the SC 707 store.
49. a. $\mu_{1}=$ without pool $\mu_{2}=$ with pool
$H_{0}: \mu_{1}=\mu_{2} \quad H_{1}: \mu_{1} \neq \mu_{2}$
Reject $H_{0}$ if $t>1.983$ or $t<-1.983$.

$$
\begin{gathered}
\bar{X}_{1}=202.8 \quad s_{1}=33.7 \quad n_{1}=38 \\
\bar{X}_{2}=231.5 \quad s_{2}=50.46 \quad n_{2}=67 \\
s_{p}^{2}=\frac{(38-1)(33.7)^{2}+(67-1)(50.46)^{2}}{38+67-2}=2,041.05 \\
t=\frac{202.8-231.5}{\sqrt{2,041.05\left(\frac{1}{38}+\frac{1}{67}\right)}}=-3.12
\end{gathered}
$$

Reject $H_{0}$. There is a difference in mean selling price for homes with and without a pool.
b. $\mu_{1}=$ without attached garage $\mu_{2}=$ with garage
$H_{0}: \mu_{1}=\mu_{2} \quad H_{1}: \mu_{1} \neq \mu_{2}$
Reject $H_{0}$ if $t>1.983$ or $t<-1.983$.

$$
\begin{aligned}
& \alpha=0.05 \quad d f=34+71-2=103 \\
& \bar{X}_{1}=185.45 \quad s_{1}=28.00 \\
& \bar{X}_{2}=238.18 \quad s_{2}=44.88 \\
& s_{p}^{2}=\frac{(34-1)(28.00)^{2}+(71-1)(44.88)^{2}}{103}=1,620.07 \\
& t=\frac{185.45-238.18}{\sqrt{1,620.07\left(\frac{1}{34}+\frac{1}{71}\right)}}=-6.28
\end{aligned}
$$

Reject $H_{0}$. There is a difference in mean selling price for homes with and without an attached garage.
c. $H_{0}: \mu_{1}=\mu_{2} \quad H_{1}: \mu_{1} \neq \mu_{2}$

Reject $H_{0}$ if $t>2.036$ or $t<-2.036$.
$\bar{X}_{1}=196.91 \quad s_{1}=35.78 \quad n_{1}=15$
$\bar{X}_{2}=227.45 \quad s_{2}=44.19 \quad n_{2}=20$

$$
\begin{aligned}
s_{p}^{2} & =\frac{(15-1)(35.78)^{2}+(20-1)(44.19)^{2}}{15+20-2}=1,667.43 \\
t & =\frac{196.91-227.45}{\sqrt{1,667.43\left(\frac{1}{15}+\frac{1}{20}\right)}}=-2.19
\end{aligned}
$$

Reject $H_{0}$. There is a difference in mean selling price for homes in Township 1 and Township 2.
d. $H_{0}: \pi_{1}=\pi_{2} \quad H_{1}: \pi_{1} \neq \pi_{2}$

If $z$ is not between -1.96 and 1.96, reject $H_{0}$.

$$
\begin{gathered}
p_{c}=\frac{24+43}{52+53}=0.64 \\
z=\frac{0.462-0.811}{\sqrt{0.64 \times 0.36 / 52+0.64 \times 0.36 / 53}}=-3.73
\end{gathered}
$$

Reject the null hypothesis. There is a difference.
51. $H_{0}: \mu_{1}=\mu_{2} \quad H_{1}: \mu_{1} \neq \mu_{2}$

If $t$ is not between -1.991 and 1.991, reject $H_{0}$.

$$
\begin{gathered}
s_{p}^{2}=\frac{(53-1)(52.9)^{2}+(27-1)(55.1)^{2}}{53+27-2}=2878 \\
t=\frac{454.8-441.5}{\sqrt{2878\left(\frac{1}{53}+\frac{1}{27}\right)}}=1.05
\end{gathered}
$$

Do not reject $H_{0}$. There may be no difference in the mean maintenance cost for the two types of buses.

## CHAPTER 12

1. 9.01 , from Appendix B. 4
2. Reject $H_{0}$ if $F>10.5$, where degrees of freedom in the numerator are 7 and 5 in the denominator. Computed $F=2.04$, found by

$$
F=\frac{s_{1}^{2}}{s_{2}^{2}}=\frac{(10)^{2}}{(7)^{2}}=2.04
$$

Do not reject $H_{0}$. There is no difference in the variations of the two populations.
5. $H_{0}: \sigma_{1}^{2}=\sigma_{2}^{2} \quad H_{1}: \sigma_{1}^{2} \neq \sigma_{2}^{2}$

Reject $H_{0}$ where $F>3.10$. (3.10 is about halfway between 3.14 and 3.07.) Computed $F=1.44$, found by:

$$
F=\frac{(12)^{2}}{(10)^{2}}=1.44
$$

Do not reject $H_{0}$. There is no difference in the variations of the two populations.
7. a. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3} ; H_{1}$ : Treatment means are not all the same.
b. Reject $H_{0}$ if $F>4.26$.
c \& d.

| Source | SS | $\boldsymbol{d f}$ | MS | $\boldsymbol{F}$ |
| :--- | :---: | ---: | ---: | :---: |
| Treatment | 62.17 | 2 | 31.08 | 21.94 |
| Error | $\frac{12.75}{74.92}$ | $\frac{9}{11}$ | 1.42 |  |
| $\quad$ Total |  |  |  |  |

e. Reject $H_{0}$. The treatment means are not all the same.
9. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3} ; H_{1}$ : Treatment means are not all the same. Reject $H_{0}$ if $F>4.26$.

| Source | SS | df | MS | $\boldsymbol{F}$ |
| :--- | ---: | :---: | ---: | :---: |
| Treatment | 276.50 | 2 | 138.25 | 14.18 |
| Error | 87.75 | 9 | 9.75 |  |

Reject $H_{0}$. The treatment means are not all the same.
11. a. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3} ; H_{1}$ : Not all means are the same.
b. Reject $H_{0}$ if $F>4.26$.
c. SST $=107.20$, SSE $=9.47$, SS total $=116.67$.
d.

| Source | SS | $\boldsymbol{d f}$ | MS | $\boldsymbol{F}$ |
| :--- | :---: | ---: | :---: | :---: |
| Treatment | 107.20 | 2 | 53.600 | 50.96 |
| Error | $\frac{9.47}{116.67}$ | $\frac{9}{11}$ | 1.052 |  |
| $\quad$ Total | 16 |  |  |  |

e. Since $50.96>4.26, H_{0}$ is rejected. At least one of the means differs.
f. $\left(\bar{X}_{1}-\bar{X}_{2}\right) \pm t \sqrt{\operatorname{MSE}\left(1 / n_{1}+1 / n_{2}\right)}$
$=(9.667-2.20) \pm 2.262 \sqrt{1.052(1 / 3+1 / 5)}$
$=7.467 \pm 1.69$
$=$ [5.777, 9.157]
Yes, we can conclude that treatments 1 and 2 have different means.
13. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3}=\mu_{4} ; H_{1}$ : Not all means are equal. $H_{0}$ is rejected if $F>3.71$.

| Source | SS | $\boldsymbol{d f}$ | MS | $\boldsymbol{F}$ |
| :--- | :---: | ---: | :---: | :---: |
| Treatment | 32.33 | 3 | 10.77 | 2.36 |
| Error | $\frac{45.67}{78.00}$ | $\frac{10}{13}$ | 4.567 |  |
| $\quad$ Total | 7 |  |  |  |

Because 2.36 is less than $3.71, H_{0}$ is not rejected. There is no difference in the mean number of weeks.
15. $H_{0}: \sigma_{1}^{2} \leq \sigma_{2}^{2} ; H_{1}: \sigma_{1}^{2}>\sigma_{2}^{2}$. $d f_{1}=21-1=20$;
$d f_{2}=18-1=17 . H_{0}$ is rejected if $F>3.16$.

$$
F=\frac{(45,600)^{2}}{(21,330)^{2}}=4.57
$$

Reject $H_{0}$. There is more variation in the selling price of oceanfront homes.
17. Sharkey: $n=7 \quad s_{s}=14.79$

White: $n=8 \quad s_{w}=22.95$
$H_{0}: \sigma_{w}^{2} \leq \sigma_{s}^{2} ; H_{1}: \sigma_{w}^{2}>\sigma_{s}^{2} . d f_{s}=7-1=6$;
$d f_{w}=8-1=7$. Reject $H_{0}$ if $F>8.26$.

$$
F=\frac{(22.95)^{2}}{(14.79)^{2}}=2.41
$$

Cannot reject $H_{0}$. There is no difference in the variation of the monthly sales.
19. a. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3}=\mu_{4}$
$H_{1}$ : Treatment means are not all equal.
b. $\alpha=.05$ Reject $H_{0}$ if $F>3.10$.
c.

| Source | SS | $\boldsymbol{d f}$ | MS | $\boldsymbol{F}$ |
| :--- | ---: | :---: | :--- | :---: |
| Treatment | 50 | $4-1=3$ | $50 / 3$ | 1.67 |
| Error | $\underline{200}$ | $\underline{24-4=20}$ | 10 |  |
| $\quad$ Total | $\underline{250}$ | $\underline{24-1=23}$ |  |  |

d. Do not reject $H_{0}$.
21. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3} ; H_{1}$ : Not all treatment means are equal. $H_{0}$ is rejected if $F>3.89$.

| Source | ss | $\boldsymbol{d f}$ | MS | $\boldsymbol{F}$ |
| :--- | :---: | ---: | ---: | :---: |
| Treatment | 63.33 | 2 | 31.667 | 13.38 |
| Error | $\underline{28.40}$ | $\underline{12}$ | 2.367 |  |
| $\quad$ Total | 91.73 | 14 |  |  |

$H_{0}$ is rejected. There is a difference in the treatment means.
23. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3}=\mu_{4} ; H_{1}$ : Not all means are equal. $H_{0}$ is rejected if $F>3.10$.

