## GLENCOE MATHEMATICS

## ALGEBRA

# Prerequisite Skills Workbook: Remediation and Intervention 

For use with<br>Glencoe Pre-Algebra<br>Glencoe Algebra 1<br>Glencoe Algebra: Concepts and Applications



New York, New York<br>Columbus, Ohio<br>Chicago, Illinois<br>Peoria, Illinois<br>Woodland Hills, California

## Glencoe/McGraw-Hill

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## Comparing and Ordering Whole Numbers

You can use a number line to compare whole numbers such as 1353 and 1250.


On a number line, values increase as you move to the right.
1250 is to the left of 1353 . 1353 is to the right of 1250 .

1250 is less than 1353.

$$
1250<1353
$$

1353 is greater than 1250 .

$$
1353>1250
$$

You can compare numbers without a number line. Start at the left and compare the digits in each place-value position.


In the hundreds place, $2<3$.
So, $1250<1353$.

## Examples

Replace each $\square$ with $<,>$, or $=$ to make a true sentence.
$15749 \bigcirc 5746$
In the ones place, $9>6$.

So, $5749>5746$.
$2 \quad 1432 \bigcirc 989$
On a number line, 1432 is to the right of 989 .

So, $1432>989$.

## 3 Order 34, 22, 39, and 105 from least to greatest.

Compare the hundreds. 105 is the greatest.
Compare the tens. 22 is the least.
Compare the ones. 34 is less than 39.
So the order from least to greatest is $22,34,39,105$

Write using the symbols $<,>$, or $=$.

1. 9 is greater than 7 .
2. 480 is greater than 48 .
3. 832 is equal to 832 .
4. 38 is less than 83 .
5. 500 is greater than 498 .
6. 365 is less than 375 .
$\qquad$

## Comparing and Ordering Whole Numbers (continued)

Fill in the blank with $<,>$, or $=$ to make a true sentence.
7. 435 $\qquad$ 534
8. 6739 $\qquad$ 6738
9. 8762 $\qquad$ 8672
10. 892 $\qquad$ 2531
11. 7059 $\qquad$ 7061
12. 629,356 $\qquad$ 630,200
13. 487,926 $\qquad$ 487,826
14. 74,923 $\qquad$ 74,923
15. 15,538 $\qquad$ 15,358
16. 124,462 $\qquad$ 124,433
17. $49,675 \quad 49,675$
18. 753,021 $\qquad$ 743,012
19. 64,336 $\qquad$ 65,376
20. 819,461 $\qquad$ 803,642

## Order the numbers from least to greatest.

21. 48
52
46
67
22. $987978990 \quad 897$
23. 99
989809
24. 865
635402
615
25. $602 \quad 206 \quad 620 \quad 260$
26. $2063 \quad 2060 \quad 2058$
27. $4007 \quad 4700 \quad 4070$
28. 214324132341
29. $6300 \quad 60036030$
30. $102 \quad 120 \quad 112 \quad 201$

## Solve. Use the chart.

31. List the states in order of size from least to greatest.
32. Which state has an area between 57,000 and 60,000 square miles?

## Rounding Whole Numbers

The distance from Atlanta, Georgia, to Memphis, Tennessee, is 371 miles. If you tell a friend that the distance is about 400 miles, you have rounded the number.

On a number line, you can see that 371 is between 300 and 400. It is closer to 400 . To the nearest hundred, 371 rounds to 400 .


You can also round numbers without using a number line. First, look at the digit to the right of the place being rounded.

- If the digit to the right is $5,6,7,8$, or 9 , round up.
- If the digit to the right is $0,1,2,3$, or 4 , the underlined digit remains the same.


## Examples

1 Round 84,373 to the nearest thousand.


To the nearest thousand, 84,373 rounds to 84,000 .
2 Round 3,546,238 to the nearest million.

$$
\text { millions } \stackrel{3,}{\boxed{3}, 546,238} \text { Round up since the digit is } 5 \text {. }
$$

To the nearest million, $3,546,238$ rounds to $4,000,000$.
Round to the nearest ten. Use the number line if necessary.


1. 682
2. 675
3. 698
4. 661

Round to the nearest hundred. Use the number line if necessary.

5. 830
6. 850
7. 778
8. 879
9. 950
10. 1022
$\qquad$
$\qquad$

## Rounding <br> Whole Numbers (continued)

Round to the nearest thousand. Use the number line if necessary.

11. 3100
12. 2500
13. 2262
14. 4700
15. 5860
16. 4082
17. 3643
18. 4216
19. 5910

Round to the underlined place-value position.
20. 267
22. 420,800
24. 43,728
26. 14,350
28. $3,398,000$
30. 532,795
32. $6,321,510$
34. $127,610,573$

Solve. Use the chart.
36. List the oceans in order of size from least area to greatest area.
37. Round each area to the nearest million.
21. $40 \underline{9} 1$
23. $5 \underline{6} 7,000$
25. 301,792
27. $\underline{9}, 798$
29. $1 \underline{8}, 499,898$
31. $\underline{8} 24,619$
33. $24,053,217$
35. $34 \underline{6}, 872,000$

| Areas of Oceans |  |
| :---: | :---: |
| Ocean | Area <br> (square kilometers) |
| Arctic | $9,485,000$ |
| Atlantic | $86,557,000$ |
| Indian | $73,427,000$ |
| Pacific | $166,241,000$ |

$\qquad$

## Adding Whole Numbers

To add whole numbers, first add the ones. Then add the digits in each place from right to left.

## Examples



## Add.

1. 72
+65

+ 

2. 62
+83

+ 

3. 39
$\begin{array}{r}+37 \\ \hline\end{array}$
4. 66
+85

+ 

5. 768
$\begin{array}{r}+\quad 67 \\ \hline\end{array}$
6. 495

| $+\quad 48$ |
| :--- |

7. $\$ 470$
$\begin{array}{r} \\ +\quad 583 \\ \hline\end{array}$
8. 237
$\begin{array}{r}+\quad 579 \\ \hline\end{array}$
9. 1570

| +2823 |
| :--- |

10. 5126
+2899
11. 3973

| $+\quad 1689$ |
| :--- |

12. 1482
$\begin{array}{r}+3497 \\ \hline\end{array}$

## Adding Whole Numbers (continued)

13. $\begin{array}{r}4632 \\ +\quad 705\end{array}$
14. 14,832
$\begin{array}{r}1429 \\ +\quad 62 \\ \hline\end{array}$
15. 23,467
$\begin{array}{r}7324 \\ +\quad \\ \hline\end{array}$
16. 36
17. 65

89
$\begin{array}{r}+\quad 23 \\ \hline\end{array}$
$\begin{array}{r} \\ +\quad 21 \\ \hline\end{array}$
14. 2039
$\begin{array}{r}+\quad 758 \\ \hline\end{array}$
15. 6720
6385
$+\quad$
16. 7916

| +8295 |
| :--- |

19. 15,732
20. 24,816
$\begin{array}{r}15615 \\ +\quad 8 \\ \hline\end{array}$
$\begin{array}{r}+\quad 15,995 \\ \hline\end{array}$
21. 168
275
$\begin{array}{r}+\quad 256 \\ \hline\end{array}$
22. 245
87
$\begin{array}{r}+316 \\ \hline\end{array}$
23. 43
24. 439
64
$\begin{array}{r}+\quad 87 \\ \hline\end{array}$
25. 518
26. 425

192

| $+\quad 36$ |
| :--- |

376
124
$+\quad 1$
30. $463+309+1542=$
32. $636+4923+481=$
34. One day, 148 copies of the student newspaper were sold. On the previous day, 164 copies were sold. How many copies were sold during these two days?

## Subtracting Whole Numbers

To subtract whole numbers, first subtract the ones. Then subtract the digits in each place from right to left. Rename as needed.

## Examples

| $\mathbf{8 9 6}$ |
| ---: | :--- |
| -145 |
| 1 |$\longrightarrow$| 896 |
| ---: |
| -145 |
| 51 |$\quad \longrightarrow$| 896 |
| ---: |
| -145 |
| 751 |

Subtract the ones.
Subtract the tens.
Subtract the hundreds.
2

| 381 | 381 | $\longrightarrow$ | 21711 |
| :---: | :---: | :---: | :---: |
| - 285 | - 285 | $\longrightarrow$ | - 285 |
|  | 6 |  | 96 |

Since $1<5$, rename 8 tens as 7 tens and 10 ones. Then, 10 ones +1 one $=11$ ones.
3

| ${ }^{49} 0{ }^{16}$ | 506 |
| :---: | :---: |
| - 238 | - 238 |
| 8 | 268 |

Since $6<8$, rename 50 tens as 49 tens 10 ones. Then, 10 ones +6 ones $=16$ ones.

## Subtract.

1. 87
$\begin{array}{r}-\quad 53 \\ \hline\end{array}$
2. 

| $-\quad 40$ |
| :--- |

3. 854

| -630 |
| :--- |

4. 695

| $-\quad 132$ |
| :--- |

5. 34
$\begin{array}{r}-\quad 8 \\ \hline\end{array}$
6. $\quad 70$

| $-\quad 28$ |
| :--- |

7. $\$ 78$
$\begin{array}{r}-\quad 59 \\ \hline\end{array}$
8. 480
$\begin{array}{r}-\quad 63 \\ \hline\end{array}$
$\qquad$

## Subtracting <br> Whole Numbers (continued)

9. 407
$-139$
10. 908
$-439$
11. 735
$-596$
12. $\begin{array}{r}810 \\ -\quad 635 \\ \hline\end{array}$
13. 401
$-293$
14. 6243
$-4564$
15. 5690
$\begin{array}{r}-\quad 792 \\ \hline\end{array}$
16. $1516-835=$
17. $16,202-9814=$
18. $51,520-35,630=$
19. $70,605-38,296=$

## Solve.

29. A cassette recorder costs $\$ 340$ at one store. At another store, the same brand costs $\$ 298$. How much would you save by buying the recorder at the second store?
30. $8312-5943=$
31. $12,915-8036=$
32. $37,982-19,395=$
33. $30,005-17,008=$
34. The Colorado River is 1,450 miles long. The Yukon River is 1,770 miles long. How much longer is the Yukon River?
$\qquad$

## Multiplying Whole Numbers

To multiply by a one-digit whole number, first multiply the ones.
Then multiply the digits in each place from right to left.

## Example

| 1835 | $\rightarrow$ | 23 835 | $\longrightarrow$ | 23 835 |
| :---: | :---: | :---: | :---: | :---: |
| $\times 6$ | $\longrightarrow$ | $\times 6$ | $\longrightarrow$ | + 6 |
| 0 |  | 10 |  | 5010 |
| Multiply the ones. |  | Multiply the tens. |  | Multiply the hundreds |
|  |  | Add 3. |  | Add 2 . |

To multiply by a two digit whole number, first multiply by the ones. Then multiply by the tens.

## Examples



## Multiply.

1. 700
$\times 25$
2. 602
$\begin{array}{r}\times \quad 4 \\ \hline\end{array}$
3. 218
$\times 63$
4. $\$ 189$
$\times \quad 42$
5. $\$ 125$
$\times \quad 11$
6. 264
$\times 40$
7. 3265
72
$\times \quad 1$
8. 6019
$\times \quad 94$
$\qquad$

## Multiplying Whole Numbers (continued)

9. 3841
$\begin{array}{r}\times \quad 65 \\ \hline\end{array}$
10. $\$ 7903$

| $\times \quad 3$ |
| :--- |

13. 4216
$\begin{array}{r}\times \quad 8 \\ \hline\end{array}$
14. 5310

| $\times \quad 50$ |
| :--- |

15. 8020
$\begin{array}{r}\times \quad 16 \\ \hline\end{array}$
16. 19,634

| $\times \quad 25$ |
| :--- |


| 80 |
| ---: |
| $\times \quad 8$ |

12. $\begin{array}{r}28,706 \\ \times \quad 49 \\ \hline\end{array}$
13. $\begin{array}{r}28,706 \\ \times \quad 49 \\ \hline\end{array}$
14. $819 \times 8=$
15. $438 \times 6=$
16. $7253 \times 38=$
17. $450 \times 30=$
18. $79,025 \times 61=$
19. $\$ 605 \times 15=$

## Solve.

25. There are 42 rows of seats in the theater. There are 36 seats in each row. How many seats are in the theater?
26. A truck carries 278 crates. Each crate holds 45 pounds of fruit. How many pounds of fruit does the truck carry?
$\qquad$
$\qquad$

## Dividing Whole Numbers

To divide whole numbers, start with the digit in the left most position.
Then divide the digit in each place from left to right.

## Examples



Start with Divide the tens. Divide the ones.
the hundreds. $\quad$ The remainder is 0 .

$3 \quad 3468 \div 17$


Since $6<17$, the quotient has 0 tens.

## Divide.

1. $5 \longdiv { 3 2 5 5 }$
2. $7 0 \longdiv { 3 5 9 }$
3. $4 7 \longdiv { 5 1 7 }$
4. $1 8 \longdiv { 9 0 1 }$
$\qquad$

## Dividing Whole Numbers (continued)

## Divide.

5. $6 5 \longdiv { 1 3 0 0 }$
6. $5 0 \longdiv { 2 5 0 0 }$
7. $5 9 \longdiv { 3 7 7 6 }$
8. $2 3 \longdiv { 1 1 8 7 }$
9. $1 5 \longdiv { 1 2 6 0 }$
10. $9 \longdiv { 7 6 9 }$
11. $6 \longdiv { 5 2 4 6 }$
12. $1 2 \longdiv { 1 1 7 6 }$
13. $2 7 \longdiv { 1 4 3 5 }$
14. $3 7 \longdiv { 5 9 2 }$
15. $3 7 \longdiv { 1 0 0 0 }$
16. $8 1 \longdiv { 5 4 3 0 }$
17. $4 6 \longdiv { \$ 1 6 5 6 }$
18. $4 2 \longdiv { 2 4 8 0 }$
19. $8 6 \longdiv { 3 4 4 0 }$
20. $6 2 \longdiv { 1 8 5 8 }$
21. $7 2 \longdiv { 4 3 , 7 0 4 }$
22. $5202 \div 18=$
23. $37,513 \div 4=$

## Solve.

27. Each tent is put up with 12 poles. How many tents can be put up with 200 poles?
28. $4886 \div 17=$
29. Gary buys backpacks to sell at his sporting goods store. Each backpack costs $\$ 38$. How many backpacks can he buy for $\$ 270$ ?

## Divisibility Rules

The following rules will help you determine if a number is divisible by $2,3,4,5,6,8,9$, or 10 .

A number is divisible by:

- 2 if the ones digit is divisible by 2 .
- 3 if the sum of the digits is divisible by 3 .
- 4 if the number formed by the last two digits is divisible by 4 .
- 5 if the ones digit is 0 or 5 .
- 6 if the number is divisible by 2 and 3 .
- 8 if the number formed by the last three digits is divisible by 8 .
- 9 if the sum of the digits is divisible by 9 .
- 10 if the ones digit is 0 .

Example Determine whether 2120 is divisible by 2, 3, 4, 5, 6, 9, or 10.
2: The ones digit is divisible by 2 .
2120 is divisible by 2.
3: The sum of the digits $2+1+2+0=5$, is not divisible by 3 . 2120 is not divisible by 3 .
4: The number formed by the last two digits, 20 , is divisible by 4 . 2120 is divisible by 4 .
5: The ones digit is 0 . 2120 is divisible by 5 .
6: The number is divisible by 2 but not by 3 . 2120 is not divisible by 6 .
8: The number formed by the last 3 digits, 120 , is divisible by 8 . 2120 is divisible by 8 .
9: The sum of the digits, $2+1+2+0=5$, is not divisible by 9 . 2120 is not divisible by 9 .
10: The ones digit is 0 . 2120 is divisible by 10 .
2120 is divisible by $2,4,5,8$, and 10 .

Determine whether the first number is divisible by the second number. Write yes or no.

1. $4829 ; 9$
2. $1355 ; 10$
3. $3714 ; 8$
4. 20,$454 ; 6$
5. $482 ; 2$
6. $1692 ; 6$
7. $633 ; 3$
8. $724 ; 4$
9. $912 ; 9$
10. $559 ; 5$
11. $616 ; 8$
12. $3000 ; 4$
$\qquad$

## Divisibility Rules (continued)

Determine whether each number is divisible by $2,3,4,5,6,8$, 9, or 10.
13. 80
14. 91
15. 180
16. 333
17. 1024
18. 11,010
19. Is 9 a factor of 154 ?
20. Is 6 a factor of 102 ?
21. Is 486 divisible by 6 ?
22. Is 441 divisible by 9 ?

Determine whether the first number is divisible by the second number.
23. 4281; 2
24. 2670; 10
25. $3945 ; 6$
26. $6132 ; 4$
27. $8304 ; 3$
28. $6201 ; 9$
29. $4517 ; 9$
30. $2304 ; 8$
31. $7000 ; 5$
32. 10,$000 ; 8$
33. $9420 ; 6$
34. $822 ; 4$

Use mental math to find a number that satisfies the given conditions.
35. a number divisible by both 3 and 5
36. a four-digit number divisible by 3 , but not by 9
37. a five-digit number not divisible by 3 or 10
38. a four-digit number divisible by 2 and 4 , but not by 8

## Decimals and Place Value

You can use a place-value chart like the one below to help you write and read decimals and understand their values.

The decimal 160.289 is shown in the chart at the right. The place-value chart can be extended in either direction. The digit 9, together with its place value, names the number nine thousandths or 0.009 .


Notice that the decimal point separates the ones and tenths places.
It is read as and.
The decimal 160.289 is read as one hundred sixty and two hundred eighty-nine thousandths.

## Examples 1 Write nine and five hundred twenty-six ten-thousandths as a number.

 9.05262 Write 623.75 in words.
six hundred twenty-three and seventy-five hundredths

## Write the number named by the underlined digit in words.

1. 0.45
2. $2.36 \underline{9}$
3. 110.51
4. 43.672
5. $98.00 \underline{8}$
6. $5.312 \underline{6}$
7. $16.0 \underline{9}$
8. $2.06 \underline{7} 4$
9. 2.0674
10. $0.0 \underline{8} 7$
11. 0.0251
12. 7.5857
$\qquad$

## Decimals and Place Value (continued)

## Write each of the following as a decimal.

13. twelve hundredths
14. four and three tenths
15. five thousandths
16. fifty-one ten-thousandths
17. seventy-five and nine thousandths
18. one hundred four and thirty-four thousandths
19. twenty and four hundred forty-five ten-thousandths
20. sixteen and forty-five thousandths
21. fifty-six and thirty-four hundredths

Write each number in words.
22. 6.04
23. 0.017
24. 5.1648
25. 18.456
26. 145.007
27. 28.796
28. 787.462
29. 9.0045

## In the 1996 Olympics, Michael Johnson won both the men's 200-meter and 400-meter track competitions.

30. His time for the 200 -meter
competition was 19.32 seconds Write this decimal in words.
31. His time for the 400 -meter competition was forty-three and forty-nine hundredths seconds. Write this as a decimal.

## Rounding Decimals

Round 34.725 to the nearest tenth.
You can use a number line.

Find the approximate location of 34.725 on the number line.
34.725 is closer to 34.7 than to 34.8
34.725 rounded to the nearest tenth is 34.7 .


You can also round without a number line.

| Find the place | Look at the digit to the right. |  |
| :--- | :--- | :--- |
| to which you | If the digit is less than 5 , round down. | 2 is less than 5. |
| want to round. | If the digit is 5 or greater, round up. | Round down. |

34.725

$$
34.725
$$

Use each number line to show how to round the decimal to the nearest tenth.


Round each number to the underlined place-value position.
4. 6.32
5. $0.4 \underline{7} 21$
6. 26.444
7. 1.161
8. $362.08 \underline{46}$
9. $15.5 \underline{5} 3$
10. $151.3 \underline{9} 1$
11. 0.55
12. $631.00 \underline{0} 8$
13. $17.3 \underline{2} 7$
14. 3.09
15. 1.58
$\qquad$

## Rounding Decimals (continued)

Round each number to the underlined place-value position.
16. 1.726
17. 54.38
18. 0.58
19. 0.9142
20. 80.659
21. 232.1
22. 1.063
23. 0.55
24. 0.8194
25. $0.4 \underline{9} 6$
26. $3.01 \underline{8} 2$
27. 71.405
28. 9.63
29. 32.71
30. 2.671
31. $4.05 \underline{0} 7$
32. $89 . \underline{9} 5$
33. 0.134
34. 5.893
35. $52 \underline{0} .6$
36. $0.70 \underline{9} 8$
37. 1.845
38. 34.55
39. 29.25
40. $56.09 \underline{2} 4$
41. 1199.7
42. 0.46
43. 0.3546

## Comparing and Ordering Decimals

To compare decimals, you compare digits in each place-value position from left to right.

## Examples 1 Compare 3.0752 and 3.1042.



So, $3.0752<3.1042$.

2 Fill in the blank with $<,>$, or $=$ to make a true sentence.

$$
14.19
$$

$\qquad$ 14.103

In the hundredths place, $9>0$. So $14.19>14.103$.

3 Order the following set of decimals from least to greatest. 8.4, 8.41, 8.406, 8.442

Annex zeros so all decimals have the same number of place-value positions.
8.400, 8.410, 8.406, 8.442

So, $8.400<8.406<8.410<8.442$.
The decimals in order from least to greatest are
8.4, 8.406, 8.41, 8.442.

## State whether each statement is true or false.

1. $0.3=0.30$
2. $0.001=0.01$
3. $0.7>0.8$
4. $0.204<0.24$
5. $17=17.00$
6. $0.9>2.0$
$\qquad$
$\qquad$

## Comparing and Ordering Decimals (continued)

Fill in the blank with $<,>$, or $=$ to make a true sentence.
7. 0.205 $\qquad$ 0.250
8. 6.035 $\qquad$ 6.0353
9. 0.40 $\qquad$ 0.400
10. 0.55 $\qquad$ 0.5
11. 6.4 $\qquad$ 6.400
12. 1.05 $\qquad$ 1.005
13. 0.002 $\qquad$ 0.02
14. 0.615 $\qquad$ 0.651
15. 7 $\qquad$ 7.00
16. 15.3 $\qquad$ 15.30
17. 11.01 $\qquad$ 11.10
18. 124.6 $\qquad$ 124.48

## Order each set of decimals from least to greatest.

19. $0.03,0.3,0.003,3.0$
20. $5.23,5.203,5.21,5.3$
21. $0.91,0.866,0.9,0.87$
22. $2.03,2.13,2.3,2.033$
23. $16.4,16.04,16.45,16.001$
24. 8.7, 8.07, 8.17, 8.01
25. $114.2,114.02,114.202,114.002$
26. $0.362,0.306,0.31,0.36$

## Solve.

27. In gymnastics, Maria receives an average score of 9.7. Rebecca receives an average score of 9.69 . Who is the winner?
28. Three golfers have the following stroke averages. Rank the golfers in order from lowest to highest stroke average.

Lopez 71.2
Higuchi 72.17
Blalock 72.15
$\qquad$

## Adding Decimals

To add decimals, first line up the decimal points. Then add as with whole numbers.

Examples 1 Add: $36.801+8.945$.

$$
\begin{array}{r}
11 \\
36.801 \\
+8.945 \\
\hline 45.746
\end{array}
$$

2 Add: $7.3+9+8.45$.
7.30
$9.00 \quad$ Write 9 as 9.00.
8.45
+24.
24.75

3 Add: $\$ 415+\$ 29.05$.
1
$\$ 415.00$

+29.05 $\quad$\begin{tabular}{l}
Annex zeros to $\$ 415$ to help align <br>
\hline$\$ 444.05$

$\quad$

the decimal points.
\end{tabular}

Add.

1. $\$ 27.06$

| $+\quad 7.06$ |
| :--- |

2. |  | 1.034 |
| :--- | :--- |
| + | 0.08 |
3. 68.7

| +8.41 |
| :--- |

4. 42.6
$+21.919$
5. 93.7
$+24.85$
6. 140.98

| $+\quad 16.5$ |
| :--- |

7. 15.987
$\begin{array}{r}+9.07 \\ \hline\end{array}$
8. 478.98
$\begin{array}{r}+99.076 \\ \hline\end{array}$
9. 14.16
$\begin{array}{r}+\quad 8.9 \\ \hline\end{array}$
10. $\begin{array}{cc} & 67.032 \\ + & 5.98\end{array}$
11. $\begin{array}{r}246.38 \\ +\quad 19.976 \\ \hline\end{array}$
12. 17.32

| +5.98 |
| :--- |

$\qquad$
$\qquad$

## Adding Decimals (continued)

## Add.

13. 510.35

$$
\begin{array}{r}
+\quad 6.7 \\
\hline
\end{array}
$$

14. 83.675

| +2.95 |
| :--- |

18. 6.5
2.81

$$
+7.9
$$

21. 7.41
2.835
$+0.9$

| 17. | 0.4 |
| ---: | ---: |
| 0.6 | $\mathbf{1 8 .}$ |
| +0.7 | 2.5 |

22. $\$ 19.99$
7.99
$\begin{array}{r}+24.50 \\ \hline\end{array}$
23. 14.8 $+9.63$
24. 0.21
25. $\$ 3.33$
0.619
6.67
$\begin{array}{r}+0.394 \\ \hline\end{array}$
$\begin{array}{r}+0.24 \\ \hline\end{array}$
26. $3.04+0.6=$
27. $19.642+2.61=$
28. $1.61+3.807=$

## Solve.

29. A gymnast scored 9.65 on the beam, 9.59 on the floor, 9.76 on the bars, and 9.52 on the vault. What was the gymnast's total score?
30. $8+4.7=$
31. $8.543+3.29=$
32. $543+9.29=$
33. A ticket to the game cost Andrea $\$ 12$. She also spent $\$ 8.09$ on food. How much did she spend in all?

## Subtracting Decimals

To subtract decimals, line up the decimal points.
Then subtract as with whole numbers.

## Examples 1 Subtract: 8.1 - 4.75.

$$
\begin{array}{r}
0.10 \\
8.10 \\
-4.75 \\
\hline 3.35
\end{array}
$$

$$
\text { 8.10 Annex a zero to } 8.1 \text { to help align }
$$

the decimal points.

2 Subtract: \$84-\$1.79.

$$
\begin{aligned}
& \$ 3.9 .10 \\
& \$ 8.00^{30} \\
& -\quad 1.79 \\
& \hline \$ 82.21
\end{aligned}
$$

3 Subtract: 16.703-8.

$$
\begin{array}{r}
16.703 \\
-8.000 \\
\hline 8.703
\end{array}
$$

Annex two zeros to $\$ 84$ to help align the decimal points.

Annex three zeros to 8 to help align the decimal points.

## Subtract.

1. 9.14
$-2.075$
2. 712.53

| $-\quad 6.44$ |
| :--- |

3. 20.14

| $-\quad 8.093$ |
| :--- |

4. $\$ 12.65$

| $-\quad 10.99$ |
| :--- |

5. 14.395

| $-\quad 2.654$ |
| :--- |

6. 2.42
$-0.5$
7. 0.261
$-0.09$
8. 9.407
$-0.22$
9. 6.324
10. 42.903
$-0.75$
$\begin{array}{r}-\quad 8.05 \\ \hline\end{array}$
11. $\quad 16.37$

| $-\quad 5.609$ |
| :--- |

12. $\begin{array}{r}18 \\ -\quad 7.63 \\ \hline\end{array}$
$\qquad$

## Subtracting Decimals (continued)

Subtract.
13. $\quad 142.6$
$-85.92$
14. 25.37
$\begin{array}{r}-\quad 8.889 \\ \hline\end{array}$
18. $\quad 99.2$
$-38.576$
22. 0.4
$-0.15$
21. $\begin{gathered} \\ - \\ -1.5\end{gathered}$
25. 1
$-0.37$
26. 14.9
$\begin{array}{r}-\quad 8.261 \\ \hline\end{array}$
29. $6.51-0.8=$
31. $2.43-0.965=$
33. $210-56.765=$

Solve.
35. Mrs. Taylor's class has earned $\$ 190.32$ for their class project.
They need $\$ 250$. How much more do they need to earn?

23. |  | 112.8 |
| ---: | :--- |
| $-\quad 81.93$ |  |
24. $\begin{array}{r} \\ \hline\end{array} 26$
25. 48.3
$\begin{array}{r}-\quad 6.75 \\ \hline\end{array}$
26. 237.84

| $-\quad 6.964$ |
| :--- |

19. $\quad 12.752$
20. 639.07

| $-\quad 6.9$ |
| :--- |

$\begin{array}{r}-\quad 64.961 \\ \hline\end{array}$
27. $\$ 73$

| $-\quad 9.69$ |
| :--- |

28. 5
$-0.088$
29. $10.86-6.872=$
30. $\$ 81-\$ 4.83=$
31. $16.7-0.082=$
32. Connie has 20 mL of sulfuric acid.

Her experiment calls for 1.6 mL . How many mL will Connie have left after the experiment?

## Multiplying Decimals by Whole Numbers

To multiply a decimal by a whole number, first multiply as with whole numbers. Then place the decimal point in the product. The product has the same number of decimal places as the decimal factor.