| Source | SS | $\boldsymbol{d f}$ | MS | $\boldsymbol{F}$ |
| :--- | :---: | ---: | ---: | :---: |
| Factor | 87.79 | 3 | 29.26 | 9.12 |
| Error | $\frac{64.17}{151.96}$ | $\underline{20}$ | 3.21 |  |
| $\quad$ Total | 23 |  |  |  |

Because the computed $F$ of $9.12>3.10$, the null hypothesis of no difference is rejected at the .05 level.
25. a. $H_{0}: \mu_{1}=\mu_{2} ; H_{1}: \mu_{1} \neq \mu_{2}$. Critical value of $F=4.75$.

| Source | SS | df | MS | $\boldsymbol{F}$ |
| :--- | :---: | :---: | :---: | :---: |
| Treatment | 219.43 | 1 | 219.43 | 23.10 |
| Error | $\underline{114.00}$ | $\underline{12}$ | 9.5 |  |
| $\quad$ Total | 333.43 | 13 |  |  |

b. $t=\frac{19-27}{\sqrt{9.5\left(\frac{1}{6}+\frac{1}{8}\right)}}=-4.806$

Then $t^{2}=F$. That is $(-4.806)^{2}=23.10$.
c. $H_{0}$ is rejected. There is a difference in the mean scores.
27. The null hypothesis is rejected because the $F$ statistic (8.26) is greater than the critical value (5.61) at the .01 significance level. The $p$-value (.0019) is also less than the significance level. The mean gasoline mileages are not the same.
29. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3}=\mu_{4} . \quad H_{1}$ : At least one mean is different. Reject $H_{0}$ if $F>2.7395$. Since 2.72 is less than 2.7395, $H_{0}$ is
not rejected. You can also see this conclusion from the $p$-value of 0.051 , which is greater than 0.05 . There is no difference in the means for the different types of first-class mail.
31. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3}=\mu_{4} ; H_{1}$ : The treatment means are not equal. Reject $H_{0}$ : if $F>2.76$.

| Source | $\boldsymbol{d f}$ | SS | MS | $\boldsymbol{F}$ |
| :--- | ---: | ---: | ---: | :---: |
| Treatment | 3 | 1,552 | 517 | 1.84 |
| Error | $\frac{60}{63}$ | $\frac{16,846}{18,399}$ | 281 |  |
| $\quad$ Total |  |  |  |  |

Because the computed $F$ of $1.84<2.76$, do not reject the null hypothesis of no difference at the 0.05 level. The mean proportions of stock investment could be the same for all age groups.
33. a.
$H_{0}: \sigma_{n p}^{2}=\sigma_{p}^{2} \quad H_{1}: \sigma_{n p}^{2} \neq \sigma_{p}^{2}$
Reject $H_{0}$ if $F>2.05$ (estimated).
$d f_{1}=67-1=66 ; d f_{2}=38-1=37$

$$
F=\frac{(50.57)^{2}}{(33.71)^{2}}=2.25
$$

Reject $H_{0}$. There is a difference in the variance of the two selling prices.
b. $H_{0}: \sigma_{g}^{2}=\sigma_{n g}^{2} ; H_{1}: \sigma_{g}^{2} \neq \sigma_{n g}^{2}$.

Reject $H_{0}$ if $F>2.21$ (estimated).

$$
F=\frac{(44.88)^{2}}{(28.00)^{2}}=2.57
$$

Reject $H_{0}$. There is a difference in the variance of the two selling prices.
c.

| Source | SS | $\boldsymbol{d f}$ | MS | $\boldsymbol{F}$ |
| :--- | ---: | ---: | ---: | :---: |
| Township | 13,263 | 4 | 3,316 | 1.52 |
| Error | $\underline{217,505}$ | $\frac{100}{230,768}$ | 2,175 |  |
| $\quad$ Total | $\mathbf{1 0 4}$ |  |  |  |

$H_{0}: \mu_{1}=\mu_{2}=\mu_{3}=\mu_{4}=\mu_{5} ; H_{1}$ : Not all treatment means are equal. Reject $H_{0}$ if $F>2.46$.
Do not reject $H_{0}$. There is no difference in the mean selling prices in the five townships.
35. a. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3} \quad H_{1}$ : Not all treatment means are equal. Reject $H_{0}$ if $F>4.89$.

| Source | SS | $\boldsymbol{d f}$ | MS | $\boldsymbol{F}$ |
| :--- | ---: | ---: | ---: | :---: |
| Treatment | 28,996 | 2 | 14,498 | 5.62 |
| Error | $\underline{198,696}$ | $\frac{77}{79}$ | 2,580 |  |
| $\quad$ Total | 227,692 |  |  |  |

Reject $H_{0}$. The mean maintenance costs are different.
b. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3} \quad H_{1}$ : Not all treatment means are equal. Reject $H_{0}$ if $F>3.12$.

| Source | SS | $\boldsymbol{d f}$ | MS | $\boldsymbol{F}$ |
| :--- | ---: | ---: | :---: | :---: |
| Treatment | 5,095 | 2 | 2,547 | 1.45 |
| Error | $\frac{135,513}{140,608}$ | $\frac{77}{79}$ | 1,760 |  |
| $\quad$ Total |  |  |  |  |

Do not reject $H_{0}$. The mean miles traveled are not different.
c. $(441.81-506.75) \pm 1.991 \sqrt{2580\left(\frac{1}{47}+\frac{1}{8}\right)}$

This reduces to $-64.94 \pm 38.68$, so the difference is between -103.62 and -26.26 . To put it another way, Bluebird is less costly than Thompson by an amount between $\$ 26.26$ and $\$ 103.62$.

CHAPTER 13

1. $\quad \Sigma(X-\bar{X})(Y-\bar{Y})=10.6, s_{x}=2.7019, s_{y}=1.3038$

$$
r=\frac{10.6}{(5-1)(2.7019)(1.3038)}=0.7522
$$

3. a. Sales.
b.

c. $\Sigma(X-\bar{X})(Y-\bar{Y})=36, n=5, s_{x}=1.5811$, $s_{y}=6.1237$

$$
r=\frac{36}{(5-1)(1.5811)(6.1237)}=0.9295
$$

d. There is a strong positive association between the variables.
5. a. Police is the independent variable, and crime is the dependent variable.
b.

c. $n=8, \Sigma(X-\bar{X})(Y-\bar{Y})=-231.75$, $s_{x}=5.8737, s_{y}=6.4462$

$$
r=\frac{-231.75}{(8-1)(5.8737)(6.4462)}=-0.8744
$$

d. Strong inverse relationship. As the number of police increases, the crime decreases.
7. Reject $H_{0}$ if $t>1.812$.

$$
t=\frac{.32 \sqrt{12-2}}{\sqrt{1-(.32)^{2}}}=1.068
$$

Do not reject $H_{0}$.
9. $H_{0}: \rho \leq 0 ; H_{1}: \rho>0$. Reject $H_{0}$ if $t>2.552$. $d f=18$.

$$
t=\frac{.78 \sqrt{20-2}}{\sqrt{1-(.78)^{2}}}=5.288
$$

Reject $H_{0}$. There is a positive correlation between gallons sold and the pump price.
11. $H_{0}: \rho \leq 0 \quad H_{1}: \rho>0$

Reject $H_{0}$ if $t>2.650$.

$$
t=\frac{0.667 \sqrt{15-2}}{\sqrt{1-0.667^{2}}}=3.228
$$

Reject $H_{0}$. There is a positive correlation between the number of passengers and plane weight.
13. a. $\hat{Y}=3.7778+0.3630 X$

$$
\begin{aligned}
& b=0.7522\left(\frac{1.3038}{2.7019}\right)=0.3630 \\
& a=5.8-0.3630(5.6)=3.7671
\end{aligned}
$$

b. 6.3081 , found by $\hat{Y}=3.7671+0.3630(7)$
15. a. $\Sigma(X-\bar{X})(Y-\bar{Y})=44.6, s_{x}=2.726, s_{y}=2.011$

$$
\begin{aligned}
& r=\frac{44.6}{(10-1)(2.726)(2.011)}=.904 \\
& b=.904\left(\frac{2.011}{2.726}\right)=0.667 \\
& a=7.4-.677(9.1)=1.333
\end{aligned}
$$

b. $\hat{Y}=1.333+.667(6)=5.335$
17. a.

b. $\quad \Sigma(X-\bar{X})(Y-\bar{Y})=629.64, s_{x}=26.17, s_{y}=3.248$

$$
r=\frac{629.64}{(12-1)(26.17)(3.248)}=.6734
$$

c. $b=.6734\left(\frac{3.248}{26.170}\right)=0.0836$

$$
a=\frac{64.1}{12}-0.0836\left(\frac{501.10}{12}\right)=1.8507
$$

d. $\hat{Y}=1.8507+0.0836(50.0)=6.0307$ (\$ millions)
19. a. $b=-.8744\left(\frac{6.4462}{5.8737}\right)=-0.9596$

$$
a=\frac{95}{8}-(-0.9596)\left(\frac{146}{8}\right)=29.3877
$$

b. 10.1957, found by $29.3877-0.9596(20)$
c. For each policeman added, crime goes down by almost one.
21. $H_{0}: \beta \geq 0 \quad H_{1}: \beta<0 \quad d f=n-2=8-2=6$

Reject $H_{0}$ if $t<-1.943$.

$$
t=-0.96 / 0.22=-4.364
$$

Reject $H_{0}$ and conclude the slope is less than zero.
23. $H_{0}: \beta=0 \quad H_{1}: \beta \neq 0 \quad d f=n-2=12-2=10$

Reject $H_{0}$ if $t$ not between -2.228 and 2.228

$$
t=0.08 / 0.03=2.667
$$

Reject $H_{0}$ and conclude the slope is different from zero.
25. The standard error of estimate is 3.379 , found by $\sqrt{\frac{68.4877}{8-2}}$.

The coefficient of determination is 0.76 , found by $(-0.874)^{2}$. Seventy-six percent of the variation in crimes can be explained by the variation in police.
27. The standard error of estimate is 0.913 , found by $\sqrt{\frac{6.667}{10-2}}$. The coefficient of determination is 0.82 , found by 29.733/36.4.