Examples 1 Multiply: $421 \times 0.6$.
421
$\times 0.6$

252.6 $\quad$| 1 decimal place in the decimal factor |
| :--- |

2 Multiply: $\$ 6.16 \times 47$.
$\$ 6.16 \quad 2$ decimal places in the decimal factor
$\times 47$
4312
24640
$\$ 289.52 \quad$ « 2 decimal places in the product

## Multiply.

1. 23
$\times 0.8$
2. 45
$\times 0.9$
3. 216
$\times 0.2$
4. $\$ 0.83$
7
$\times \quad 7$
5. $\$ 4.16$
$\times \quad 15$
6. 27
$\begin{array}{r}\times 0.6 \\ \hline\end{array}$
7. 0.63
$\begin{array}{r}\times \quad 4 \\ \hline\end{array}$
8. $\$ 5.65$
$\begin{array}{r}\times \quad 14 \\ \hline\end{array}$
9. 231
$\times 0.41$
10. 0.62
$\times \quad 11$
11. $\$ 7.44$

| $\times \quad 26$ |
| :--- |

12. 218
$\begin{array}{r}\times 0.54 \\ \hline\end{array}$
$\qquad$

## Multiplying Decimals by Whole Numbers (continued)

## Multiply.

13. $\begin{array}{r}113 \\ \times 0.6 \\ \hline\end{array}$
14. 2.48
$\begin{array}{r}\times \quad 24 \\ \hline\end{array}$
15. $\quad 15.48$
$\begin{array}{r}\times \quad 19 \\ \hline\end{array}$
16. 214.8

| $\times \quad 37$ |
| :--- |

17. 438
18. 395
$\times 0.85$
$\times 2.63$
19. $\begin{array}{r}87 \\ \times 0.8 \\ \hline\end{array}$
20. 416
$\times 0.38$
21. $25 \times 0.15=$
22. $\$ 0.23 \times 15=$
23. $19 \times 0.19=$
24. $4.67 \times 15=$
25. $\$ 16.50 \times 12=$

## Solve.

31. Turkey is on sale for $\$ 0.89$ per pound. How much does William pay for a 14-pound turkey?
32. $419 \times 2.3=$
33. $0.842 \times 93=$
34. $143 \times 0.55=$
35. A clothing fabric factory needs 3.25 yards of fabric to make one skirt. How many yards are needed to make 2,000 skirts?
$\qquad$

## Multiplying Decimals by Decimals

Multiply decimals just like you multiply whole numbers. The number of decimal places in the product is equal to the sum of the number of decimal places in the factors.

Example Multiply 0.038 and $\mathbf{0 . 1 7}$.


The product is 0.00646 .

Place the decimal point in each product.

1. $1.47 \times 6=882$
2. $0.9 \times 2.7=243$
3. $6.48 \times 2.4=15552$

## Multiply.

4. 0.8
$\times \quad 7$
5. 0.04
$\times \quad 0.3$
6. 0.16
$\times \quad 26$
7. 

0.003
$\times \quad 4.2$
8. $12.2 \times 0.06$
9. $0.0015 \times 0.15$
10. $1.9 \times 2.2$
11. $3.59 \times 0.02$
12. $12.2 \times 0.007$
13. $0.7 \times 3.11$
$\qquad$
$\qquad$

## Multiplying Decimals by Decimals (continued)

Multiply.
14. 0.6
$\times 0.7$
15. 6.3
$\begin{array}{r} \\ \times 5.1 \\ \hline\end{array}$
16. $\quad 18.2$
$\times 0.51$
17. $0.52 \times 0.03$
18. $0.29 \times 29.1$
19. $6.1 \times 0.0054$
20. $6.8 \times 0.39$
21. $3.57 \times 0.09$
22. $3.72 \times 8.4$

Solve each equation.
23. $t=0.32 \times 0.05$
24. $6.4 \times 3.9=h$
25. $k=0.09 \times 2.3$
26. $a=0.4 \times 9$
27. $0.23 \times 0.003=m$
28. $1.09 \times 6.24=v$

Evaluate each expression if $\boldsymbol{m}=0.9$ and $\boldsymbol{n}=\mathbf{6 . 2}$.
29. $m \cdot 0.43$
30. $0.002 \cdot n$
31. $17.4 \cdot m$

Evaluate each expression if $\mathbf{a}=0.4$ and $\boldsymbol{b}=5.8$.
32. $0.48 \cdot a$
33. $b \cdot 13.8$
34. $0.003 \cdot a$
35. $1.4 \cdot b$
36. $3.6 \cdot a$
37. $24.5 \cdot a$
$\qquad$
$\qquad$

## Dividing Decimals by Whole Numbers

To divide a decimal by a whole number, first place the decimal point in the quotient directly above the decimal point in the dividend. Then divide as with numbers.

## Examples 1 Divide $\$ 58.10$ by 7.

|  | 8. |  | \$8.30 |
| :---: | :---: | :---: | :---: |
| $7 \longdiv { \$ 5 8 . 1 0 } \longrightarrow$ | $7 \longdiv { \$ 5 8 . 1 0 }$ | $\longrightarrow$ | $7 \longdiv { \$ 5 8 . 1 0 }$ |
|  | -56 |  | $-56 \downarrow$ |
| Place the decimal point in the quotient. | 2 |  | 21 |
|  |  |  | $-21 \downarrow$ |
|  |  |  | 00 |
|  |  |  | -00 |
|  |  |  | 0 |

2 Divide 17.5 by 14.


## Divide.

1. $9 \longdiv { 1 2 . 6 }$
2. $9 \longdiv { \$ 4 . 1 4 }$
3. $4 \longdiv { \$ 2 3 . 6 4 }$
4. $2 6 \longdiv { 0 . 5 2 }$
5. $1 6 \longdiv { 2 5 . 6 }$
6. $3 2 \longdiv { \$ 2 . 8 8 }$
7. $9 \longdiv { 2 7 . 5 4 }$
8. $4 \longdiv { \$ 1 1 . 6 0 }$
$\qquad$

## Dividing Decimals by Whole Numbers (continued)

## Divide.

9. $6 \longdiv { 1 . 5 }$
10. $1 8 \longdiv { 2 5 . 2 }$
11. $3 4 \longdiv { 5 3 . 7 2 }$
12. $1 4 \longdiv { 3 7 . 8 }$
13. $2 9 \longdiv { 1 0 4 . 4 }$
14. $3 4 \longdiv { 1 2 . 9 2 }$
15. $6 1 \longdiv { 1 0 3 . 7 }$
16. $7 4 \longdiv { 2 6 . 6 4 }$
17. $1 2 \longdiv { 3 0 1 . 8 }$
18. $3 3 \longdiv { 8 9 . 1 }$
19. $2 6 \longdiv { 5 0 . 7 }$
20. $1 5 \longdiv { \$ 6 2 . 4 0 }$
21. $2.4 \div 96=$
22. $15.5 \div 50=$
23. $30.45 \div 35=$
24. $41.8 \div 55=$

Solve.
29. Eric bought an 8 -ounce can of frozen orange juice on sale for $\$ 0.72$. What is the cost per ounce?
22. $5.59 \div 26=$
24. $34.55 \div 20=$
26. $27.93 \div 19=$
28. $411.84 \div 72=$
30. Lucy runs 4 miles in 22.7 minutes. What is her average time per mile?

## Dividing Decimals by Decimals

To divide by a decimal, change the divisor to a whole number.

Example Find $0.5194 \div 0.49$.

0.49. \begin{tabular}{r}
1.06 <br>
$\frac{0.51 .94}{49}$ <br>

| 294 |
| ---: |
| 294 |
| 0 |

\end{tabular}

Change 0.49 to 49.
Move the decimal point two places to the right.
Move the decimal point in the dividend the same number of places to the right.
Divide as with whole numbers.

## Without finding or changing each quotient, change each problem so that the divisor is a whole number.

1. $3.4 \div 1.1$
2. $76.44 \div 0.006$
3. $0.56 \div 0.4$
4. $89.45 \div 0.908$
5. $5.675 \div 6.8$
6. $0.00864 \div 0.012$
7. $0.84 \div 0.2$
8. $1.02 \div 0.3$
9. $3.9 \div 1.3$
10. $13.6 \div 0.003$
11. $1.622 \div 1.4$
12. $0.00025 \div 0.035$

## Divide.

13. $0 . 9 \longdiv { 6 . 3 }$
14. $0 . 6 \longdiv { 0 . 5 4 0 }$
15. $0 . 3 \longdiv { 1 2 9 }$
16. $2 . 4 \longdiv { 0 . 1 9 2 }$
17. $0 . 4 4 \longdiv { 5 . 2 8 }$
18. $0 . 0 2 5 \longdiv { 0 . 0 4 }$
$\qquad$

## Dividing Decimals by Decimals (continued)

## Divide.

19. $0 . 5 \longdiv { 9 . 5 }$
20. $0 . 8 \longdiv { 0 . 0 4 8 }$
21. $0 . 4 \longdiv { 8 2 }$
22. $3 . 5 \longdiv { 2 . 3 8 }$
23. $0 . 6 2 \longdiv { 6 0 0 . 1 6 }$
24. $8 \longdiv { 0 . 0 0 9 2 }$
25. $0 . 3 8 \longdiv { 7 6 0 . 3 8 }$
26. $1 . 4 \longdiv { 1 2 1 . 8 }$
27. $0 . 0 1 5 \longdiv { 0 . 0 6 }$
28. $1 . 3 \longdiv { 7 8 0 }$
29. $0 . 0 8 \longdiv { 0 . 0 0 1 2 }$
30. $0 . 7 \longdiv { 5 . 9 5 }$

Solve each equation.
31. $7.8 \div 2.6=k$
32. $3.92 \div 0.08=m$
33. $s=149.73 \div 0.23$
34. $v=155 \div 0.1$
35. $c=1098 \div 6.1$
36. $3633.4 \div 3.7=d$
37. $903.6 \div 25.1=n$
38. $363.6 \div 5=r$
39. $2.004 \div 0.2=b$
40. $w=84.7 \div 3.85$
41. $165.2 \div 8.26=t$
42. $29.28 \div 1.22=s$
43. $y=0.0528 \div 0.06$
44. $16.84 \div 0.4=m$
45. $k=2.05 \div 0.5$

## Multiplying Decimals by Powers of 10

You can find the product of a decimal and a power of 10 without using a calculator or paper and pencil. Suppose you wanted to find the product of 36 and powers of 10 .

| Decimal | Power of Ten |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 36 | $\div$ | $10^{-3}$ or 0.001 | $=$ | Quotient |
| 36 | $\div$ | $10^{-2}$ or 0.01 | $=$ | 0.036 |
| 36 | $\div$ | $10^{-1}$ or 0.1 | $=$ | 3.6 |
| 36 | $\div$ | $10^{0}$ or 1 | $=$ | 36 |
| 36 | $\div$ | $10^{1}$ or 10 | $=$ | 360 |
| 36 | $\div$ | $10^{2}$ or 100 | $=$ | 3600 |
| 36 | $\div$ | $10^{3}$ or 1000 | $=$ | 36,000 |
| 36 | $\div$ | $10^{4}$ or 10,000 | $=$ | 360,000 |

For powers of 10 that are less than 1, the exponent in the power of 10 tells you the number of places to move the decimal point to the right. For powers of 10 that are greater than 1 , the decimal point moves to the left.

Examples $1 \quad \mathbf{6} \cdot \mathbf{1 0}^{\mathbf{3}}=\mathbf{6 0 0 0} \quad$ Move the decimal point 3 places to the right.
$24.5 \cdot \mathbf{1 0}^{-2}=\mathbf{0 . 0 4 5} \quad$ Move the decimal point 2 places to the left.

## Multiply mentally.

1. $8 \cdot 0.01$
2. $55.8 \cdot 100$
3. $59 \cdot 10^{4}$
4. $14 \cdot 0.1$
5. $0.13 \cdot 10^{-3}$
6. $18 \cdot 10^{2}$
7. $17 \cdot 100$
8. $1.46 \cdot 0.001$
9. $12 \cdot 10^{-1}$
$\qquad$
$\qquad$

## Multiplying Decimals by Powers of 10 (continued)

## Multiply mentally.

10. $77 \cdot 1000$
11. $143 \cdot 100$
12. $15 \cdot 10$
13. $15 \cdot 10^{0}$
14. $1.36 \cdot 1000$
15. $184 \cdot 10^{-3}$
16. $1.7 \cdot 0.01$
17. $0.08 \cdot 10^{-2}$
18. $1432 \cdot 10^{4}$
19. $43 \cdot 10$
20. $13.5 \cdot 0.01$
21. $55 \cdot 10^{-2}$
22. $137 \cdot 100$
23. $43 \cdot 1000$
24. $281 \cdot 10^{2}$

Solve each equation.
25. $v=78 \cdot 10$
26. $q=654 \cdot 10^{0}$
27. $m=198 \cdot 0.001$
28. $r=876 \cdot 100$
29. $s=15 \cdot 10^{-2}$
30. $t=12.5 \cdot 0.01$
31. $p=1.4 \cdot 1000$
32. $q=385 \cdot 10^{-3}$
33. $u=8.8 \cdot 10$
34. $14 \cdot 100=r$
35. $w=1.34 \cdot 10^{3}$
36. $k=14.8 \cdot 0.1$
37. $n=123 \cdot 0.1$
38. $4326 \cdot 10^{0}=y$
39. $81.18 \cdot 10^{-3}=j$
40. $480 \cdot 10^{4}=m$
41. $r=6820 \cdot 10^{1}$
42. $q=2.813 \cdot 10^{-2}$

## Dividing Decimals by Powers of 10

You can find the quotient of a decimal and a power of 10 without using a calculator or paper and pencil. Suppose you wanted to find the quotient of 5540 and powers of 10 .

| Decimal | Power of Ten |  |  |  |
| :---: | :---: | :---: | :--- | :---: |
| 5540 | $\div$ | $10^{-3}$ or 0.001 | $=$ | $5,540,000$ |
| 5540 | $\div$ | $10^{-2}$ or 0.01 | $=$ | 554,000 |
| 5540 | $\div$ | $10^{-1}$ or 0.1 | $=$ | 55,400 |
| 5540 | $\div$ | 100 or 1 | $=$ | 5540 |
| 5540 | $\div$ | $10^{1}$ or 10 | $=$ | 554 |
| 5540 | $\div$ | $10^{2}$ or 100 | $=$ | 55.4 |
| 5540 | $\div$ | $10^{3}$ or 1000 | $=$ | 5.54 |
| 5540 | $\div$ | $10^{4}$ or 10,000 | $=$ | 0.554 |

For powers of 10 that are less than 1, the exponent in the power of 10 tells you the number of places to move the decimal point to the left. For powers of 10 that are greater than 1 , the decimal point moves to the right.

Examples $18 \div 103=0.008$
$20.34 \div 10^{-2}=34$

Move the decimal point 3 places to the left.
Move the decimal point 2 places to the right.

## Divide mentally.

1. $6 \div 0.01$
2. $35.7 \div 100$
3. $764 \div 10^{4}$
4. $18 \div 0.1$
5. $0.145 \div 10^{-3}$
6. $24 \div 10^{2}$
7. $47 \div 100$
8. $1.53 \div 0.001$
9. $61 \div 10^{-1}$
$\qquad$

## Dividing Decimals by Powers of 10 (continued)

Divide mentally.
10. $88 \div 1000$
11. $234 \div 100$
12. $34 \div 10$
13. $19 \div 10^{0}$
14. $1.27 \div 1000$
15. $765 \div 10^{-3}$
16. $1.1 \div 0.01$
17. $0.04 \div 10^{-2}$
18. $1561 \div 10^{4}$
19. $54 \div 10$
20. $15.2 \div 0.01$
21. $66 \div 10^{-2}$
22. $128 \div 100$
23. $55,510 \div 1000$
24. $426 \div 10^{2}$

Solve each equation.
25. $v=87 \div 10$
26. $q=737 \div 10^{0}$
27. $m=891 \div 0.001$
28. $r=678 \div 100$
29. $s=24 \div 10^{-2}$
30. $t=16.4 \div 0.01$
31. $p=1.3 \div 1000$
32. $q=0.573 \div 10^{-3}$
33. $u=9.9 \div 10$
34. $148 \div 100=r$
35. $w=1.28 \div 10^{3}$
36. $k=16.5 \div 0.1$
37. $n=154 \div 0.1$
38. $3546 \div 10^{0}=y$
39. $41.14 \div 10^{-3}=j$
40. $360 \div 10^{4}=m$
41. $r=7610 \div 10^{1}$
42. $q=2.532 \div 10^{-2}$
$\qquad$

## Equivalent Fractions

To find equivalent fractions, multiply or divide the numerator and denominator by the same nonzero number.


The shaded region at the right shows that $\frac{4}{16}$ and $\frac{1}{4}$ are equivalent.


## Examples

1 Complete $\frac{9}{12}=\frac{18}{}$ so that the fractions are equivalent.


Since $9 \times 2=18$, multiply both the numerator and the denominator by 2 .

2 Find three fractions equivalent to $\frac{4}{9}$.


Complete so that the fractions are equivalent.

1. $\frac{3}{4}=\frac{}{12}$
2. $\frac{4}{9}=\frac{}{18}$
3. $\frac{4}{5}=\frac{}{20}$
4. $\frac{5}{8}=\frac{}{24}$
$\qquad$

## Equivalent Fractions (continued)

Complete so that the fractions are equivalent.
5. $\frac{3}{5}=\underline{15}$
6. $\frac{5}{7}=\underline{10}$
7. $\frac{4}{9}=\underline{12}$
8. $\frac{3}{8}=\frac{6}{}$
9. $\frac{2}{3}=\frac{-}{24}$
10. $\frac{5}{15}=\frac{-}{3}$
11. $\frac{5}{20}=\frac{}{4}$
12. $\frac{7}{56}=\frac{}{8}$
13. $\frac{16}{40}=\frac{2}{}$
14. $\frac{27}{72}=\frac{3}{}$
15. $\frac{40}{64}=\frac{5}{}$
16. $\frac{10}{45}=\frac{2}{}$
17. $\frac{16}{18}=\frac{8}{}$
18. $\frac{4}{7}=\frac{}{42}$
19. $\frac{6}{11}=\frac{}{33}$
20. $\frac{5}{12}=\frac{25}{}$

Find three fractions equivalent to each of the following.
21. $\frac{1}{2}$
22. $\frac{4}{5}$
23. $\frac{2}{3}$
24. $\frac{5}{6}$
25. $\frac{7}{8}$
26. $\frac{9}{10}$

## Solve.

27. Ms. Yen works 10 months of 12 each year. Give two fractions that represent the fraction of a year she works.
28. During a basketball game, there are 10 players on the floor. Five of the players are on the home team. Give two fractions that represent the fraction of players on the floor that are on the home team.

## Simplifying Fractions

To write a fraction in simplest form, divide both the numerator and denominator by their greatest common factor (GCF).
Example 1 Write $\frac{16}{100}$ in simplest form.

| Step 1 | Step 2 |
| :--- | :--- |
| Find the GCF of 16 and 100. |  |
| You can use prime factorization. | Divide both 16 and 100 by their |
| $16=2 \times 2 \times 2 \times 2$ |  |
| $100=2 \times 2 \times 5$ |  |
| GCF: $2 \times 2=4$ |  |
|  |  |
|  | A fraction is in simplest form when <br> the GCF of both its numerator and <br> denominator is l. |

The fraction $\frac{16}{100}$ written in simplest from is $\frac{4}{25}$.

Example 2 Write $\frac{6}{15}$ in simplest form.


Write each fraction in simplest form.

1. $\frac{4}{6}$
2. $\frac{2}{4}$
3. $\frac{6}{12}$
4. $\frac{8}{10}$
5. $\frac{6}{14}$
6. $\frac{6}{9}$
7. $\frac{2}{8}$
8. $\frac{3}{12}$
$\qquad$

## Simplifying Fractions (continued)

Write each fraction in simplest form.
9. $\frac{13}{26}$
10. $\frac{16}{24}$
11. $\frac{12}{18}$
12. $\frac{12}{16}$
13. $\frac{5}{15}$
14. $\frac{15}{25}$
15. $\frac{3}{15}$
16. $\frac{10}{30}$
17. $\frac{9}{21}$
18. $\frac{14}{30}$
19. $\frac{20}{36}$
20. $\frac{6}{24}$
21. $\frac{27}{9}$
22. $\frac{10}{100}$
23. $\frac{25}{40}$
24. $\frac{8}{16}$
25. $\frac{10}{25}$
26. $\frac{8}{40}$
27. $\frac{12}{30}$
28. $\frac{16}{20}$
29. $\frac{7}{42}$
30. $\frac{15}{30}$
31. $\frac{9}{33}$
32. $\frac{10}{16}$

## Solve. Write the answer in simplest form.

33. Tara takes 12 vacation days in June, which has 30 days. What fraction of the month is she on vacation?
Express your answer in simplest form.
34. During a one-hour (60 minute) practice, Calvin shot free throws for 15 minutes. What fraction of an hour did he shoot free throws? Express your answer in simplest form.

## Writing Improper Fractions as Mixed Numbers

A fraction such as $\frac{8}{5}$ is called an improper fraction because the numerator is greater than the denominator. Improper fractions are often expressed as mixed numbers. A mixed number is the sum of a whole number and a fraction. Follow the steps in Example 1 to write $\frac{8}{5}$ as a mixed number.
Example 1 Write $\frac{8}{5}$ as a mixed number in simplest form.

| Step 1 | Step 2 |
| :---: | :---: |
| Divide the numerator | Write the remainder |
| by the denominator. | as a fraction. |
| $5 \sqrt{8}$ | $5)_{8}^{5}$ |
| $\frac{-5}{3}$ | $\frac{-5}{3}$ |

Example 2 Write $\frac{38}{4}$ as a mixed number in simplest form.

$$
\begin{aligned}
& \quad 9 \frac{2}{4}=9 \frac{1}{2} \\
& 4 \longdiv { 3 8 } \\
& -36 \\
& \frac{2}{2}
\end{aligned}
$$

Write each improper fraction as a mixed number in simplest form.

1. $\frac{7}{5}$
2. $\frac{13}{8}$
3. $\frac{13}{4}$
4. $\frac{22}{7}$
5. $\frac{6}{4}$
6. $\frac{14}{8}$
7. $\frac{9}{6}$
8. $\frac{14}{10}$
$\qquad$
$\qquad$

## Writing Improper Fractions as Mixed Numbers (continued)

Write each improper fraction as a mixed number in simplest form.
9. $\frac{28}{16}$
10. $\frac{25}{10}$
11. $\frac{33}{9}$
12. $\frac{40}{16}$
13. $\frac{13}{5}$
14. $\frac{9}{2}$
15. $\frac{15}{3}$
16. $\frac{21}{8}$
17. $\frac{17}{12}$
18. $\frac{12}{5}$
19. $\frac{13}{3}$
20. $\frac{15}{10}$
21. $\frac{28}{12}$
22. $\frac{21}{5}$
23. $\frac{19}{6}$
24. $\frac{31}{8}$
25. $\frac{16}{5}$
26. $\frac{27}{15}$
27. $\frac{32}{12}$
28. $\frac{48}{24}$
29. $\frac{36}{24}$
30. $\frac{25}{20}$
31. $\frac{30}{12}$
32. $\frac{24}{10}$

Solve. Write each answer as a mixed number in simplest form.
33. Carrie rode her bike 22 miles in 3 hours. What is the average number of miles she rode in one hour?
34. Mr. Steele has managed the Classic Theater for 21 months. How many years has he managed the Classic Theater?

## Writing Mixed Numbers as Improper Fractions

Follow the steps in Example 1 to change a mixed number to an improper fraction.
Example 1 Write $3 \frac{1}{2}$ as an improper fraction.

| Step 1 | Step 2 |
| :--- | :---: |
| First multiply the whole number <br> by the denominator and add the <br> numerator. Then write this sum <br> over the denominator. | Simplify. |
| $3 \frac{1}{2}=\frac{(3 \times 2)+1}{2}$ |  |

Example 2 Write $8 \frac{3}{5}$ as an improper fraction.

$$
8 \frac{3}{5}=\frac{(5 \times 8)+3}{5}=\frac{43}{5}
$$

Write each mixed number as an improper fraction.

1. $6 \frac{1}{3}$
2. $5 \frac{3}{4}$
3. $7 \frac{1}{6}$
4. $9 \frac{1}{8}$
5. $2 \frac{3}{16}$
6. $4 \frac{3}{10}$
7. $4 \frac{2}{3}$
8. $3 \frac{3}{5}$
9. $5 \frac{6}{7}$
10. $3 \frac{7}{9}$
11. $2 \frac{11}{12}$
12. $4 \frac{7}{8}$
$\qquad$

## Writing Mixed Numbers as Improper Fractions (continued)

Write each mixed number as an improper fraction.
13. $1 \frac{3}{8}$
14. $5 \frac{2}{5}$
15. $2 \frac{3}{4}$
16. $1 \frac{7}{8}$
17. $1 \frac{7}{12}$
18. $4 \frac{1}{2}$
19. $2 \frac{9}{10}$
20. $3 \frac{5}{8}$
21. $3 \frac{2}{3}$
22. $4 \frac{3}{4}$
23. $5 \frac{2}{3}$
24. $5 \frac{1}{8}$
25. $5 \frac{9}{10}$
26. $6 \frac{7}{8}$
27. $4 \frac{3}{10}$
28. $10 \frac{2}{3}$
29. $9 \frac{7}{12}$
30. $8 \frac{5}{11}$
31. $15 \frac{2}{7}$
32. $12 \frac{4}{7}$
33. $11 \frac{4}{5}$
34. $18 \frac{2}{3}$
35. $20 \frac{1}{4}$
36. $16 \frac{4}{9}$
37. $5 \frac{12}{13}$
38. $16 \frac{2}{13}$
39. $24 \frac{1}{3}$
40. $8 \frac{16}{17}$
41. $9 \frac{5}{17}$
42. $7 \frac{6}{19}$
43. $5 \frac{8}{9}$
44. $16 \frac{10}{13}$

## Comparing and Ordering Fractions

One way to compare fractions is to express them as fractions with the same denominator. The least common denominator (LCD) is the least common multiple of the denominators.

Example Replace the $\square$ with $<,>$, or $=$ to make a true sentence. $\frac{5}{8} \bigcirc \frac{2}{3}$
The LCM of 8 and 3 is 24 . Express $\frac{5}{8}$ and $\frac{2}{3}$ as fractions with a denominator of 24 .

$\frac{15}{24} \bigcirc \frac{16}{24}$
Compare the numerators. Since $15<16$,

$$
\frac{15}{24}<\frac{16}{24} \text {. Therefore, } \frac{5}{8}<\frac{2}{3} .
$$

Find the LCD for each pair of fractions.

1. $\frac{2}{5}, \frac{1}{3}$
2. $\frac{3}{4}, \frac{5}{6}$
3. $\frac{1}{2}, \frac{4}{7}$
4. $\frac{4}{5}, \frac{2}{3}$
5. $\frac{5}{8}, \frac{7}{12}$
6. $\frac{1}{2}, \frac{6}{7}$
7. $\frac{1}{6}, \frac{9}{10}$
8. $\frac{3}{4}, \frac{2}{9}$
9. $\frac{5}{12}, \frac{3}{16}$

Replace each $\bigcirc$ with $<,>$, or $=$ to make a true sentence.
10. $\frac{3}{4} \bigcirc \frac{4}{5}$
11. $\frac{3}{8} \bigcirc \frac{9}{24}$
12. $\frac{2}{3} \bigcirc \frac{9}{15}$
13. $\frac{7}{12} \bigcirc \frac{2}{3}$
14. $\frac{5}{11} \bigcirc \frac{1}{3}$
15. $\frac{27}{36} \bigcirc \frac{3}{4}$
$\qquad$
$\qquad$

## Comparing and Ordering Fractions (continued)

 with $<,>$, or $=$ to make a true sentence.16. $\frac{5}{6} \bigcirc \frac{7}{8}$
17. $\frac{6}{7} \bigcirc \frac{4}{5}$
18. $\frac{3}{9} \bigcirc \frac{1}{3}$
19. $\frac{5}{8} \bigcirc \frac{7}{12}$
20. $\frac{5}{7} \bigcirc \frac{7}{10}$
21. $\frac{2}{3} \bigcirc \frac{3}{4}$
22. $\frac{2}{15} \bigcirc \frac{1}{6}$
23. $\frac{3}{8} \bigcirc \frac{6}{16}$
24. $\frac{5}{12} \bigcirc \frac{2}{5}$
25. $\frac{3}{10} \bigcirc \frac{5}{14}$
26. $\frac{4}{9} \bigcirc \frac{3}{7}$
27. $\frac{1}{6} \bigcirc \frac{2}{12}$
28. $\frac{3}{5} \bigcirc \frac{5}{9}$
29. $\frac{7}{9} \bigcirc \frac{4}{7}$
30. $\frac{9}{10} \bigcirc \frac{11}{12}$
31. $\frac{1}{4} \bigcirc \frac{2}{8}$
32. $\frac{2}{9} \bigcirc \frac{4}{15}$
33. $\frac{8}{9} \bigcirc \frac{7}{8}$

Order the following fractions from least to greatest.
34. $\frac{3}{4}, \frac{2}{5}, \frac{5}{8}, \frac{1}{2}$
35. $\frac{2}{3}, \frac{4}{9}, \frac{5}{6}, \frac{7}{12}$
36. $\frac{1}{3}, \frac{2}{7}, \frac{3}{14}, \frac{1}{6}$
37. $\frac{7}{15}, \frac{3}{5}, \frac{5}{12}, \frac{1}{2}$
38. $\frac{11}{12}, \frac{5}{6}, \frac{3}{4}, \frac{9}{16}$
39. $\frac{4}{5}, \frac{2}{3}, \frac{11}{35}, \frac{7}{9}$
40. $\frac{7}{8}, \frac{4}{5}, \frac{3}{4}, \frac{9}{10}$
41. $\frac{1}{3}, \frac{2}{5}, \frac{3}{12}, \frac{3}{10}$
42. $\frac{1}{2}, \frac{3}{5}, \frac{2}{7}, \frac{5}{9}$
43. $\frac{1}{10}, \frac{2}{3}, \frac{1}{12}, \frac{5}{6}$
$\qquad$

## Multiplying Fractions

To multiply fractions, multiply the numerators. Then multiply the denominators. Simplify the product if possible.
Examples 1 Multiply $\frac{4}{7}$ times $\frac{\mathbf{5}}{\mathbf{9}}$.

$$
\begin{aligned}
\frac{4}{7} \times \frac{5}{9} & =\frac{4 \times 5}{7 \times 9} & & \begin{array}{l}
\text { Multiply the numerators. } \\
\text { Multiply the denominators }
\end{array} \\
& =\frac{20}{63} & &
\end{aligned}
$$

The product of $\frac{4}{7}$ and $\frac{5}{9}$ is $\frac{20}{63}$.