Eighty-two percent of the variation in kilowatt hours can be explained by the variation in the number of rooms.
29. a. $r^{2}=\frac{1000}{1500}=.6667$
b. $r=\sqrt{.6667}=.8165$
c. $s_{y . x}=\sqrt{\frac{500}{13}}=6.2017$
31. a. $6.308 \pm(3.182)(.993) \sqrt{.2+\frac{(7-5.6)^{2}}{29.2}}$
$=6.308 \pm 1.633$
$=[4.675,7.941]$
b. $6.308 \pm(3.182)(.993) \sqrt{1+1 / 5+.0671}$
$=[2.751,9.865]$
33. a. $4.2939,6.3721$
b. $2.9854,7.6806$
35. No, relationship is nonlinear. Correlation coefficient is 0.298 . The correlation is 0.298 Yes, transformed relationship is linear. Correlation coefficient is 0.99 .
37. $H_{0}: \rho \leq 0 ; H_{1}: \rho>0$. Reject $H_{0}$ if $t>1.714$.

$$
t=\frac{.94 \sqrt{25-2}}{\sqrt{1-(.94)^{2}}}=13.213
$$

Reject $H_{0}$. There is a positive correlation between passengers and weight of luggage.
39. $H_{0}: \rho \leq 0 ; H_{1}: \rho>0$. Reject $H_{0}$ if $t>2.764$.

$$
t=\frac{.47 \sqrt{12-2}}{\sqrt{1-(.47)^{2}}}=1.684
$$

Do not reject $H_{0}$. There is not a positive correlation between engine size and performance. $p$-value is greater than .05 , but less than .10.
41. a.


The sales volume is inversely related to their market share.
b. $\bar{X}=\frac{154.1}{13}=11.854 \quad \bar{Y}=\frac{503.5}{13}=38.7308$

$$
\begin{gathered}
s_{x}=\sqrt{\frac{163.032}{12}}=3.686 \quad s_{y}=\sqrt{\frac{1154.41}{12}}=9.808 \\
r=\frac{-299.792}{(13-1)(3.686)(9.808)}=-0.691
\end{gathered}
$$

c. $H_{0}: \rho \geq 0 \quad H_{1}: \rho<0$

Reject $H_{0}$ if $t<-2.718$.
$d f=11 \quad t=\frac{-0.691 \sqrt{13-2}}{\sqrt{1-(-0.691)^{2}}}=-3.17$
Reject $H_{0}$. There is a negative correlation between cars sold and market share.
d. $47.7 \%$, found by $(-0.691)^{2}$, of the variation in market share is accounted for by variation in cars sold.
43. a. $r=-0.241$
b. $R^{2}=(-0.241)^{2}=0.0581$; relationship is very weak
c. $H_{0}: \rho \geq 0 ; H_{1}: \rho<0$. Reject $H_{0}$ if $t<-1.697$

$$
t=\frac{-0.241 \sqrt{32-2}}{\sqrt{1-(-0.241)^{2}}}=-1.36
$$

Do not reject $H_{0}$. There is not enough evidence to suggest that points scored and points allowed per game are negatively or inversely related.
45. a.


There is an inverse relationship between the variables. As the months owned increase, the number of hours exercised decreases.
b. $r=-0.827$
c. $H_{0}: \rho \geq 0 ; H_{1}: \rho<0$. Reject $H_{0}$ if $t<-2.896$.

$$
t=\frac{-0.827 \sqrt{10-2}}{\sqrt{1-(-0.827)^{2}}}=-4.16
$$

Reject $H_{0}$. There is a negative association between months owned and hours exercised.
47. a. Median age and population are directly related.
b. $r=\frac{11.93418}{(10-1)(2.207)(1.330)}=0.452$
c. The slope of 0.272 indicates that for each increase of 1 million in the population, the median age increases on average by 0.272 years.
d. The median age is 32.08 years, found by $31.4+0.272(2.5)$.
e. The $p$-value ( 0.190 ) for the population variable is greater than, say, 0.05. A test for significance of that coefficient would fail to be rejected. In other words, it is possible the population coefficient is zero.
f. $H_{0}: \rho=0 \quad H_{1}: \rho \neq 0$ Reject $H_{0}$ if $t$ is not between -2.306 and 2.306.
$d f=8 \quad t=\frac{0.452 \sqrt{10-2}}{\sqrt{1-(0.452)^{2}}}=1.433$
Do not reject $H_{0}$.
There may be no relationship between age and population.
49. a. $b=-0.4667, a=11.2358$
b. $\hat{Y}=11.2358-0.4667(7.0)=7.9689$
c. $7.9689 \pm(2.160)(1.114) \sqrt{1+\frac{1}{15}+\frac{(7-7.1333)^{2}}{73.7333}}$
$=7.9689 \pm 2.4854$
$=[5.4835,10.4543]$
d. $r^{2}=0.499$. Nearly $50 \%$ of the variation in the amount of the bid is explained by the number of bidders.
51. a. 15


There appears to be a relationship between the two variables. As the distance increases, so does the shipping time.
b. $r=2.004$
$H_{0}: \rho \leq 0 ; H_{1}: \rho>0$. Reject $H_{0}$ if $t>1.734$.

$$
t=\frac{0.692 \sqrt{20-2}}{\sqrt{1-(0.692)^{2}}}=4.067
$$

$H_{0}$ is rejected. There is a positive association between shipping distance and shipping time.
c. $r^{2}=0.479$. Nearly half of the variation in shipping time is explained by shipping distance.
d. $s_{y \cdot x}=2.004$
53. a. $b=2.41$
$a=26.8$
The regression equation is: Price $=26.8+2.41 \times$ Dividend. For each additional dollar of dividend, the price increases by $\$ 2.41$.
b. $r^{2}=\frac{5,057.6}{7,682.7}=0.658 \quad$ Thus, $65.8 \%$ of the variation in price is explained by the dividend.
c. $r=\sqrt{.658}=0.811 \quad H_{0}: \rho \leq 0 \quad H_{1}: \rho>0$ At the $5 \%$ level, reject $H_{0}$ when $t>1.701$.

$$
t=\frac{0.811 \sqrt{30-2}}{\sqrt{1-(0.811)^{2}}}=7.34
$$

Thus, $H_{0}$ is rejected. The population correlation is positive.
55. a. 35
b. $s_{y \cdot x}=\sqrt{29,778,406}=5,456.96$
c. $r^{2}=\frac{13,548,662,082}{14,531,349,474}=0.932$
d. $r=\sqrt{0.932}=0.966$
e. $H_{0}: \rho \leq 0, H_{1}: \rho>0$; reject $H_{0}$ if $t>1.692$.

$$
t=\frac{.966 \sqrt{35-2}}{\sqrt{1-(.966)^{2}}}=21.46
$$

Reject $H_{0}$. There is a direct relationship between size of the house and its market value.
57. a. The regression equation is Price $=-773+1,408$ Speed.
b. The second laptop $(1.6,922)$ with a residual of -557.60 , is priced $\$ 557.60$ below the predicted price. That is a noticeable "bargain."
c. The correlation of Speed and Price is 0.835 .
$H_{0}: \rho \leq 0 \quad H_{1}: \rho>0 \quad$ Reject $H_{0}$ if $t>1.8125$.

$$
t=\frac{0.835 \sqrt{12-2}}{\sqrt{1-(0.835)^{2}}}=4.799
$$

Reject $H_{0}$. It is reasonable to say the population correlation is positive.
59. a. $r=.987, H_{0}: \rho \leq 0, H_{1}: \rho>0$. Reject $H_{0}$ if $t>1.746$.

$$
t=\frac{.987 \sqrt{18-2}}{\sqrt{1-(.987)^{2}}}=24.564
$$

b. $\hat{Y}=-29.7+22.93 X$; an additional cup increases the dog's weight by almost 23 pounds.
c. Dog number 4 is an overeater.
61. a.


The relationship is direct. Fares increase for longer flights.
b. The correlation of Distance and Fare is 0.656 .
$H_{0}: \rho \leq 0 \quad H_{1}: \rho>0$
Reject $H_{0}$ if $t>1.701 \quad d f=28$

$$
t=\frac{0.656 \sqrt{30-2}}{\sqrt{1-(0.656)^{2}}}=4.599
$$

Reject $H_{0}$. There is a significant positive correlation between fares and distances.
c. $43 \%$, found by $(0.656)^{2}$, of the variation in fares is explained by the variation in distance.
d. The regression equation is Fare $=147.08+0.05265$ Distance. Each additional mile adds $\$ 0.05265$ to the fare. A 1,500-mile flight would cost $\$ 226.06$, found by $\$ 147.08+0.05265(1500)$.
e. A flight of 4,218 miles is outside the range of the sampled data. So the regression equation may not be useful.
63. a. There does seem to be a direct relationship between the variables.

b. $(71.86+.1004(100))=81.90$ wins
c. $(.1004 \times 5)=.5020$ wins
d. $H_{0}: \beta \leq 0 ; H_{1}: \beta>0$. $d f=n-2=30-2=28$

Reject $H_{0}$ if $t>1.701 . t=0.1004 / 0.05094=1.97$
Reject $H_{0}$ and conclude the slope is positive.
e. 0.1218 , or $12.18 \%$, found by $427.86 / 3512.00$
f. The correlation between wins and batting average is 0.461 ; the correlation between wins and ERA is -0.681 . The relationship between wins and ERA is stronger. For batting average: $H_{0}: \rho \leq 0 ; H_{1}: \rho>0$.
Reject $H_{0}$ if $t>1.701$.

$$
t=\frac{0.461 \sqrt{30-2}}{\sqrt{1-(0.461)^{2}}}=2.749
$$

Rejected $H_{0}$. Team wins and team batting average are positively related.
For ERA, $H_{0}: \rho \geq 0 ; H_{1}: \rho<0$.
Reject $H_{0}$ if $t<-1.701$.

$$
t=\frac{-0.681 \sqrt{30-2}}{\sqrt{1-(-0.681)^{2}}}=-4.921
$$

Rejected $H_{0}$. Team wins and ERA are inversely related.