2 Multiply $\frac{\mathbf{5}}{\mathbf{6}}$ times $\frac{\mathbf{3}}{\mathbf{5}}$.

$$
\begin{aligned}
\frac{5}{6} \times \frac{3}{5} & =\frac{5 \times 3}{6 \times 5} & & \text { Multiply the numerators. } \\
& =\frac{15}{30} \text { or } \frac{1}{2} & & \text { Multiply the denominators. }
\end{aligned}
$$

The product of $\frac{5}{6}$ and $\frac{3}{5}$ is $\frac{1}{2}$.

## Multiply.

1. $\frac{2}{3} \times \frac{1}{4}$
2. $\frac{3}{7} \times \frac{1}{2}$
3. $\frac{1}{3} \times \frac{3}{5}$
4. $\frac{1}{2} \times \frac{6}{7}$
5. $\frac{7}{10} \times \frac{5}{7}$
6. $\frac{1}{4} \times \frac{1}{4}$
7. $\frac{1}{3} \times \frac{1}{5}$
8. $\frac{5}{8} \times \frac{1}{2}$
9. $\frac{4}{9} \times \frac{3}{4}$
10. $\frac{2}{3} \times \frac{3}{8}$
11. $\frac{1}{7} \times \frac{1}{7}$
12. $\frac{2}{9} \times \frac{1}{2}$
13. $\frac{3}{5} \times \frac{5}{6}$
14. $\frac{2}{7} \times \frac{1}{3}$
15. $\frac{5}{12} \times \frac{1}{5}$
16. $\frac{1}{2} \times \frac{1}{5}$
17. $\frac{6}{7} \times \frac{8}{15}$
18. $\frac{8}{9} \times \frac{9}{10}$
19. $\frac{4}{5} \times \frac{5}{14}$
20. $\frac{7}{8} \times \frac{4}{9}$
21. $\frac{5}{8} \times \frac{3}{4}$

## Multiplying Fractions (continued)

## Use the recipe for lemon chicken saute below to answer Exercises 22-25.

| 6 boneless chicken breasts, rolled in flour | $\frac{1}{3}$ cup teriyaki sauce |
| :--- | :--- |
| $\frac{1}{4}$ cup butter | $\frac{1}{2}$ teaspoon sugar |
| 3 tablespoons lemon juice | $\frac{1}{8}$ teaspoon pepper |
| 1 teaspoon garlic |  |

22. If Julie wants to make half of this recipe, how much pepper should she use?
23. If Julie wants to make one-third of this recipe, how much teriyaki sauce should she use?
24. If Julie wants to make two-thirds of this recipe, how much sugar should she use?
25. If Julie wants to make two-thirds of this recipe, how much butter should she use?
26. If about $\frac{1}{3}$ of Earth is able to be farmed and $\frac{2}{5}$ of this land is planted in grain crops, what part of Earth is planted in grain crops?
27. Two fifths of the students at Main Street Middle School are in seventh grade. If half of the students in seventh grade are boys, what fraction of the students are seventh grade boys?
$\qquad$

## Multiplying Fractions and Mixed Numbers

To multiply fractions: Multiply the numerators.
Then multiply the denominators.
$\frac{5}{6} \times \frac{3}{5}=\frac{5 \times 3}{6 \times 5}=\frac{15}{30}=\frac{1}{2}$

To multiply mixed numbers: Rename each mixed number as a fraction. Multiply the fractions.

$$
7 \times 1 \frac{1}{4}=\frac{7}{1} \times \frac{5}{4}=\frac{35}{4}=8 \frac{3}{4}
$$

Multiply. Write each product in simplest form.

1. $\frac{2}{3} \times \frac{1}{4}$
2. $\frac{3}{7} \times \frac{1}{2}$
3. $\frac{1}{3} \times \frac{3}{5}$
4. $\frac{1}{2} \times \frac{6}{7}$
5. $\frac{3}{8} \times 4$
6. $\frac{7}{10} \times \frac{5}{7}$
7. $\frac{4}{9} \times 3$
8. $\frac{1}{4} \times \frac{1}{4}$
9. $1 \frac{1}{2} \times 6$
10. $\frac{3}{4} \times 1 \frac{2}{3}$
11. $3 \frac{1}{3} \times 2 \frac{1}{2}$
12. $4 \frac{1}{5} \times \frac{1}{7}$
$\qquad$

## Multiplying Fractions and Mixed Numbers (continued)

Multiply. Write each product in simplest form.
13. $1 \frac{1}{9} \times \frac{3}{5}$
14. $6 \times \frac{11}{12}$
15. $\frac{1}{2} \times 2 \frac{2}{3}$
16. $\frac{2}{3} \times \frac{1}{2}$
17. $\frac{3}{4} \times \frac{1}{9}$
18. $3 \times \frac{4}{9}$
19. $\frac{1}{5} \times \frac{1}{4}$
20. $\frac{1}{4} \times \frac{4}{5}$
21. $\frac{4}{9} \times \frac{3}{4}$
22. $\frac{13}{21} \times \frac{7}{13}$
23. $\frac{7}{8} \times \frac{4}{9}$
24. $\frac{5}{7} \times \frac{7}{10}$
25. $\frac{4}{5} \times \frac{5}{14}$
26. $\frac{1}{4} \times \frac{5}{8}$
27. $\frac{2}{3} \times \frac{5}{9}$
28. $\frac{4}{5} \times 7$
29. $2 \frac{2}{5} \times 1 \frac{3}{7}$
30. $6 \times \frac{2}{3}$
31. $3 \frac{3}{4} \times \frac{1}{2}$
32. $1 \frac{5}{9} \times 2 \frac{4}{7}$
33. $4 \frac{1}{3} \times \frac{1}{2}$

## Dividing Fractions

To divide by a fraction, multiply by its reciprocal.
Simplify the quotient if possible.

## Examples 1 Divide $\frac{2}{3}$ by $\frac{5}{7}$.

$$
\begin{aligned}
\frac{2}{3} \div \frac{5}{7} & =\frac{2}{3} \times \frac{7}{5} & & \text { Multiply by the reciprocal of } \frac{5}{7} . \\
& =\frac{2 \times 7}{3 \times 5} & & \text { Multiply the numerators. } \\
& =\frac{14}{15} & &
\end{aligned}
$$

The quotient is $\frac{14}{15}$.
2 Divide $\frac{3}{4}$ by $\frac{9}{10}$.

$$
\begin{aligned}
\frac{3}{4} \div \frac{9}{10} & =\frac{3}{4} \times \frac{10}{9} & & \text { Multiply by the reciprocal of } \frac{9}{10} . \\
& =\frac{3 \times 10}{4 \times 9} & & \text { Multiply the numerators. } \\
& =\frac{30}{36} \text { or } \frac{5}{6} & & \text { Sultiply the denominators. }
\end{aligned}
$$

The quotient is $\frac{5}{6}$.

## Divide.

1. $\frac{3}{4} \div \frac{1}{2}$
2. $\frac{4}{5} \div \frac{1}{3}$
3. $\frac{1}{5} \div \frac{1}{4}$
4. $\frac{4}{7} \div \frac{8}{9}$
5. $\frac{3}{8} \div \frac{3}{4}$
6. $\frac{9}{7} \div \frac{3}{14}$
7. $\frac{4}{5} \div \frac{2}{5}$
8. $\frac{7}{8} \div \frac{1}{4}$
9. $\frac{2}{5} \div \frac{5}{8}$
$\qquad$

## Dividing Fractions (continued)

## Divide.

10. $\frac{1}{3} \div \frac{1}{6}$
11. $\frac{5}{8} \div \frac{5}{12}$
12. $\frac{4}{5} \div \frac{2}{7}$
13. $\frac{2}{5} \div \frac{3}{10}$
14. $\frac{5}{7} \div \frac{3}{4}$
15. $\frac{2}{3} \div \frac{4}{9}$
16. $\frac{4}{7} \div \frac{4}{5}$
17. $\frac{5}{6} \div \frac{1}{9}$
18. $\frac{4}{5} \div \frac{2}{3}$
19. About $\frac{1}{20}$ of the population of the world lives in South America. If about $\frac{1}{35}$ of the population of the world lives in Brazil, what fraction of the population of South America lives in Brazil?
20. Three fourths of a pizza is left. If the pizza was originally cut in $\frac{1}{8}$ pieces, how many pieces are left?

The area of each rectangle is given. Find the missing length for each rectangle.
21.

22.

23.

24.

$\qquad$

## Dividing Fractions and Mixed Numbers

To divide fractions and mixed numbers:

1. Write any mixed numbers as improper fractions.
2. Find the reciprocal of the divisor.
3. Multiply the dividend by the reciprocal of the divisor.

$$
\begin{aligned}
& \text { Examples } 1 \quad \mathbf{5} \div \frac{\mathbf{5}}{\mathbf{1 2}} \quad \text { The reciprocal of } \frac{5}{12} \text { is } \frac{12}{5} \text {. } \\
& \frac{5}{8} \div \frac{5}{12}=\frac{5}{8} \times \frac{12}{5} \\
& =\frac{60}{40} \text { or } 1 \frac{1}{2} \\
& 2 \quad \mathbf{7} \div \mathbf{3} \frac{\mathbf{1}}{\mathbf{2}} \longrightarrow \frac{\mathbf{7}}{\mathbf{1}} \div \frac{\mathbf{7}}{\mathbf{2}} \quad \text { The reciprocal of } \frac{7}{2} \text { is } \frac{2}{7} \text {. } \\
& 7 \div 3 \frac{1}{2}=\frac{7}{1} \times \frac{2}{7} \\
& =\frac{14}{7} \text { or } 2
\end{aligned}
$$

Name the reciprocal of each number.

1. $\frac{6}{11}$
2. $\frac{14}{5}$
3. 8
4. $\frac{1}{5}$

Divide. Write each quotient in simplest form.
5. $\frac{7}{8} \div \frac{1}{4}$
6. $\frac{2}{5} \div \frac{5}{8}$
7. $\frac{1}{3} \div \frac{1}{6}$
8. $8 \div \frac{1}{3}$
9. $\frac{5}{9} \div 5$
10. $\frac{2}{4} \div 1 \frac{1}{2}$
11. $2 \frac{1}{2} \div 5$
12. $3 \frac{1}{3} \div \frac{2}{9}$
13. $\frac{5}{8} \div 2 \frac{1}{2}$
$\qquad$
$\qquad$

## Dividing Fractions and Mixed Numbers (continued)

Divide. Write each quotient in simplest form.
14. $1 \frac{1}{3} \div 2 \frac{1}{2}$
15. $3 \frac{1}{3} \div 1 \frac{2}{5}$
16. $\frac{9}{10} \div 5 \frac{2}{5}$
17. $\frac{7}{8} \div \frac{2}{3}$
18. $5 \div \frac{3}{5}$
19. $3 \frac{1}{4} \div 2 \frac{1}{3}$

Solve each equation. Write each answer in simplest form.
20. $s=\frac{3}{4} \div \frac{1}{2}$
21. $k=\frac{4}{5} \div \frac{1}{3}$
22. $\frac{1}{5} \div \frac{1}{4}=y$
23. $u=4 \div \frac{1}{3}$
24. $\frac{4}{7} \div \frac{8}{9}=j$
25. $w=\frac{3}{8} \div \frac{3}{4}$
26. $\frac{9}{7} \div 1 \frac{3}{4}=h$
27. $\frac{4}{5} \div \frac{2}{5}=p$
28. $5 \div 3 \frac{3}{4}=q$
29. $c=\frac{3}{8} \div 2 \frac{1}{4}$
$30 t=7 \frac{1}{3} \div 4$
31. $m=3 \frac{1}{4} \div 2 \frac{1}{4}$
32. $n=1 \frac{2}{7} \div 1 \frac{13}{14}$
33. $1 \frac{1}{5} \div \frac{3}{10}=r$
34. $7 \frac{1}{2} \div 2 \frac{5}{6}=w$

## Adding Fractions

To add fractions with like denominators, add the numerators. Write the sum over the common denominator. Simplify the sum if possible.
Example 1 Add: $\frac{7}{\mathbf{8}}+\frac{\mathbf{5}}{\mathbf{8}}$.

$$
\begin{array}{r}
\frac{7}{8} \\
+\frac{5}{8} \\
\hline \frac{12}{8}=\frac{3}{2} \text { or } 1 \frac{1}{2} \quad \text { Simplify the sum } .
\end{array}
$$

To add fractions with unlike denominators, rename the fractions with a common denominator. Then add the fractions.
Example 2 Add: $\frac{1}{9}+\frac{5}{6}$.

$$
\begin{aligned}
& \frac{1}{9}=\frac{2}{18} \quad \text { Use } 18 \text { for the common denominator. } \\
&+\frac{5}{6}=\frac{15}{\frac{18}{18}} \\
&+
\end{aligned}
$$

## Add.

1. $\begin{array}{r}\frac{4}{7} \\ +\frac{2}{7} \\ \hline\end{array}$
2. $\begin{array}{r}\frac{5}{9} \\ +\frac{4}{9} \\ \hline\end{array}$
3. $\begin{array}{r}\frac{11}{15} \\ +\frac{2}{15} \\ \hline\end{array}$
4. $\begin{array}{r}\frac{11}{15} \\ +\frac{7}{15} \\ \hline\end{array}$
5. $\begin{array}{r}\frac{6}{7} \\ +\frac{6}{7} \\ \hline\end{array}$
6. $\frac{11}{12}$
$+\frac{5}{12}$
$\qquad$

## Adding Fractions (continued)

## Add.

7. $\frac{3}{8}$

$$
+\frac{5}{8}
$$

8. $\frac{12}{13}$
$\begin{array}{r}+\frac{14}{13} \\ \hline\end{array}$
9. $\frac{1}{2}$
$\begin{array}{r}+\frac{3}{4} \\ \hline\end{array}$
10. $\frac{1}{8}$
$+\frac{1}{9}$
11. $\frac{1}{3}$ $+\frac{1}{6}$
12. $\frac{3}{5}$ $+\frac{2}{7}$
13. $\frac{7}{16}+\frac{3}{8}$
14. $\frac{7}{10}+\frac{2}{5}$
15. $\frac{3}{14}+\frac{1}{7}$
16. $\frac{5}{12}+\frac{1}{3}$
17. $\frac{1}{6}+\frac{1}{8}$
18. $\frac{1}{6}+\frac{4}{9}$
19. $\frac{3}{8}+\frac{5}{8}+\frac{1}{8}$
20. $\frac{1}{2}+\frac{1}{3}+\frac{1}{4}$
21. $\frac{2}{3}+\frac{3}{4}+\frac{1}{6}$
22. After running $\frac{7}{8}$ mile in a horse race, a horse ran an additional $\frac{3}{8}$ mile to cool down. How far did the horse run altogether?
23. In 1991, about $\frac{1}{5}$ of the crude oil produced was from North America, and about $\frac{2}{7}$ of the crude oil produced was from the Middle East. What fraction of the crude oil produced was from North America or the Middle East?
24. In 1991, about $\frac{3}{10}$ of the petroleum consumed was in North America, and about $\frac{1}{5}$ of the petroleum consumed was in Western Europe. What fraction of the petroleum consumed was in North America or Western Europe?