## CHAPTER 14

1. a. Multiple regression equation
b. The $Y$-intercept
c. $\hat{Y}=64,100+0.394(796,000)+9.6(6,940)$

$$
-11,600(6.0)=\$ 374,748
$$

3. a. 497.736, found by
$\hat{Y}=16.24+0.017(18)$

$$
\begin{aligned}
& +0.0028(26,500)+42(3) \\
& +0.0012(156,000) \\
& +0.19(141)+26.8(2.5)
\end{aligned}
$$

b. Two more social activities. Income added only 28 to the index; social activities added 53.6.
5. a. $s_{Y \cdot 12}=\sqrt{\frac{\text { SSE }}{n-(k+1)}}=\sqrt{\frac{583.693}{65-(2+1)}}$
$=\sqrt{9.414}=3.068$
$95 \%$ of the residuals will be between $\pm 6.136$, found by 2(3.068).
b. $R^{2}=\frac{\mathrm{SSR}}{\mathrm{SS} \text { total }}=\frac{77.907}{661.6}=.118$

The independent variables explain 11.8\% of the variation.
c. $R_{a d j}^{2}=1-\frac{\frac{\text { SSE }}{n-(k+1)}}{\frac{\text { SS total }}{n-1}}=1-\frac{\frac{583.693}{65-(2+1)}}{\frac{661.6}{65-1}}$

$$
=1-\frac{9.414}{10.3375}=1-.911=.089
$$

7. a. $\hat{Y}=84.998+2.391 X_{1}-0.4086 X_{2}$
b. 90.0674 , found by $\hat{Y}=84.998+2.391(4)-0.4086(11)$
c. $n=65$ and $k=2$
d. $H_{0}: \beta_{1}=\beta_{2}=0 \quad H_{1}$ : Not all $\beta$ 's are 0 Reject $H_{0}$ if $F>3.15$.
$F=4.14$, reject $H_{0}$. Not all net regression coefficients equal zero.
e. For $X_{1} \quad$ For $X_{2}$
$H_{0}: \beta_{1}=0 \quad H_{0}: \beta_{2}=0$
$H_{1}: \beta_{1} \neq 0 \quad H_{1}: \beta_{2} \neq 0$
$t=1.99 \quad t=-2.38$
Reject $H_{0}$ if $t>2.0$ or $t<-2.0$.
Delete variable 1 and keep 2.
f. The regression analysis should be repeated with only $X_{2}$ as the independent variable.
8. a. The regression equation is: Performance $=29.3+5.22$ Aptitude + 22.1 Union

| Predictor | Coef | SE Coef | T | P |
| :--- | ---: | ---: | ---: | ---: |
| Constant | 29.28 | 12.77 | 2.29 | 0.041 |
| Aptitude | 5.222 | 1.702 | 3.07 | 0.010 |
| Union | 22.135 | 8.852 | 2.50 | 0.028 |


| Analysis of Variance |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Source | DF | SS | MS | F | P |
| Regression | 2 | 3919.3 | 1959.6 | 6.85 | 0.010 |
| Residual Error | 12 | 3434.0 | 286.2 |  |  |
| Total |  | 7353.3 |  |  |  |

b. These variables are effective in predicting performance. They explain $45.5 \%$ of the variation in performance. In particular, union membership increases the typical performance by 22.1.
c. $H_{0}: \beta_{2}=0 \quad H_{1}: \beta_{2} \neq 0$

Reject $H_{0}$ if $t<-2.179$ or $t>2.179$.
Since 2.50 is greater than 2.179 , we reject the null hypothesis and conclude that union membership is significant and should be included.
11. a. $n=40$
b. 4
c. $R^{2}=\frac{750}{1250}=.60$
d. $s_{y \cdot 1234}=\sqrt{500 / 35}=3.7796$
e. $H_{0}: \beta_{1}=\beta_{2}=\beta_{3}=\beta_{4}=0$
$H_{1}$ : Not all the $\beta$ s equal zero.
$H_{0}$ is rejected if $F>2.65$.

$$
F=\frac{750 / 4}{500 / 35}=13.125
$$

$H_{0}$ is rejected. At least one $\beta_{i}$ does not equal zero.
13. a. $n=26$
b. $R^{2}=100 / 140=.7143$
c. 1.4142 , found by $\sqrt{2}$
d. $H_{0}: \beta_{1}=\beta_{2}=\beta_{3}=\beta_{4}=\beta_{5}=0$
$H_{1}$ : Not all the $\beta$ s are 0 .
$H_{0}$ is rejected if $F>2.71$.
Computed $F=10.0$. Reject $H_{0}$. At least one regression coefficient is not zero.
e. $H_{0}$ is rejected in each case if $t<-2.086$ or $t>2.086$. $X_{1}$ and $X_{5}$ should be dropped.
15. a. $\$ 28,000$
b. $R^{2}=\frac{\mathrm{SSR}}{\mathrm{SS} \text { total }}=\frac{3,050}{5,250}=.5809$
c. 9.199 , found by $\sqrt{84.62}$
d. $H_{0}$ is rejected if $F>2.97$ (approximately)

$$
\text { Computed } F=\frac{1,016.67}{84.62}=12.01
$$

$H_{0}$ is rejected. At least one regression coefficient is not zero.
e. If computed $t$ is to the left of -2.056 or to the right of 2.056, the null hypothesis in each of these cases is rejected. Computed $t$ for $X_{2}$ and $X_{3}$ exceed the critical value. Thus, "population" and "advertising expenses" should be retained and "number of competitors," $X_{1}$, dropped.
17. a. The strongest correlation is between GPA and legal. No problem with multicollinearity.
b. $R^{2}=\frac{4.3595}{5.0631}=.8610$
c. $H_{0}$ is rejected if $F>5.41$.

$$
F=\frac{1.4532}{0.1407}=10.328
$$

At least one coefficient is not zero.
d. Any $H_{0}$ is rejected if $t<-2.571$ or $t>2.571$. It appears that only GPA is significant. Verbal and math could be eliminated.
e. $R^{2}=\frac{4.2061}{5.0631}=.8307$
$R^{2}$ has only been reduced .0303.
f. The residuals appear slightly skewed (positive), but acceptable.
g. There does not seem to be a problem with the plot.
19. a. The correlation of Screen and Price is 0.893 . So there does appear to be a linear relationship between the two.
b. Price is the "dependent" variable.
c. The regression equation is Price $=-2484+101$ Screen. For each inch increase in screen size, the price increases \$101 on average.
d. Using "dummy" indicator variables for Sharp and Sony, the regression equation is Price $=-2308+94.1$ Screen + 15 Manufacturer Sharp + 381 Manufacturer Sony. Sharp can obtain on average $\$ 15$ more than Samsung and Sony can collect an additional benefit of $\$ 381$ more than Samsung.
e. Here is some of the output.

| Predictor | Coef | SE Coef | T | P |
| :--- | ---: | ---: | ---: | ---: |
| Constant | -2308.2 | 492.0 | -4.69 | 0.000 |
| Screen | 94.12 | 10.83 | 8.69 | 0.000 |
| Manufacturer_Sharp | 15.1 | 171.6 | 0.09 | 0.931 |
| Manufacturer_Sony | 381.4 | 168.8 | 2.26 | 0.036 |

The $p$-value for Sharp is relatively large. A test of their coefficient would not be rejected. That means they may not have any real advantage over Samsung. On the other hand, the $p$-value for the Sony coefficient is quite small. That indicates that it did not happen by chance and there is some real advantage to Sony over Samsung.
f. A histogram of the residuals indicates they follow a normal distribution.
g. The residual variation may be increasing for larger fitted values.
21. a.

Scatter Diagram of Sales vs. Advertising, Accounts, Competitors, Potential

$\frac{\mathscr{\infty}}{\infty}$


Sales seem to fall with the number of competitors and rise with the number of accounts and potential.
b. Pearson correlations

|  | Sales | Advertising | Accounts Competitors |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Advertising | 0.159 |  |  |  |
| Accounts | 0.783 | 0.173 |  |  |
| Competitors | -0.833 | -0.038 | -0.324 |  |
| Potential | 0.407 | -0.071 | 0.468 | -0.202 |

The number of accounts and the market potential are moderately correlated.
c. The regression equation is:

Sales $=178+1.81$ Advertising +3.32 Accounts -21.2 Competitors +0.325 Potential

| Predictor | Coef | SE Coef | T | P |
| :--- | ---: | ---: | ---: | ---: |
| Constant | 178.32 | 12.96 | 13.76 | 0.000 |
| Advertising | 1.807 | 1.081 | 1.67 | 0.109 |
| Accounts | 3.3178 | 0.1629 | 20.37 | 0.000 |
| Competitors | -21.1850 | 0.7879 | -26.89 | 0.000 |
| Potential | 0.3245 | 0.4678 | 0.69 | 0.495 |
| $\mathrm{~S}=9.60441$ | $\mathrm{R}-\mathrm{Sq}=98.9 \%$ | $\mathrm{R}-\mathrm{Sq}($ adj $)=$ | $98.7 \%$ |  |

Analysis of Variance

| Source | DF | SS | MS | F | P |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Regression | 4 | 176777 | 44194 | 479.10 | 0.000 |
| Residual Error | 21 | 1937 | 92 |  |  |
| Total | 25 | 178714 |  |  |  |

The computed $F$ value is quite large. So we can reject the null hypothesis that all of the regression coefficients are zero. We conclude that some of the independent variables are effective in explaining sales.
d. Market potential and advertising have large $p$-values ( 0.495 and 0.109 , respectively). You would probably drop them.
e. If you omit potential, the regression equation is: Sales $=180+1.68$ Advertising +3.37 Accounts -21.2 Competitors

| Predictor | Coef | SE Coef | T | P |
| :--- | ---: | ---: | ---: | ---: |
| Constant | 179.84 | 12.62 | 14.25 | 0.000 |
| Advertising | 1.677 | 1.052 | 1.59 | 0.125 |
| Accounts | 3.3694 | 0.1432 | 23.52 | 0.000 |
| Competitors | -21.2165 | 0.7773 | -27.30 | 0.000 |

Now advertising is not significant. That would also lead you to cut out the advertising variable and report that the polished regression equation is:
Sales $=187+3.41$ Accounts -21.2 Competitors

| Predictor | Coef | SE Coef | T | P |
| :--- | ---: | ---: | ---: | ---: |
| Constant | 186.69 | 12.26 | 15.23 | 0.000 |
| Accounts | 3.4081 | 0.1458 | 23.37 | 0.000 |
| Competitors | -21.1930 | 0.8028 | -26.40 | 0.000 |

f.