## Adding Fractions and Mixed Numbers

To add fractions and mixed numbers, first rename each fraction as necessary. Then add the fractions. Next, add the whole numbers. Rename and simplify if necessary.

Example 1 Add: $4 \frac{5}{6}+5 \frac{1}{4}$.

| Step 1 | Step 2 | Step 3 |
| :---: | :---: | :--- |
| $\begin{array}{l}\text { Rename each fraction } \\ \text { by finding the LCD if } \\ \text { necessary. } \\ 4 \frac{5}{6} \longrightarrow 4 \frac{10}{12}\end{array}$ | $\begin{array}{l}\text { Add the fractions. Then } \\ \text { add the whole numbers. } \\ +5 \frac{1}{4}\end{array} \longrightarrow+5 \frac{3}{12}$ |  |\(\left.\quad \begin{array}{l}Rename and simplify <br>


if necessary.\end{array}\right]\)| $4 \frac{13}{12}=10 \frac{1}{12}$ |
| :--- |

Example 2 Add: $14 \frac{5}{9}+7$.

$$
\begin{array}{r}
14 \frac{5}{9} \\
+7 \\
\hline 21 \frac{5}{9}
\end{array}
$$

Add. Write each sum in simplest form.

1. 13

$$
+9 \frac{7}{8}
$$

2. $6 \frac{1}{4}$
$+8 \frac{3}{4}$
3. $5 \frac{1}{6}$
$\begin{array}{r}+7 \frac{1}{3} \\ \hline\end{array}$
4. $11 \frac{3}{4}$
$+8 \frac{2}{3}$
5. $16 \frac{1}{2}$
$\begin{array}{r}14 \frac{5}{7} \\ \hline\end{array}$
6. $15 \frac{1}{2}$
$+9 \frac{4}{5}$
7. $18 \frac{7}{8}$
$+15 \frac{5}{8}$
8. $12 \frac{1}{10}$
$+7 \frac{5}{6}$
$\qquad$
$\qquad$

## Adding Fractions and Mixed Numbers (continued)

Add. Write each sum in simplest form.
9. $18 \frac{7}{8}$
$+13$
10. 11
$+3 \frac{5}{9}$
11. $9 \frac{7}{9}$
$+3 \frac{4}{9}$
12. $8 \frac{2}{5}$
$+4 \frac{4}{5}$
13. $12 \frac{1}{2}$
$+8 \frac{2}{3}$
14. $14 \frac{5}{8}$
$+6 \frac{5}{6}$
15. $16 \frac{2}{5}$
$\begin{array}{r}+13 \frac{3}{4} \\ \hline\end{array}$
16. $13 \frac{4}{15}$
$+12 \frac{3}{5}$
17. $16 \frac{2}{5}$
18. $12 \frac{3}{8}$
$+8 \frac{1}{10}$
$+10 \frac{3}{4}$
19. $\begin{array}{r}4 \frac{4}{9} \\ +5 \frac{5}{12} \\ \hline\end{array}$
20. $18 \frac{2}{3}$
$+12 \frac{8}{9}$
21. $10 \frac{6}{7}$
$+5 \frac{2}{5}$
22. $15 \frac{3}{4}$
$+8 \frac{5}{8}$
23. $24 \frac{1}{2}$
$+12 \frac{3}{4}$
24. $20 \frac{2}{9}$
$+8 \frac{1}{12}$
25. $8 \frac{2}{11}+6 \frac{1}{2}=$
26. $9 \frac{5}{9}+10 \frac{5}{12}=$
27. $6 \frac{4}{9}+8 \frac{7}{15}=$
28. $12 \frac{4}{15}+5 \frac{7}{12}=$
29. $14 \frac{4}{9}+10 \frac{2}{3}=$
30. $19 \frac{2}{7}+12 \frac{5}{21}=$

## Subtracting Fractions

To subtract fractions with like denominators, subtract the numerators.
Write the difference over the common denominator. Simplify the difference if possible.
Example 1 Subtract: $\frac{3}{4}-\frac{1}{4}$.

| Step 1 | Step 2 |
| :---: | :---: |
| Subtract the numerators. Write the <br> difference over the like denominator. | Simplify the difference. |
| $\frac{3}{4}-\frac{1}{4}=\frac{3-1}{4}$ or $\frac{2}{4}$ | $\frac{2}{4}=2$ |
|  | The GCF of 2 and 4 is 2. |

To subtract fractions with unlike denominators, rename the fractions with a common denominator. Then subtract the fractions.
Example 2 Subtract: $\frac{7}{10}-\frac{2}{5}$.

$$
\begin{aligned}
& \frac{7}{10}=\frac{7}{10} \quad \text { Use } 10 \text { for the common denominator. } \\
&-\frac{2}{5}=\frac{4}{\frac{10}{3}} \\
& \frac{10}{10}
\end{aligned}
$$

Subtract. Write each difference in simplest form.

1. $\frac{5}{6}-\frac{4}{6}$
2. $\frac{9}{10}-\frac{3}{10}$
3. $\frac{9}{16}-\frac{3}{16}$
4. $\frac{11}{12}-\frac{3}{12}$
$\qquad$

## Subtracting Fractions (continued)

## Subtract. Write each difference in simplest form.

5. $\frac{11}{14}-\frac{5}{14}$
6. $\frac{8}{9}-\frac{2}{9}$
7. $\frac{5}{6}-\frac{1}{3}$
8. $\frac{11}{12}-\frac{3}{4}$
9. $\frac{9}{10}-\frac{2}{5}$
10. $\frac{5}{7}-\frac{3}{14}$
11. $\frac{20}{21}-\frac{5}{14}$
12. $\frac{9}{14}-\frac{1}{2}$
13. $\frac{11}{15}-\frac{3}{10}$
14. $\frac{5}{6}-\frac{1}{12}$
15. $\frac{7}{18}-\frac{1}{6}$
16. $\frac{9}{20}-\frac{1}{8}$
17. $\frac{7}{12}-\frac{2}{9}$
18. $\frac{13}{18}-\frac{5}{12}$
19. $\frac{9}{16}-\frac{1}{6}$
20. $\frac{17}{24}-\frac{3}{10}$

## Subtracting Fractions and Mixed Numbers

To subtract fractions and mixed numbers, first rename each fraction by finding the LCD if necessary. Then rename, if necessary, to subtract. Next subtract the fractions and then the whole numbers. Rename and simplify if necessary.

## Example 1 Find $4 \frac{\mathbf{2}}{5}-1 \frac{9}{10}$.

| Step 1 | Step 2 | Step 3 |
| :---: | :---: | :---: |
| Rename each fraction finding the LCD if necessary. $\begin{array}{r} 4 \frac{2}{5} \rightarrow 4 \frac{4}{10} \\ -1 \frac{9}{10} \rightarrow-1 \frac{9}{10} \\ \hline \end{array}$ | Rename if necessary to subtract. $\begin{aligned} & 4 \frac{4}{10}=3+\frac{10}{10}+\frac{4}{10} \\ &=3 \frac{14}{10} \\ & 4 \frac{4}{10} \rightarrow 3 \frac{14}{10} \\ &-1 \frac{9}{10} \rightarrow-1 \frac{9}{10} \\ & \hline \end{aligned}$ | Subtract and simplify if necessary. $\begin{array}{r} 3 \frac{14}{10} \\ -1 \frac{9}{10} \\ \hline 2 \frac{5}{10} \text { or } 2 \frac{1}{2} \end{array}$ |

Example 2 Find 6-3 $\frac{1}{6}$.

$$
\begin{aligned}
6 & \rightarrow \\
-3 \frac{1}{6} & \rightarrow \frac{-3 \frac{6}{6}}{2 \frac{5}{6}}
\end{aligned}
$$

Subtract. Write each difference in simplest form.

1. $14 \frac{2}{3}$
$-12$
2. 10
$-4 \frac{3}{4}$
3. $7 \frac{7}{9}$
$-3 \frac{4}{9}$
4. $8 \frac{1}{3}$
$-4 \frac{2}{3}$
5. $15 \frac{1}{4}$
$-5 \frac{1}{2}$
6. $\begin{array}{r}16 \frac{3}{8} \\ -2 \frac{5}{6} \\ \hline\end{array}$
7. $14 \frac{3}{7}$
8. $18 \frac{3}{10}$
$-10 \frac{1}{2}$
$-7 \frac{4}{5}$
$\qquad$

## Subtracting Fractions and Mixed Numbers (continued)

## Subtract. Write each difference in simplest form.

9. $8 \frac{1}{5}$
$-2 \frac{3}{5}$
10. 6
$-3 \frac{2}{7}$
11. $9 \frac{5}{12}$
$-3 \frac{3}{4}$
12. $16 \frac{2}{9}$
$-2 \frac{2}{3}$
13. $23 \frac{1}{2}$
$-15 \frac{1}{4}$
14. $13 \frac{2}{15}$
$-8 \frac{1}{5}$
15. $16 \frac{3}{8}$
$-14 \frac{3}{4}$
16. $19 \frac{1}{6}$
$-4 \frac{2}{3}$
17. $9 \frac{2}{9}$
$-1 \frac{1}{18}$
18. 7
$-2 \frac{4}{7}$
19. $16 \frac{3}{4}$
$-5 \frac{11}{12}$
20. $12 \frac{1}{3}$
$-10 \frac{3}{4}$
21. $\begin{array}{r}26 \frac{1}{4} \\ -15 \frac{3}{5} \\ \hline\end{array}$
22. $14 \frac{1}{9}$
$-8 \frac{2}{3}$
23. $6 \frac{3}{11}-5 \frac{1}{3}$
24. $8 \frac{2}{9}-1 \frac{7}{12}$
25. $14 \frac{3}{10}-6 \frac{4}{5}$
26. $12 \frac{5}{6}-10 \frac{2}{3}$
$\qquad$

## Changing Fractions to Decimals

A fraction is another way of writing a division problem. To change a fraction to a decimal, divide the numerator by the denominator.

Examples 1 About $\frac{1}{20}$ of the heat in a house is lost through the doors. Write this fraction as a decimal.
$\frac{1}{20}$ means $1 \div 20$ or $20 \sqrt{1}$.
0.05
$2 0 \longdiv { 1 . 0 0 }$

So, $\frac{1}{20}=0.05$.

2 Express $\frac{1}{3}$ as a decimal.

$$
\begin{aligned}
& 3 \longdiv { 0 . 3 3 \ldots } \\
& \frac{1}{3}=0.33 \ldots \text { or } 0 . \overline{3} \quad \text { The bar status shows that } 3 \text { repeats. }
\end{aligned}
$$

Express each fraction as a decimal. Use bar notation if necessary.

1. $\frac{4}{25}$
2. $\frac{3}{5}$
3. $\frac{7}{20}$
4. $\frac{3}{50}$
5. $\frac{9}{10}$
6. $\frac{7}{8}$
7. $\frac{1}{3}$
8. $\frac{14}{16}$
9. $\frac{20}{30}$
10. $\frac{5}{9}$
11. $\frac{19}{20}$
12. $\frac{5}{200}$
$\qquad$

## Changing Fractions to Decimals (continued)

## Express each fraction as a decimal. Use bar notation if necessary.

13. $\frac{10}{50}$
14. $\frac{13}{20}$
15. $\frac{5}{6}$
16. $\frac{4}{5}$
17. $\frac{7}{10}$
18. $\frac{13}{40}$
19. $\frac{39}{50}$
20. $\frac{2}{25}$
21. $\frac{7}{16}$
22. $\frac{34}{125}$
23. $\frac{16}{25}$
24. $\frac{99}{100}$
25. $\frac{17}{20}$
26. $\frac{3}{150}$
27. $\frac{3}{8}$
28. $\frac{2}{3}$

A mill is a unit of money that is used in assessing taxes.
One mill is equal to $\frac{1}{10}$ of a cent or $\frac{1}{1000}$ of a dollar.
29. Money is usually written using decimals. Express each fraction above as a decimal using the correct money symbol.
30. Find the number of cents and the number of dollars equal to 375 mills.
31. Find the number of cents and the number of dollars equal to 775 mills.
32. Find the number of cents and the number of dollars equal to 1,000 mills.

## Writing Decimals as Fractions

To write a terminating decimal as a fraction, write the digits to the right of the decimal point over a power of ten. The power of ten is determined by the place-value position of the last digit in the decimal. For example, if the last digit is in the hundredths place, use 100. If the last digit is in the thousandths place, use 1000 .

## Example $1 \quad$ Write 0.375 as a fraction.

Since the last digit, 5 , is in the thousandths place, write
375 over 1000. Then simplify.

$$
0.375=\frac{375}{1000} \text { or } \frac{3}{8}
$$

Repeating decimals can also be written as fractions using the method shown below.