## Histogram of the Residuals (response is Sales)



The histogram looks to be normal. There are no problems shown in this plot.
g. The variance inflation factor for both variables is 1.1. They are less than 10. There are no troubles as this value indicates the independent variables are not strongly correlated with each other.
23. The computer output is:

| Predictor | Coef | StDeV | t-ratio | $p$ |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Constant | 651.9 | 345.3 | 1.89 | 0.071 |  |
| Service | 13.422 | 5.125 | 2.62 | 0.015 |  |
| Age | -6.710 | 6.349 | -1.06 | 0.301 |  |
| Gender | 205.65 | 90.27 | 2.28 | 0.032 |  |
| Job | -33.45 | 89.55 | -0.37 | 0.712 |  |
| Analysis | of | Variance |  |  |  |
| SOURCE | DF | SS | $M S$ | $F$ | $p$ |
| Regression | 4 | 1066830 | 266708 | 4.77 | 0.005 |
| Error | 25 | 1398651 | 55946 |  |  |
| Total | 29 | 2465481 |  |  |  |

a. $\hat{Y}=651.9+13.422 X_{1}-6.710 X_{2}+205.65 X_{3}-33.45 X_{4}$
b. $R^{2}=.433$, which is somewhat low for this type of study.
c. $H_{0}: \beta_{1}=\beta_{2}=\beta_{3}=\beta_{4}=0 ; H_{1}$ : not all $\beta$ s equal zero. Reject $H_{0}$ if $F>2.76$.

$$
F=\frac{1,066,830 / 4}{1,398,651 / 25}=4.77
$$

$H_{0}$ is rejected. Not all the $\beta_{i}$ 's equal 0 .
d. Using the .05 significance level, reject the hypothesis that the regression coefficient is 0 if $t<-2.060$ or $t>$ 2.060. Service and gender should remain in the analyses; age and job should be dropped.
e. Following is the computer output using the independent variables service and gender.

| Predictor | Coef | StDev | t-ratio | $p$ |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Constant | 784.2 | 316.8 | 2.48 | 0.020 |  |
| Service | 9.021 | 3.106 | 2.90 | 0.007 |  |
| Gender | 224.41 | 87.35 | 2.57 | 0.016 |  |
|  |  |  |  |  |  |
| Analysis | of | Variance |  |  |  |
| SOURCE | $D F$ | $S S$ | $M S$ | $F$ | $p$ |
| Regression | 2 | 998779 | 499389 | 9.19 | 0.001 |
| Error | 27 | 1466703 | 54322 |  |  |
| Total | 29 | 2465481 |  |  |  |

A man earns \$224 more per month than a woman. The difference between technical and clerical jobs is not significant.
25. a. $Y=29.913-5.324 X_{1}+1.449 X_{2}$
b. EPS is $(t=-3.26, p$-value $=.005)$. Yield is not $(t=0.81$, $p$-value $=.431$ ).
c. An increase of 1 in EPS results in a decline of 5.324 in $P / E$. When yield increases by one, P/E increases by 1.449.
d. Stock number 2 is undervalued.
e. Below is a residual plot. It does not appear to follow the normal distribution.

f. There does not seem to be a problem with the plot of the residuals versus the fitted values.

g. The correlation between yield and EPS is not a problem. No problem with multicollinearity.

|  | P/E | EPS |
| :--- | ---: | ---: |
| EPS | -0.602 |  |
| Yield | .054 | .162 |

27. a. The regression equation is

Sales (000) $=1.02+0.0829$ Infomercials

| Predictor | Coef | SE Coef | T | P |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Constant | 1.0188 | 0.3105 | 3.28 | 0.006 |  |
| Infomercials | 0.08291 | 0.01680 | 4.94 | 0.000 |  |
|  |  |  |  |  |  |
| Analysis of | Variance |  |  |  |  |
| Source | DF | SS | MS | F | P |
| Regression | 1 | 2.3214 | 2.3214 | 24.36 | 0.000 |
| Residual Error | 13 | 1.2386 | 0.0953 |  |  |
| Total | 14 | 3.5600 |  |  |  |

The global test demonstrates there is a relationship between sales and the number of infomercials.
b.


The residuals appear to follow the normal distribution.
29. The computer output is as follows:

| Predictor | Coef | SE Coef | $T$ | $P$ |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Constant | 38.71 | 39.02 | .99 | .324 |  |
| Bedrooms | 7.118 | 2.551 | 2.79 | 0.006 |  |
| Size | 0.03800 | 0.01468 | 2.59 | 0.011 |  |
| Pool | 18.321 | 6.999 | 2.62 | 0.010 |  |
| Distance | -0.9295 | 0.7279 | -1.28 | 0.205 |  |
| Garage | 35.810 | 7.638 | 4.69 | 0.000 |  |
| Baths | 23.315 | 9.025 | 2.58 | 0.011 |  |
| S $=33.21$ | R-Sq $=$ | $53.2 \%$ | R-Sq | $($ adj) | $=$ |
| S |  | $50.3 \%$ |  |  |  |
| Analysis of | Variance |  |  |  |  |
| SOURCE |  | DF | SS | MS | $F$ |
| Regression | 6 | 122676 | 20446 | 18.54 | 0.000 |
| Residual | Error | 98 | 108092 | 1103 |  |
| Total | 104 | 230768 |  |  |  |

a. Each additional bedroom adds about $\$ 7,000$ to the selling price, each additional square foot adds $\$ 38$, a pool adds $\$ 18,300$ to the value, an attached garage increases the value by $\$ 35,800$, and each mile the home is from the center of the city reduces the selling price by $\$ 929$.
b. The $R$-square value is 0.532 .
c. The correlation matrix is as follows:

|  | Price | Bedrooms | Size | Pool | Distance | Garage |
| :--- | ---: | ---: | ---: | ---: | ---: | :--- |
| Bedrooms | 0.467 |  |  |  |  |  |
| Size | 0.371 | 0.383 |  |  |  |  |
| Pool | 0.294 | 0.005 | 0.201 |  |  |  |
| Distance | -0.347 | -0.153 | -0.117 | -0.139 |  |  |
| Garage | 0.526 | 0.234 | 0.083 | 0.114 | -0.359 |  |
| Baths | 0.382 | 0.329 | 0.024 | 0.055 | -0.195 | 0.221 |

The independent variable garage has the strongest correlation with price. Distance is inversely related, as expected, and there does not seem to be a problem with correlation among the independent variables.
d. The results of the global test suggest that some of the independent variables have net regression coefficients different from zero.
e. We can delete distance.
f. The new regression output follows.

| Predictor | Coef | SE Coef | $T$ | $P$ |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Constant | 17.01 | 35.24 | .48 | .630 |  |
| Bedrooms | 7.169 | 2.559 | 2.80 | 0.006 |  |
| Size | 0.03919 | 0.01470 | -2.67 | 0.009 |  |
| Pool | 19.110 | 6.994 | 2.73 | 0.007 |  |
| Garage | 38.847 | 7.281 | 5.34 | 0.000 |  |
| Baths | 24.624 | 8.995 | 2.74 | 0.007 |  |
| S = 33.32 | R-Sq $=$ | $52.4 \%$ | R-Sq(adj) | $=$ | $50.0 \%$ |
| Analysis of | Variance |  |  |  |  |
| SOURCE |  | $D F$ | $S S$ | MS | $F$ |
| Regression | 5 | 120877 | 24175 | 21.78 | 0.000 |
| Residual | Error | 99 | 109890 | 1110 |  |
| Total | 104 | 230768 |  |  |  |

In reviewing the $p$-values for the various regression coefficients, all are less than .05. We leave all the independent variables.
g. \& h. Analysis of the residuals, not shown, indicates the normality assumption is reasonable. In addition, there is no pattern to the plots of the residuals and the fitted values of $Y$.
31. a. The regression equation is

$$
\begin{aligned}
\text { Maintenance }= & 102+5.94 \text { Age }+0.374 \text { Miles } \\
& -11.8 \text { GasolineIndicator }
\end{aligned}
$$

Each additional year of age adds $\$ 5.94$ to upkeep cost. Every extra mile adds $\$ 0.374$ to maintenance total. Gasoline buses are cheaper to maintain than diesel by $\$ 11.80$ per year.
b. The coefficient of determination is 0.286 , found by 65135/227692. Twenty-nine percent of the variation in maintenance cost is explained by these variables.
c. The correlation matrix is:

|  | Maintenance | Age | Miles |
| :--- | :---: | ---: | ---: |
| Age | 0.465 |  |  |
| Miles | 0.450 | 0.522 |  |
| GasolineIndicato | -0.118 | -0.068 | 0.025 |

Age and Miles both have moderately strong correlations with maintenance cost. The highest correlation among the independent variables is 0.522 between Age and Miles. That is smaller than 0.70 so multicollinearity may not be a problem.
d.

| Analysis of Variance |  |  |  |  |  |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: |
| Source | DF | SS | MS | F | P |
| Regression | 3 | 65135 | 21712 | 10.15 | 0.000 |
| Residual Error | 76 | 162558 | 2139 |  |  |
| Total | 79 | 227692 |  |  |  |

The $p$-value is zero. Reject the null hypothesis of all coefficients being zero and say at least one is important.
e.

| Predictor | Coef | SE Coef | T | P |
| :--- | ---: | ---: | ---: | ---: |
| Constant | 102.3 | 112.9 | 0.91 | 0.368 |
| Age | 5.939 | 2.227 | 2.67 | 0.009 |
| Miles | 0.3740 | 0.1450 | 2.58 | 0.012 |
| GasolineIndicator | -11.80 | 10.99 | -1.07 | 0.286 |

The $p$-value of the gasoline indicator is bigger than 0.10. Consider deleting it.
f. The condensed regression equation is

$$
\text { Maintenance }=106+6.17 \text { Age }+0.363 \text { Miles }
$$

g.


The normality conjecture appears realistic.
h.


This plot appears to be random and to have a constant variance.

## CHAPTER 15

1. a. 3
b. 7.815
2. a. Reject $H_{0}$ if $\chi^{2}>5.991$
b. $\chi^{2}=\frac{(10-20)^{2}}{20}+\frac{(20-20)^{2}}{20}+\frac{(30-20)^{2}}{20}=10.0$
c. Reject $H_{0}$. The proportions are not equal.
3. $H_{0}$ : The outcomes are the same; $H_{1}$ : The outcomes are not the same. Reject $H_{0}$ if $\chi^{2}>9.236$.

$$
x^{2}=\frac{(3-5)^{2}}{5}+\cdots+\frac{(7-5)^{2}}{5}=7.60
$$

Do not reject $H_{0}$. Cannot reject $H_{0}$ since outcomes are the same.
7. $H_{0}$ : There is no difference in the proportions. $H_{1}$ : There is a difference in the proportions. Reject $H_{0}$ if $\chi^{2}>15.086$.

$$
\chi^{2}=\frac{(47-40)^{2}}{40}+\cdots+\frac{(34-40)^{2}}{40}=3.400
$$

Do not reject $H_{0}$. There is no difference in the proportions.
9. a. Reject $H_{0}$ if $\chi^{2}>9.210$.
b. $\chi^{2}=\frac{(30-24)^{2}}{24}+\frac{(20-24)^{2}}{24}+\frac{(10-12)^{2}}{12}=2.50$
c. Do not reject $H_{0}$.
11. $H_{0}$ : Proportions are as stated; $H_{1}$ : Proportions are not as stated. Reject $H_{0}$ if $\chi^{2}>11.345$.

$$
x^{2}=\frac{(50-25)^{2}}{25}+\cdots+\frac{(160-275)^{2}}{275}=115.22
$$

Reject $H_{0}$. The proportions are not as stated.
13. $H_{0}$ : The population of clients follows a normal distribution. $H_{1}$ : The population of clients does not follow a normal distribution.
Reject the null if chi-square is greater than 5.991.

| Number of <br> Clients | z-values | Area | Found by | $\boldsymbol{f}_{\boldsymbol{e}}$ |
| :--- | :---: | :---: | :---: | :---: |
| Under 30 | Under -1.58 | 0.0571 | $0.5000-0.4429$ | 2.855 |
| 30 up to 40 | -1.58 up to -0.51 | 0.2479 | $0.4429-0.1950$ | 12.395 |
| 40 up to 50 | -0.51 up to 0.55 | 0.4038 | $0.1950+0.2088$ | 20.19 |
| 50 up to 60 | 0.55 up to 1.62 | 0.2386 | $0.4474-0.2088$ | 11.93 |
| 60 or more | 1.62 or more | 0.0526 | $0.5000-0.4474$ | 2.63 |

The first and last class both have expected frequencies smaller than 5 . They are combined with adjacent classes.

| Number <br> of Clients | Area | $\boldsymbol{f}_{\boldsymbol{e}}$ | $\boldsymbol{f}_{\boldsymbol{o}}$ | $\boldsymbol{f}_{\boldsymbol{e}}-\boldsymbol{f}_{\boldsymbol{o}}$ | $\left(\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}\right)^{\mathbf{2}}$ | $\left[\left(\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}\right)^{\mathbf{2}}\right] / \boldsymbol{f}_{\boldsymbol{e}}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Under 40 | 0.3050 | 15.25 | 16 | -0.75 | 0.5625 | 0.0369 |
| 40 up to 50 | 0.4038 | 20.19 | 22 | -1.81 | 3.2761 | 0.1623 |
| 50 or more | $\mathbf{0 . 2 9 1 2}$ | $\frac{14.56}{1.0000}$ | $\frac{12}{50.00}$ | $\frac{2.56}{50}$ | 6.5536 | $\underline{0.4501}$ |
| $\quad$ Total | $\mathbf{1 . 0 0}$ |  | 0.6493 |  |  |  |

Since 0.6493 is not greater than 5.991 , we fail to reject the null hypothesis. These data could be from a normal distribution.
15. The $p$-value of 0.746 is greater than 0.05 and the plotted values are close to the line. Thus it is reasonable to say the readings are normally distributed.
17. $H_{0}$ : There is no relationship between community size and section read. $H_{1}$ : There is a relationship. Reject $H_{0}$ if $\chi^{2}>9.488$.

$$
\chi^{2}=\frac{(170-157.50)^{2}}{157.50}+\cdots+\frac{(88-83.62)^{2}}{83.62}=7.340
$$

Do not reject $H_{0}$. There is no relationship between community size and section read.
19. $H_{0}$ : No relationship between error rates and item type. $H_{1}$ : There is a relationship between error rates and item type. Reject $H_{0}$ if $\chi^{2}>9.21$.

$$
\chi^{2}=\frac{(20-14.1)^{2}}{14.1}+\cdots+\frac{(225-225.25)^{2}}{225.25}=8.033
$$

Do not reject $H_{0}$. There is not a relationship between error rates and item type.
21. $H_{0}: \pi_{s}=0.50, \pi_{r}=\pi_{e}=0.25$
$H_{1}$ : Distribution is not as given above.
$d f=2$. Reject $H_{0}$ if $\chi^{2}>4.605$.

| Turn | $\boldsymbol{f}_{\boldsymbol{o}}$ | $\boldsymbol{f}_{\boldsymbol{e}}$ | $\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}$ | $\left(\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}\right)^{2} / \boldsymbol{f}_{\boldsymbol{e}}$ |
| :--- | ---: | ---: | :---: | :---: |
| Straight | 112 | 100 | 12 | 1.44 |
| Right | 48 | 50 | -2 | 0.08 |
| Left | $\underline{40}$ | $\underline{50}$ | -10 | $\underline{2.00}$ |
| $\quad$ Total | 200 | 200 |  | 3.52 |

$H_{0}$ is not rejected. The proportions are as given in the null hypothesis.
23. $H_{0}$ : There is no preference with respect to TV stations.
$H_{1}$ : There is a preference with respect to TV stations.
$d f=3-1=2 . H_{0}$ is rejected if $\chi^{2}>5.991$.

| TV Station | $\boldsymbol{f}_{\boldsymbol{o}}$ | $\boldsymbol{f}_{\boldsymbol{e}}$ | $\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}$ | $\left(\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}\right)^{\mathbf{2}}$ | $\left(\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}\right)^{\mathbf{2}} / \boldsymbol{f}_{\boldsymbol{e}}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| WNAE | 53 | 50 | 3 | 9 | 0.18 |
| WRRN | 64 | 50 | 14 | 196 | 3.92 |
| WSPD | $\frac{33}{150}$ | $\frac{50}{150}$ | $\frac{-17}{0}$ | 289 | $\underline{5.78}$ |
|  | 15.88 |  |  |  |  |

$H_{0}$ is rejected. There is a preference for TV stations.
25. $H_{0}: \pi_{n}=0.21, \pi_{m}=0.24, \pi_{s}=0.35, \pi_{w}=0.20$ $H_{1}$ : The distribution is not as given.
Reject $H_{0}$ if $\chi^{2}>11.345$.

| Region | $\boldsymbol{f}_{\boldsymbol{o}}$ | $\boldsymbol{f}_{\boldsymbol{e}}$ | $\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}$ | $\left(\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}\right)^{\mathbf{2}} / \boldsymbol{f}_{\boldsymbol{e}}$ |
| :--- | ---: | ---: | ---: | :---: |
| Northeast | 68 | 84 | -16 | 3.0476 |
| Midwest | 104 | 96 | 8 | 0.6667 |
| South | 155 | 140 | 15 | 1.6071 |
| West | $\underline{73}$ | $\underline{80}$ | $\underline{-7}$ | $\underline{0.6125}$ |
| Total | $\overline{400}$ | $\mathbf{4 0 0}$ | 0 | 5.9339 |

$H_{0}$ is not rejected. The distribution of order destinations reflects the population.
27. $H_{0}$ : The proportions are the same.
$H_{1}$ : The proportions are not the same.
Reject $H_{0}$ if $\chi^{2}>16.919$.

| $\boldsymbol{f}_{\boldsymbol{o}}$ | $\boldsymbol{f}_{\boldsymbol{e}}$ | $\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}$ | $\left(\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}}\right)^{\mathbf{2}}$ | $\left(\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{e}\right)^{\mathbf{2}} / \boldsymbol{f}_{\boldsymbol{e}}$ |
| :---: | ---: | ---: | :---: | :---: |
| 44 | 28 | 16 | 256 | 9.143 |
| 32 | 28 | 4 | 16 | 0.571 |
| 23 | 28 | -5 | 25 | 0.893 |
| 27 | 28 | -1 | 1 | 0.036 |
| 23 | 28 | -5 | 25 | 0.893 |
| 24 | 28 | -4 | 16 | 0.571 |
| 31 | 28 | 3 | 9 | 0.321 |
| 27 | 28 | -1 | 1 | 0.036 |
| 28 | 28 | 0 | 0 | 0.000 |
| 21 | 28 | -7 | 49 | $\underline{1.750}$ |
|  |  |  |  | 14.214 |

Do not reject $H_{0}$. The digits are evenly distributed.
29. $H_{0}$ : The population of wages follows a normal distribution. $H_{1}$ : The population of hourly wages does not follow a normal distribution.
Reject the null if chi-square is greater than 7.779.