## Example 2 Write $0.555 \ldots$ as a fraction.

Let $N=0.555 \ldots$ Then $10 N=5.555 \ldots$.
Subtract $N$ from $10 N$ to eliminate the repeating part.

$$
\begin{aligned}
& 10 N=5.555 \ldots \\
&-N=0.555 \ldots \\
& \hline 9 N=5 \\
& N=\frac{5}{9} \\
& \text { So, } 0.555 \ldots=\frac{5}{9}
\end{aligned}
$$

Write each decimal as a fraction.

1. 0.525
2. 0.45
3. $0.333 \ldots$
4. 0.43
5. 0.8
6. $0.1212 \ldots$
7. 0.345
8. 0.1862
9. $0.4555 \ldots$
$\qquad$

## Writing Decimals as Fractions (continued)

Write each decimal as a fraction.
10. 0.456
11. 0.32
12. $0.222 \ldots$
13. 0.35
14. 0.48
15. 0.955
16. $0.8222 \ldots$
17. $0.4545 \ldots$
18. $0.444 \ldots$
19. 0.565
20. 0.435
21. 0.552
22. 0.855
23. 0.842
24. 0.944
25. 0.732
26. 0.245
27. 0.485
28. $0.666 \ldots$
29. $0.8585 \ldots$
30. 0.9655

## Writing Decimals as Percents

To express a decimal as a percent, first express the decimal as a fraction with a denominator of 100 . Then express the fraction as a percent.

Examples Express each decimal as a percent.

$$
1 \begin{array}{rlrl}
\mathbf{0 . 0 9}=\frac{9}{100} & 2 & \mathbf{0 . 0 0 5} & =\frac{5}{1000} \\
& =\frac{0.5}{100} & \mathbf{1 . 8} & =\frac{18}{10} \\
& =9 \% & & =\frac{180}{100} \\
& =0.5 \% & & =180 \%
\end{array}
$$

A shortcut to writing a decimal as a percent is to move the decimal point two places to the right and add a percent sign (\%).

Examples Express each decimal as a percent.
$4 \quad 0.25$
50.9

$$
\begin{aligned}
0.25 & =0.25 \% \\
& =25 \%
\end{aligned}
$$

$$
\begin{aligned}
0.9 & =0.90 \% \\
& =90 \%
\end{aligned}
$$

## Express each decimal as a percent.

1. 0.66
2. 0.08
3. 0.75
4. 0.001
5. 1.19
6. 0.72
7. 0.136
8. 4.02
9. 0.36
10. 0.18
11. 0.09
12. 0.2
13. 0.625
14. 0.007
15. 1.4
16. 0.093
$\qquad$

## Writing Decimals as Percents (continued)

## Express each decimal as a percent.

17. 0.8
18. 0.54
19. 3.75
20. 0.02
21. 0.258
22. 0.016
23. 0.49
24. 0.003
25. 0.96
26. 0.52
27. 0.15
28. 0.008
29. 3.62
30. 0.623
31. 0.035
32. 7.08
33. 0.5
34. 0.97
35. 0.6
36. 0.425
37. 0.08
38. 2.5
39. 0.001
40. 0.074
41. 0.345
42. 0.19
43. 0.062
44. 0.19
45. 0.005
46. 0.37
47. 0.8
48. 0.04
$\qquad$
$\qquad$

## Writing Percents as Decimals

To express a percent as a decimal, divide by 100 and write as a decimal.
Examples Express each percent as a decimal.

$$
1 \mathbf{5 6 \%} \quad \begin{aligned}
\mathbf{3 . 4 \%} & \\
56 \% & =\frac{56}{100} \\
=0.56 & \begin{aligned}
3.4 \% & =\frac{3.4}{100} \\
& =\frac{34}{1000} \\
&
\end{aligned} \\
&
\end{aligned}
$$

A shortcut to writing a percent as a decimal is to move the decimal point two places to the left and drop the percent sign.

## Examples Express each percent as a decimal.

$318 \%$

$$
\begin{aligned}
18 \% & =\underbrace{18}_{0} \\
& =0.18
\end{aligned}
$$

4 0.5\%

$$
0.5 \%=000.5
$$

$$
=0.005
$$

## Express each percent as a decimal.

1. $45 \%$
2. $91 \%$
3. $24.5 \%$
4. $8.37 \%$
5. $13 \%$
6. $6 \%$
7. $76.5 \%$
8. $1.22 \%$
9. $14.5 \%$
10. $26 \%$
11. $1.8 \%$
12. $80 \%$
$\qquad$

## Writing Percents as Decimals (continued)

## Express each percent as a decimal.

13. $8 \%$
14. $32 \%$
15. $15 \%$
16. $15.7 \%$
17. $16.23 \%$
18. $2.01 \%$
19. $3.2 \%$
20. $80 \%$
21. $1.32 \%$
22. $21 \%$
23. $25 \%$
24. $13 \%$
25. $4 \%$
26. $40 \%$
27. $62.5 \%$
28. $30 \%$
29. $60.3 \%$
30. $12.3 \%$
31. $10.25 \%$
32. $8.6 \%$
33. $12.15 \%$
34. $102 \%$
35. $450.5 \%$
36. $175 \%$
37. $0.05 \%$
38. $0.25 \%$
39. $0.105 \%$
40. $14.36 \%$
41. $2.18 \%$
42. $38.65 \%$
$\qquad$
$\qquad$
$\qquad$

## Writing Fractions as Percents

To express a fraction as a percent, first set up a proportion. Then solve the proportion using cross products.

Example Express $\frac{13}{20}$ as a percent.

$$
\begin{aligned}
\frac{13}{20} & =\frac{k}{100} & & \text { Set up a proportion. } \\
13 \times 100 & =20 \times k & & \text { Find the cross products. } \\
1300 & =20 k & & \\
1300 \div 20 & =20 k \div 20 & & \text { Divide each side by } 20 . \\
65 & =k & & \\
\frac{13}{20} & =\frac{65}{100} \text { or } 65 \% & &
\end{aligned}
$$

Express each shaded section as a fraction and as a percent.
1.

2.

3.

4.

5.

6.


Express each fraction as a percent.
7. $\frac{17}{100}$
8. $\frac{4}{5}$
9. $\frac{1}{4}$
10. $\frac{8}{20}$
11. $\frac{1}{50}$
12. $\frac{7}{10}$
13. $\frac{6}{25}$
14. $\frac{1}{10}$
15. $\frac{1}{25}$
16. $\frac{1}{5}$
17. $\frac{6}{50}$
18. $\frac{8}{10}$
19. $\frac{12}{5}$
20. $\frac{15}{20}$
21. $\frac{150}{50}$
22. $\frac{19}{20}$
$\qquad$
$\qquad$

## Writing Fractions as Percents (continued)

Use a $10 \times 10$ grid to shade the amount stated in each fraction. Then express each fraction as a percent.
23. $\frac{1}{10}$

24. $\frac{1}{20}$

25. $\frac{1}{50}$


Express each fraction as a percent.
26. $\frac{47}{100}$
27. $\frac{8}{25}$
28. $\frac{9}{12}$
29. $\frac{13}{50}$
30. $\frac{11}{20}$
31. $\frac{7}{5}$
32. $\frac{3}{100}$
33. $\frac{21}{25}$
34. $\frac{3}{10}$
35. $\frac{3}{20}$
36. $\frac{31}{50}$
37. $\frac{5}{4}$
38. $\frac{6}{10}$
39. $\frac{15}{5}$
40. $\frac{12}{50}$
41. $\frac{1}{20}$
42. $\frac{17}{20}$
43. $\frac{152}{50}$
44. $\frac{400}{100}$
45. $\frac{30}{25}$
46. $\frac{9}{10}$
47. $\frac{49}{50}$
48. $\frac{24}{25}$
49. $\frac{40}{20}$
50. $\frac{5}{15}$
51. $\frac{12}{20}$
52. $\frac{18}{10}$
53. $\frac{1000}{100}$
54. $\frac{13}{20}$
55. $\frac{215}{50}$
56. $\frac{25}{20}$
57. $\frac{8}{5}$
58. $\frac{16}{10}$
59. $\frac{43}{50}$
60. $\frac{75}{25}$
61. $\frac{22}{20}$

## Writing Percents as Fractions

To express a percent as a fraction, divide by 100 and simplify.
Examples Express each percent as a fraction.

$$
\begin{aligned}
& 1 \text { 65\% } \\
& 65 \%=\frac{65}{100} \\
& =\frac{13}{20} \\
& 2 \text { 2.5\% } \\
& 2.5 \%=\frac{2.5}{100} \\
& =\frac{25}{1000} \\
& =\frac{1}{40}
\end{aligned}
$$

## Express each percent as a fraction.

1. $45 \%$
2. $91 \%$
3. $24.5 \%$
4. $8 \%$
5. $32 \%$
6. $15 \%$
7. $15.7 \%$
8. $16.23 \%$
9. $2.01 \%$
10. $3.2 \%$
11. $80 \%$
12. $1.32 \%$
13. $21 \%$
14. $25 \%$
15. $13 \%$
$\qquad$

## Writing Percents as Fractions (continued)

## Express each percent as a fraction.

16. $4 \%$
17. $40 \%$
18. $62.5 \%$
19. $30 \%$
20. $60.3 \%$
21. $12.3 \%$
22.15\%
22. $32 \%$
23. $67 \%$
24. $62.8 \%$
25. $18 \%$
26. $23 \%$
27. $70 \%$
28. $1.5 \%$
29. $3.2 \%$
30. $1.82 \%$
31. $14.8 \%$
32. $16 \%$
33. $120 \%$
34. $18.5 \%$
35. $255 \%$
36. $100.5 \%$
37. $1.255 \%$
38. $6.8 \%$
39. $0.09 \%$
40. $45.45 \%$
41. $50.15 \%$

## Comparing and Ordering Rational Numbers

To compare fractions, write each fraction as a decimal.
Then compare the decimals.
$\begin{array}{ll}\text { Example } \quad 1 \quad \text { Compare } \frac{\mathbf{2}}{\mathbf{3}} \text { and } \frac{\mathbf{3}}{5} . \\ & \frac{2}{3}=0.6666666667 \\ & \frac{3}{5}=0.6 \\ & \text { Since } 0.6666666667>0.6, \frac{2}{3}>\frac{3}{5} .\end{array}$

To compare percents, compare the numbers without the percent sign.
Example 2 Compare 15\% and 17.5\%.
Since $15<17.5,15 \%<17.5 \%$.

Fill in each $\square$ with $<,>$, or $=$ to make a true sentence.

1. $\frac{2}{7} \bigcirc \frac{3}{8}$
2. $\frac{3}{11} \circlearrowleft \frac{1}{5}$
3. $\frac{11}{21} \bigcirc \frac{9}{16}$
4. $\frac{14}{21} \bigcirc \frac{10}{15}$
5. $\frac{25}{27} \bigcirc \frac{17}{19}$
6. $\frac{3}{10}$

7. $1 \frac{7}{8} \bigcirc 2 \frac{4}{5}$
8. $3 \frac{7}{9} \bigcirc 3 \frac{6}{7}$
9. $5 \frac{10}{19} \bigcirc 5 \frac{15}{24}$
10. $14 \%$
 $12.5 \%$
11. $5 \%$

12. $0.04 \%$
 $0.25 \%$
13. $250 \%$
 $126 \%$
14. $16.6 \%$
 $10 \%$
15. $75.8 \%$
 $75.9 \%$
$\qquad$

## Comparing and Ordering Rational Numbers (continued)

Write each set of fractions in order from least to greatest.
16. $\frac{3}{5}, \frac{7}{9}, \frac{4}{5}, \frac{1}{2}$
17. $\frac{3}{8}, \frac{2}{7}, \frac{8}{11}, \frac{5}{16}$
18. $\frac{9}{14}, \frac{6}{7}, \frac{3}{4}, \frac{12}{19}$
19. $\frac{11}{23}, \frac{19}{27}, \frac{7}{10}, \frac{15}{17}$

The Pittsburgh Pirates have won 14 out of 21 games, and the New York Mets have won 15 out of 23 games. Use this information to answer Exercises 20-23.
20. Which team has the better record?
21. Suppose the Pirates win 2 of their next three games and the Mets win all of their next 3 games. Which team has the better record?
22. Suppose the Pirates went on to win 21 games after playing 30 games. Is their record better now than it was before? Explain.
23. Suppose the Mets went on to win 16 games after playing 30 games. Is their record better now than it was before? Explain.
24. Larry has $\frac{5}{6}$ yard of material. Does he have enough to make a vest that requires $\frac{3}{4}$ yard of material? Explain.
$\qquad$

## Length in the Customary System

| Length |
| :--- |
| 1 foot $(\mathrm{ft})=12$ inches (in.) |
| 1 yard $(\mathrm{yd})=3$ feet or 36 inches |
| 1 mile $(\mathrm{mi})=5280$ feet or 1760 yards |

Example 1 Draw a line segment measuring $3 \frac{3}{8}$ inches.
Use a ruler divided in eighths.
Find $3 \frac{3}{8}$ on the ruler.


Draw the line segment from 0 to $3 \frac{3}{8}$.
To change from a smaller unit to a larger unit, divide.
To change from a larger unit to a smaller unit, multiply.
Examples

$$
\begin{array}{ll}
2 & \mathbf{3 f t}= \\
& 3 \times 12=36 \\
& 3 \mathrm{ft}=36 \mathrm{in} . \\
\mathbf{3} & \mathbf{9 f t}= \\
& 9 \div 3=3 \\
& 9 \mathrm{ft}=3 \mathrm{yd}
\end{array}
$$

$\qquad$ in. $\quad 1 f t=12$ in., so multiply by 12.
$\qquad$ yd $\quad 1 y d=3 f t$, so divide by 3 .

## Draw a line segment of each length.

1. $1 \frac{1}{2}$ inches
2. $1 \frac{1}{8}$ inches
3. $1 \frac{1}{4}$ inches
4. $\frac{3}{4}$ inch
5. $1 \frac{3}{8}$ inches
6. $1 \frac{5}{8}$ inches
7. $3 \frac{1}{2}$ inches
8. $\frac{3}{8}$ inch
9. $1 \frac{3}{4}$ inches
10. $2 \frac{1}{4}$ inches
11. $2 \frac{5}{8}$ inches
12. $3 \frac{1}{8}$ inches
$\qquad$

## Length in the <br> Customary System (continued)

## Complete.

13. $5 \mathrm{ft}=$ $\qquad$ in.
14. $2 \mathrm{mi}=$ $\qquad$ ft
15. $12 \mathrm{yd}=\ldots \mathrm{ft}$
16. 24 in . $=$ $\qquad$ yd
17. 48 in. $=$ $\qquad$ ft
18. $3520 \mathrm{yd}=$ $\qquad$ mi
19. 72 in. $=$ $\qquad$ yd
20. 30 in. $=$ $\qquad$ ft
21. $4 \mathrm{mi}=$ $\qquad$ ft
22. 90 in. $=$ $\qquad$ yd
23. 60 in. $=$ $\qquad$ yd
24. $6 \mathrm{mi}=$ $\qquad$ yd
25. $6.5 \mathrm{ft}=$ $\qquad$ in.
26. $15 \mathrm{ft}=$ $\qquad$ yd
27. $9 \mathrm{yd}=$ $\qquad$ in.
28. $12 \mathrm{ft}=$ $\qquad$ in.
$\qquad$ mi in.