| Wage | $z$-values | Area | Found by | $f_{e}$ | $f_{0}$ | $f_{e}-f_{o}$ | $\left(f_{o}-f_{e}\right)^{2}$ | $\left[\left(f_{o}-f_{e}\right)^{2}\right] / f_{e}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Under \$6.50 | Under -1.72 | 0.0427 | $\begin{aligned} & 0.5000- \\ & 0.4573 \end{aligned}$ | 11.529 | 20 | -8.471 | 71.7578 | 6.2241 |
| $\begin{aligned} & 6.50 \text { up } \\ & \text { to } 7.50 \end{aligned}$ | $\begin{aligned} & -1.72 \text { up } \\ & \text { to }-0.72 \end{aligned}$ | 0.1931 | $\begin{aligned} & 0.4573- \\ & 0.2642 \end{aligned}$ | 52.137 | 24 | 28.137 | 791.6908 | 15.1848 |
| $\begin{aligned} & 7.50 \text { up } \\ & \text { to } 8.50 \end{aligned}$ | $\begin{aligned} & -0.72 \text { up } \\ & \text { to } 0.28 \end{aligned}$ | 0.3745 | $\begin{aligned} & 0.2642+ \\ & 0.1103 \end{aligned}$ | 101.115 | 130 | -28.885 | 834.3432 | 8.2514 |
| $\begin{aligned} & 8.50 \text { up } \\ & \text { to } 9.50 \end{aligned}$ | $\begin{aligned} & 0.28 \text { up } \\ & \text { to } 1.27 \end{aligned}$ | 0.2877 | $\begin{aligned} & 0.3980- \\ & 0.1103 \end{aligned}$ | 77.679 | 68 | 9.679 | 93.6830 | 1.2060 |
| 9.50 or more | $1.27 \text { or }$ <br> more | 0.1020 | $\begin{aligned} & 0.5000- \\ & 0.3980 \end{aligned}$ | 27.54 | 28 | $-0.46$ | 0.2116 | 0.0077 |
| Total |  | 1.0000 |  | 270 | 270 | 0 |  | 30.874 |

Since 30.874 is greater than 7.779 , we reject the null hypothesis; wages do not follow a normal distribution.
31.


The $p$-value ( 0.097 ) is greater than 0.05 . Do not reject the null hypothesis. The data could be normally distributed.
33. $H_{0}$ : Gender and attitude toward the deficit are not related. $H_{1}$ : Gender and attitude toward the deficit are related.
Reject $H_{0}$ if $\chi^{2}>5.991$.

$$
\begin{aligned}
\chi^{2}= & \frac{(244-292.41)^{2}}{292.41}+\frac{(194-164.05)^{2}}{164.05} \\
& +\frac{(68-49.53)^{2}}{49.53}+\frac{(305-256.59)^{2}}{256.59} \\
& +\frac{(114-143.95)^{2}}{143.95}+\frac{(25-43.47)^{2}}{43.47}=43.578
\end{aligned}
$$

Since $43.578>5.991$, you reject $H_{0}$. A person's position on the deficit is influenced by his or her gender.
35. $H_{0}$ : Whether a claim is filed and age are not related. $H_{1}$ : Whether a claim is filed and age are related. Reject $H_{0}$ if $\chi^{2}>7.815$.

$$
\chi^{2}=\frac{(170-203.33)^{2}}{203.33}+\cdots+\frac{(24-35.67)^{2}}{35.67}=53.639
$$

Reject $H_{0}$. Age is related to whether a claim is filed.
37. $H_{0}: \pi_{B L}=\pi_{O}=.23, \pi_{Y}=\pi_{G}=.15, \pi_{B R}=\pi_{R}=.12 . H_{1}$ : The proportions are not as given. Reject $H_{0}$ if $\chi^{2}>15.086$.

| Color | $\boldsymbol{f}_{\boldsymbol{o}}$ | $\boldsymbol{f}_{\boldsymbol{e}}$ | $\left(\boldsymbol{f}_{\boldsymbol{o}}-\boldsymbol{f}_{\boldsymbol{e}} \mathbf{)}^{\mathbf{2}} / \boldsymbol{f}_{\boldsymbol{e}}\right.$ |
| :--- | ---: | ---: | :---: |
| Blue | 12 | 16.56 | 1.256 |
| Brown | 14 | 8.64 | 3.325 |
| Yellow | 13 | 10.80 | 0.448 |
| Red | 14 | 8.64 | 3.325 |
| Orange | 7 | 16.56 | 5.519 |
| Green | $\mathbf{1 2}$ | 10.80 | $\underline{0.133}$ |
| Total | $\mathbf{7 2}$ |  | $\mathbf{1 4 . 0 0 6}$ |

Do not reject $H_{0}$. The color distribution agrees with the manufacturer's information.
39. a. $H_{0}$ : Payroll and winning are not related.
$H_{1}$ : Payroll and winning are related.
Reject $H_{0}$ if $\chi^{2}>3.84$.

|  | Payroll |  |  |
| :--- | :---: | :---: | :---: |
| Winning | Lower Half | Top Half | Total |
| No | 8 | 6 | 14 |
| Yes | $\frac{7}{15}$ | $\frac{9}{15}$ | 16 |
| Total |  |  |  |

$\chi^{2}=\frac{(8-7)^{2}}{7}+\frac{(6-7)^{2}}{7}+\frac{(7-8)^{2}}{8}+\frac{(9-8)^{2}}{8}=0.5357$
Do not reject $H_{0}$. Conclude that payroll and winning may not be related.
b.


The attendance $p$-value is 0.243 , which is greater than 0.05 . Do not reject the null hypothesis. Attendance could be normally distributed. The payroll $p$-value is 0.064 , which is greater than 0.05 . Do not reject the null hypothesis. Payroll could be normally distributed.

## PRACTICE TEST—CHAPTER 1

## Part I

1. Statistics
2. Descriptive statistics
3. Statistical inference
4. Sample
5. Population
6. Nominal
7. Ratio
8. Ordinal
9. Interval
10. Discrete
11. Nominal
12. Nominal

Part II

1. a. 11.1
b. About 3 to 1
c. 65
2. a. Ordinal
b. $67.7 \%$

## PRACTICE TEST—CHAPTER 2

Part I

1. Frequency table
2. Frequency distribution
3. Bar chart
4. Pie chart
5. Histogram or frequency polygon
6. 7
7. Class interval
8. Midpoint
9. Total number of observations
10. Upper class limits

Part II

1. a. $\$ 30$
b. 105
c. 52
d. . 19
e. $\$ 165$
f. $\$ 120, \$ 330$
g.

Selling Price of Homes in Warren, PA


Selling Price of Homes in Warren, PA


PRACTICE TEST—CHAPTER 3
Part I

1. Parameter
2. Statistic
3. Zero
4. Median
5. $50 \%$
6. Mode
7. Range
8. Variance
9. Variance
10. Never
11. Median
12. Normal rule or empirical rule

Part II

1. a. $\bar{X}=\frac{560}{8}=70$
b. Median $=71.5$
c. Range $=80-52=28$
d. $s=\sqrt{\frac{610.0}{8-1}}=9.335$
2. $\bar{X}_{w}=\frac{200(\$ 36)+300(\$ 40)+500(\$ 50)}{200+300+500}=\$ 44.20$
3. $-0.88 \pm 2(1.41)$
$-0.88 \pm 2.82$
-3.70, 1.94

## PRACTICE TEST—CHAPTER 4

Part I

1. Dot plot
2. Box plot
3. Scatter diagram
4. Contingency table
5. Quartile
6. Percentile
7. Skewness
8. First quartile
9. Inter quartile range

Part II

1. a.

| DotPlot |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - ・ヵ - |  |  | - •••• |  |  |  |
| 0 | 20 | 40 | 60 | 80 | 100 | 120 |
|  | \$ Million |  |  |  |  |  |

b. $L_{50}=(11+1) \frac{50}{100}=6$
median $=35$
c. $L_{25}=(11+1) \frac{25}{100}=3$
$Q_{1}=23$
d. $L_{75}=(11+1) \frac{75}{100}=9$

$$
Q_{3}=91
$$


2. a. $P(H)=\frac{144}{449}=0.32$
b. $P(H \mid<30)=\frac{21}{89}=0.24$
c. $P(H \mid>60)=\frac{75}{203}=0.37$. Age is related to high blood pressure, because $P(H \mid>60)$ is greater than $P(H \mid<30)$.

## PRACTICE TEST—CHAPTER 5

Part I

1. Probability
2. Experiment
3. Event
4. Relative frequency
5. Subjective
6. Classical
7. Mutually exclusive
8. Exhaustive
9. Mutually exclusive
10. Complement rule
11. Joint probability
12. Independent

Part II

1. a. $P($ Both $)=P\left(B_{1}\right) \cdot P\left(B_{2} \mid B_{1}\right)$

$$
=\left(\frac{5}{20}\right)\left(\frac{4}{19}\right)=.0526
$$

b. $P$ (at least 1 ) $=1-P$ (neither)

$$
=1-\left(\frac{15}{20}\right)\left(\frac{14}{19}\right)=1-.5526=.4474
$$

2. $P($ At least 1$)=P$ (Jogs) $+P$ (Bike) $-P$ (Both)

$$
=.30+.20-12=.38
$$

3. $X=5!=120$

## PRACTICE TEST—CHAPTER 6

## Part I

1. Probability distribution
2. Probability
3. One
4. Mean
5. Two
6. Never
7. Equal
8. $\pi$
9. .075
10. . 183

## Part II

1. a. Binomial
b. $P(x=1)={ }_{16} C_{1}(.15)^{1}(.85)^{15}=(16)(.15)(.0874)=.210$
c. $P(x \geq 1)=1-P(x=0)=1-{ }_{16} C_{0}(.15)^{0}(.85)^{16}=.9257$
2. a. Poisson
b. $P(x=3)=\frac{3^{3} e^{-3}}{3!}=\frac{27}{(6)(20.0855)}=.224$
c. $P(x=0)=\frac{3^{0} e^{-3}}{0!}=.050$
d. $P(x \geq 1)=1-P(x=0)=1-.050=.950$
3. 

| Exemptions <br> $\mathbf{x}$ | Probability <br> $\boldsymbol{P}(\boldsymbol{x})$ | $\boldsymbol{x} \cdot \boldsymbol{P}(\boldsymbol{x})$ | $(\boldsymbol{x}-\mathbf{2 . 2})^{\mathbf{2}} \cdot \boldsymbol{P}(\boldsymbol{x})$ |
| :---: | :---: | :---: | :---: |
| 1 | 0.2 | 0.2 | 0.288 |
| 2 | 0.5 | 1 | 0.02 |
| 3 | 0.2 | 0.6 | 0.128 |
| 4 | 0.1 | 0.4 | $\underline{0.324}$ |
|  |  | 2.2 | $\mathbf{0 . 7 6}$ |

a. $\mu=1(.2)+2(.5)+3(.2)+4(.1)=2.2$
b. $\quad \sigma^{2}=(1-2.2)^{2}(.2)+\cdots+(4-2.2)^{2}(.1)=0.76$

## PRACTICE TEST—CHAPTER 7

Part I

1. One
2. Infinite
3. Discrete
4. Always equal
5. Infinite
6. One
7. Any of these values
8. . 2764
9. . 9396
10. . 0450

## Part II

$$
\begin{aligned}
& \text { 1. } \text { a. } \\
& z=\frac{2000-1600}{850}=.47 \\
& P(0 \leq z<.47)=.1808 \\
& \text { b. } \\
& z=\frac{900-1600}{850}=-0.82 \\
& P(-0.82 \leq z \leq .47)=.2939+.1808=.4747 \\
& \text { c. } z=\frac{1800-1600}{850}=0.24 \\
& P(0.24 \leq z \leq .47)=.1808-.0948=-.0860
\end{aligned}
$$

d. $1.65=\frac{X-1600}{850}$
$X=1600+1.65(850)=\$ 3002.50$

## PRACTICE TEST—CHAPTER 8

## Part I

1. Random sample
2. No size restriction
3. Strata
4. Sampling error
5. Sampling distribution of sample means
6. 120
7. Standard error of the mean
8. Always equal
9. Decrease
10. Normal distribution

## Part II

$$
\begin{aligned}
& \text { 1. } z=\frac{11-12.2}{2.3 / \sqrt{12}}=-1.81 \\
& P(z<-1.81)=.5000-.4649=.0351
\end{aligned}
$$

## PRACTICE TEST—CHAPTER 9

Part I

1. Point estimate
2. Confidence interval
3. Narrower
4. Proportion
5. 95
6. Standard deviation
7. Binomial
8. $z$ distribution
9. Population median
10. Population mean

Part II

1. a. Unknown
b. 9.3 years
c. $s_{\bar{x}}=\frac{2.0}{\sqrt{26}}=0.392$
d. $9.3 \pm(1.708) \frac{2.0}{\sqrt{26}}$
$9.3 \pm 0.67$
(8.63, 9.97)
2. $n=(.27)(.73)\left(\frac{2.326}{.02}\right)^{2}=2.666$
3. $.64 \pm 1.96 \sqrt{\frac{.64(.36)}{100}}$
$.64 \pm .094$
[.546, .734]

## PRACTICE TEST—CHAPTER 10

Part I

1. Null hypothesis
2. Accept
3. Significant level
4. Test statistic
5. Critical value
6. Two
7. Standard deviation (or variance)
8. $p$-value
9. Binomial
10. Five

Part II

1. $H_{0}: \mu \leq 90, H_{1}: \mu>90$
$d f=18-1=17$
Reject $H_{0}$ if $t>2.567$
$t=\frac{96-90}{12 / \sqrt{18}}=2.121$

Do not reject $H_{0}$. We cannot conclude that the mean time in the park is more than 90 minutes.
2. $H_{0}: \mu \leq 9.75 \quad H_{1}: \mu>9.75$

Reject $H_{0}$ if $z>1.645$
note $\sigma$ is known, so $z$ is used and we assume a . 05 significance level.
$z=\frac{9.85-9.75}{0.27 / \sqrt{25}}=1.852$
Reject $H_{0}$. The mean weight is more than 9.75 ounces.
3. $H_{0}: \pi \geq 0.67, H_{1}: \pi<0.67$

Reject $H_{0}$ if $z<-1.645$.

$$
z=\frac{\frac{180}{300}-0.67}{\sqrt{\frac{0.67(1-0.67)}{300}}}=-2.578
$$

Reject $H_{0}$. Less than .67 of the couples seek their mate's approval.

## PRACTICE TEST—CHAPTER 11

Part I

1. Zero
2. $z$
3. Proportions
4. Population standard deviation
5. Difference
6. $t$ distribution
7. $n-2$
8. Paired
9. Independent
10. Dependent sample

Part II

1. $H_{0}: \mu_{y}=\mu_{h} ; H_{1}: \mu_{y} \neq \mu_{h}$
$d f=14+12-2=24$
Reject $H_{0}$ if $t<-2.064$ or $t>2.064$

$$
\begin{aligned}
s_{p}^{2} & =\frac{(14-1) 30^{2}+(12-1)(40)^{2}}{14+12-2}=1220.83 \\
t & =\frac{837-797}{\sqrt{1220.83\left(\frac{1}{14}+\frac{1}{12}\right)}}=\frac{40.0}{13.7455}=2.910
\end{aligned}
$$

Reject $H_{0}$. There is a difference in the mean miles traveled.
2. $H_{0}: \pi_{E}=\pi_{T} \quad H_{1}: \pi_{E} \neq \pi_{T}$

Reject $H_{0}$ if $z<-1.96$ or $z>1.96$

$$
P_{C}=\frac{128+149}{300+400}=\frac{277}{700}=.396
$$

$$
z=\frac{\frac{128}{300}-\frac{149}{400}}{\sqrt{\frac{.396(1-.396)}{300}+\frac{.396(1-.396)}{400}}}=\frac{.054}{.037}=1.459
$$

Do not reject $H_{0}$. There is no difference on the proportion that liked the soap in the two cities.

## PRACTICE TEST—CHAPTER 12

Part I

1. F distribution
2. Positively skewed
3. Variances
4. Means
5. Population standard deviations
6. Error or Residual
7. Equal
8. Degrees of freedom
9. Variances
10. Independent

Part II

1. $H_{0}: \sigma_{h}^{2}=\sigma_{y}^{2} ; H_{1}: \sigma_{h}^{2} \neq \sigma_{y}^{2}$
$d f_{y}=12-1=11 \quad d f_{h}=14-1=13$
Reject $H_{0}$ if $F>2.635$.
$F=\frac{(40)^{2}}{(30)^{2}}=1.78$
Do not reject $H_{0}$. Cannot conclude there is a difference in the variation of the miles traveled.
2. a. 3
b. 21
c. 3.55
d. $H_{0}: \mu_{1}=\mu_{2}=\mu_{3}$ $H_{1}$ : not all treatment means are the same
e. Reject $H_{0}$
f. The treatment means are not the same.

## PRACTICE TEST—CHAPTER 13

Part I

1. Scatter diagram
2. -1 and 1
3. Less than zero
4. Coefficient of determination
5. $t$
6. Predicted or fitted
7. Sign
8. Larger
9. Error
10. Independent

Part II

1. a. 25
b. Shares of stock
c. $\hat{Y}=197.9229+24.9145 X$
d. Direct
e. $r=\sqrt{\frac{152,399.0211}{208,333.1400}}=0.855$
f. $\hat{Y}=197.9229+24.9145(10)=447.0679$, or 447
g. Increase almost 25
h. $H_{0}: \beta \leq 0$
$H_{1}: \beta>0$
Reject $H_{0}$ if $t>1.71$
$t=\frac{24.9145}{3.1473}=7.916$
Reject $H_{0}$. There is a positive relationship between years and shares.

## PRACTICE TEST—CHAPTER 14

Part I

1. Independent variables
2. Least squares
3. Mean square error
4. Independent variables
5. Independent variable
6. Different from zero
7. $F$ distribution
8. $t$ distribution
9. Linearity
10. Correlated
11. Multicollinearity
12. Dummy variable

Part II

1. a. Four
b. $Y=70.06+0.42 x_{1}+0.27 x_{2}+0.75 x_{3}+0.42 x_{4}$
c. $R^{2}=\frac{1050.8}{1134.6}=0.926$
d. $s_{y .1234}=\sqrt{4.19}=2.05$
e. $H_{0}: \beta_{1}=\beta_{2}=\beta_{3}=\beta_{4}=0$
$H_{1}$ : not all $\beta_{i}=0$
Reject $H_{0}$ if $F>2.87$.
$F=\frac{262.70}{4.19}=62.70$
Reject $H_{0}$. Not all the regression coefficients equal zero.
d. $H_{0}: \beta_{i}=0, H_{1}: \beta_{i} \neq 0$

Reject $H_{0}$ if $t<-2.086$ or $t>2.086$.

| $\beta_{1}=0$ | $\beta_{2}=0$ | $\beta_{3}=0$ | $\beta_{4}=0$ |
| :--- | :--- | :--- | :--- |
| $\beta_{1} \neq 0$ | $\beta_{2} \neq 0$ | $\beta_{3} \neq 0$ | $\beta_{4} \neq 0$ |
| $t=2.47$ | $t=1.29$ | $t=2.50$ | $t=6.00$ |
| Reject $H_{0}$ | Do not reject $H_{0}$ | Reject $H_{0}$ | Reject $H_{0}$ |

Conclusion. Drop variable 2 and retain the others.

## PRACTICE TEST—CHAPTER 15

Part I

1. Nominal
2. No assumption
3. Can have negative values
4. 2
5. 6
6. Independent
7. 4
8. The same
9. 9.488
10. Degrees of freedom

## Part II

1. $H_{0}$ : There is no difference between the school district and census data.
$H_{1}$ : There is a difference between the school district and census data.
Reject $H_{0}$ if $\chi^{2}>7.815$.
$x^{2}=\frac{(120-130)^{2}}{130}+\frac{(40-40)^{2}}{40}+\frac{(30-20)^{2}}{20}+\frac{(10-10)^{2}}{10}=5.77$
Do not reject $H_{0}$. There is no difference between the census and school district data.
2. $H_{0}$ : Gender and book type are independent.
$H_{1}$ : Gender and book type are related.
Reject $H_{0}$ if $\chi^{2}>5.991$.
$\chi^{2}=\frac{(250-197.31)^{2}}{197.31}+\cdots+\frac{(200-187.5)^{2}}{187.5}=54.842$
Reject $H_{0}$. Men and women read different types of books.