## Capacity in the Customary System

| Capacity |
| :---: |
| 1 cup $(\mathrm{c})=8$ fluid ounces (fl oz) |
| 1 pint $(\mathrm{pt})=2$ cups |
| 1 quart $(\mathrm{qt})=2$ pints |
| 1 gallon (gal) $=4$ quarts |

To change from one customary unit of capacity to another, you either multiply or divide. When changing from a smaller unit to a larger unit, divide.
When changing from a larger unit to a smaller unit, multiply.

Examples 112 qt $=\longrightarrow$ pt

$$
12 \times 2=24
$$

$$
12 \mathrm{qt}=24 \mathrm{pt}
$$

$28 \mathrm{pt}=$ $\qquad$ gal
$8 \div 2=4$
$4 \div 4=1$
$8 \mathrm{pt}=1 \mathrm{gal}$

You are changing from a larger unit (qt) to a smaller unit (pt), so multiply.

Since $1 q t=2 p t$, multiply by 2.

You are changing from a smaller unit (pt) to a larger unit (gal), so divide.
Divide by 2 to change pints to quarts.
Divide by 4 to change quarts to gallons.

## Complete.

1. $8 \mathrm{c}=$ $\qquad$ fl oz
2. $8 \mathrm{qt}=$ $\qquad$ gal
3. $16 \mathrm{pt}=$ $\qquad$ qt
4. $5 \mathrm{c}=$ $\qquad$ pt
5. $16 \mathrm{qt}=$ $\qquad$ pt
6. $18 \mathrm{c}=$ $\qquad$ qt
7. $8 \mathrm{gal}=$ $\qquad$
8. $16 \mathrm{gal}=$ $\qquad$ qt
$\qquad$

## Capacity in the Customary System (continued)

Complete.
9. $16 \mathrm{fl} \mathrm{oz}=$ $\qquad$ c
11. $3 \mathrm{qt}=$ $\qquad$ pt
13. $15 \mathrm{pt}=$ $\qquad$ qt
15. $16 \mathrm{c}=$ $\qquad$ fl oz
17. $3 \mathrm{qt}=$ $\qquad$ c
19. $64 \mathrm{pt}=$ $\qquad$ gal
21. $1 \mathrm{qt}=$ $\qquad$ fl oz
23. $17 \mathrm{c}=$ $\qquad$ pt
25. $2.5 \mathrm{gal}=$ $\qquad$ qt
27. $16 \mathrm{qt}=$ $\qquad$ gal
29. $16 \mathrm{qt}=$ $\qquad$ c
31. A recipe calls for 3 cups of milk How many fluid ounces of milk are need for the recipe?
10. $16 \mathrm{pt}=$ $\qquad$ c
12. $5 \mathrm{gal}=$ $\qquad$
14. $12 \mathrm{pt}=$ $\qquad$ c
16. $10 \mathrm{pt}=$ $\qquad$ qt
18. $12 \mathrm{c}=$ $\qquad$ fl oz
20. $4 \mathrm{gal}=$ $\qquad$ c
22. $5 \mathrm{c}=$ $\qquad$ fl oz
24. $6 \mathrm{qt}=$ $\qquad$ gal
26. $3 \frac{1}{2} \mathrm{gal}=$ $\qquad$
28. $80 \mathrm{fl} \mathrm{oz}=$ $\qquad$
30. $8 \mathrm{c}=$ $\qquad$ qt
32. Jenna bought 64 fl oz of juice. How many quarts of juice did she buy?
$\qquad$

## Weight in the <br> Customary System

| Weight |
| :---: |
| 1 pound $(\mathrm{lb})=16$ ounces (oz) |
| 1 ton $(T)=2000$ pounds |

To change from one customary unit of weight to another, you either multiply or divide.
When changing from a smaller unit to a larger unit, divide.
When changing from a larger unit to a smaller unit, multiply.

Examples $1 \mathbf{1 0} \frac{\mathbf{1}}{\mathbf{2}} \mathbf{l b}=\ldots \quad \mathbf{o z} \quad$ You are changing from a larger unit (lb) to a smaller unit (oz), so multiply.
$10 \frac{1}{2} \times 16=\frac{21}{2} \times \frac{16^{8}}{1}=\frac{168}{1}$ or $168 \quad \begin{aligned} & \text { Since } 1 \text { pound }=16 \text { ounces, } \text { multiply } \\ & \text { by } 16 .\end{aligned}$
$10 \frac{1}{2} \mathrm{lb}=168 \mathrm{oz}$
$2 \mathbf{3 2 ~ o z}=\ldots \mathbf{~ l b} \quad$ You are changing from a smaller unit (oz) to a larger unit (lb), so divide.
$32 \div 16=2$
Divide by 16 to change ounces to pounds.
$32 \mathrm{oz}=2 \mathrm{lb}$

## Complete.

1. $2 \mathrm{~T}=$ $\qquad$ lb
$\qquad$
2. $8500 \mathrm{lb}=$ T
3. $24 \mathrm{oz}=$ $\qquad$ lb
4. $4 \mathrm{lb}=$ $\qquad$ oz
5. $3 \frac{1}{2} \mathrm{lb}=\square \mathrm{oz}$
6. $2500 \mathrm{lb}=$ $\qquad$ T
7. $10 \mathrm{lb}=$ $\qquad$ oz
8. $1 \mathrm{~T}=$ $\qquad$ oz

## Weight in the <br> Customary System (continued)

## Complete.

9. $256 \mathrm{oz}=$ $\qquad$ lb
10. $3 \mathrm{~T}=$ $\qquad$ lb
11. $12,000 \mathrm{lb}=$ $\qquad$ T
12. $16 \mathrm{~T}=$ $\qquad$ lb
13. $3 \mathrm{lb}=$ $\qquad$ oz
14. $64 \mathrm{oz}=$ $\qquad$ lb
15. $2.5 \mathrm{~T}=$ $\qquad$ lb
16. $17 \mathrm{oz}=$ $\qquad$ lb
17. $\frac{1}{5} \mathrm{~T}=$ $\qquad$ lb
18. $6.5 \mathrm{~T}=$ $\qquad$ lb
19. $20 \mathrm{lb}=$ $\qquad$ oz
20. A recipe calls for 3 ounces of butter How many pounds of butter are needed for the recipe?
21. $10 \mathrm{~T}=$ $\qquad$ oz
22. $16 \mathrm{lb}=$ $\qquad$ oz
23. $7 \mathrm{~T}=$ $\qquad$ lb
24. $12 \mathrm{oz}=$ $\qquad$ lb
25. $12 \mathrm{oz}=$ $\qquad$ lb
26. $4 \mathrm{oz}=$ $\qquad$ lb
27. $5 \mathrm{lb}=$ $\qquad$ oz
28. $6 \mathrm{oz}=$ $\qquad$ lb
29. $3 \frac{1}{2} \mathrm{~T}=$ $\qquad$ oz
30. $500 \mathrm{lb}=$ $\qquad$ T
31. $2.25 \mathrm{~T}=$ $\qquad$ lb
32. Jenna bought 64 ounces of bananas. How many pounds of bananas did she buy?

## Length in the Metric System

| Length |
| :---: |
| 1 centimeter $(\mathrm{cm})=10$ millimeters $(\mathrm{mm})$ |
| 1 meter $(\mathrm{m})=100$ centimeters |
| 1 meter $=1000$ millimeters |
| 1 kilometer $(\mathrm{km})=1000$ meters |

To change from one metric unit of length to another, you either multiply or divide.
When changing from a smaller unit to a larger unit, divide.
When changing from a larger unit to a smaller unit, multiply.

| Examples 1 | $\mathbf{3 m}=\square \mathbf{m m}$ | You are changing from a larger unit (m) to a smaller unit (mm), so multiply. |
| :---: | :---: | :---: |
|  | $3 \times 1000=3000$ | Since $1 \mathrm{~m}=1000 \mathrm{~mm}$, multiply by 1000. Move the decimal point 3 places to the right. |
|  | $3 \mathrm{~m}=3000 \mathrm{~mm}$ |  |
| 2 | $5000 \mathrm{~m}=\ldots \mathrm{km}$ | You are changing from a smaller unit (m) to a larger unit (km), so divide. |
|  | $5000 \div 1000=5.000$ | Since 1000 meters $=1$ kilometer, divide by 1000. Move the decimal point 3 places to the left. |
|  | $5000 \mathrm{~m}=5 \mathrm{~km}$ |  |

## Complete.

1. $300 \mathrm{~mm}=$ $\qquad$ cm
2. $2000 \mathrm{~m}=$ $\qquad$ km
3. $60 \mathrm{~cm}=$ $\qquad$ m
4. $1500 \mathrm{~m}=$ $\qquad$ km
5. $6 \mathrm{~km}=$ $\qquad$ m
6. $8 \mathrm{~km}=$ $\qquad$ cm
7. $80 \mathrm{~mm}=$ $\qquad$ cm $\qquad$ m
$\qquad$
$\qquad$

## Length In the <br> Metric System (continued)

## Complete.

9. $2000 \mathrm{~mm}=$ $\qquad$ cm
10. $300 \mathrm{~mm}=$ $\qquad$ cm
11. $160 \mathrm{~cm}=$ $\qquad$ mm
12. $3000 \mathrm{~cm}=$ $\qquad$ m
13. $2000 \mathrm{~km}=$ $\qquad$ m
14. $4100 \mathrm{~cm}=$ $\qquad$ m
15. $42,000 \mathrm{~m}=$ $\qquad$ km
$\qquad$
16. $8 \mathrm{~m}=$ cm
17. $16.3 \mathrm{~mm}=$ $\qquad$ cm
18. $15.5 \mathrm{~cm}=$ $\qquad$ mm
19. A napkin is 37 centimeters long. How many millimeters is this?
20. $2 \mathrm{~m}=$ $\qquad$ cm
21. $7 \mathrm{~cm}=$ $\qquad$ mm
22. $20 \mathrm{~km}=$ $\qquad$ m
23. $24,000 \mathrm{~mm}=$ $\qquad$ m
24. $42 \mathrm{~cm}=$ $\qquad$ mm
25. $8700 \mathrm{~cm}=$ $\qquad$ m
26. $4 \mathrm{~km}=$ $\qquad$ m
$\qquad$ mm
27. $4.1 \mathrm{~km}=$ $\qquad$ m
28. $160 \mathrm{~km}=$ $\qquad$ m
29. A race is 80,000 meters long. How long is the race in kilometers?

## Capacity in the Metric System

| Capacity |
| :---: |
| 1 liter $(\mathrm{L})=1000$ milliliters $(\mathrm{mL})$ |
| 1 kiloliter $(k L)=1000$ liters |

To change from one metric unit of capacity to another, you either multiply or divide.
When changing from a smaller unit to a larger unit, divide.
When changing from a larger unit to a smaller unit, multiply.

| Examples | 1 | $1325 \mathrm{~mL}=\ldots \mathrm{L}$ | You are changing from a smaller unit (mL) to a larger unit (L), so divide. |
| :---: | :---: | :---: | :---: |
|  |  | $1325 \div 1000=1.325$ | Since $1 m L=1000$ L, divide by 1000 . Move the decimal point 3 places to the left. |
|  |  | $1325 \mathrm{~mL}=1.325 \mathrm{~L}$ |  |
|  | 2 | $2 \mathrm{~kL}=\ldots \mathrm{L}$ | You are changing from a larger unit ( $k L$ ) to a smaller unit (L), so multiply. |
|  |  | $2 \times 1000=\underbrace{2000}_{200}$ | Since $1 \mathrm{~kL}=1000$ L, multiply by 1000. Move the decimal point 3 places to the right. |
|  |  | $2 \mathrm{~kL}=2000 \mathrm{~L}$ |  |

## Complete.

1. $76 \mathrm{~mL}=$ $\qquad$ L
2. $1800 \mathrm{~L}=$ $\qquad$ kL

$$
\text { 3. } 140 \mathrm{~L}=\square \mathrm{mL}
$$

4. $7500 \mathrm{~L}=$ $\qquad$ mL
5. $8.2 \mathrm{~kL}=$ $\qquad$
6. $140 \mathrm{~L}=$ $\qquad$ kL
7. $6000 \mathrm{~mL}=$ $\qquad$ L
8. $400 \mathrm{~kL}=$ $\qquad$ L
$\qquad$

## Capacity in the Metric System (continued)

## Complete.

9. $5 \mathrm{~kL}=$ $\qquad$ L
10. $4 \mathrm{~L}=$ $\qquad$ mL
11. $3250 \mathrm{~mL}=$ $\qquad$ L
12. $750 \mathrm{~L}=$ $\qquad$ kL
13. $12 \mathrm{~L}=$ $\qquad$ mL
$\qquad$ L
14. $36 \mathrm{~kL}=$ $\qquad$ L
15. $2.4 \mathrm{~L}=$ $\qquad$ mL
16. $5.35 \mathrm{~L}=$ $\qquad$ mL
17. $180 \mathrm{~L}=$ $\qquad$ kL
18. Karen uses 2 L of liquid in her punch recipe. How many mL does she use?
19. $940 \mathrm{~mL}=$ $\qquad$ L
20. $850 \mathrm{~L}=$ $\qquad$ kL
21. $2000 \mathrm{~L}=$ $\qquad$ kL
22. $1400 \mathrm{~L}=$ $\qquad$ kL
23. $3.4 \mathrm{~kL}=$ $\qquad$ L
24. $3400 \mathrm{~mL}=$ $\qquad$ L
25. $8 \mathrm{~L}=$ $\qquad$ mL
26. $3.8 \mathrm{~kL}=$ $\qquad$ L
27. $10.6 \mathrm{~kL}=$ $\qquad$ L
28. $1400 \mathrm{~mL}=$ $\qquad$ L
29. José brought home a soft drink bottle that contained 2000 milliliters of liquid. What is the capacity in liters?

## Mass in the Metric System

| Mass |
| :---: |
| 1 gram $(\mathrm{g})=1000$ milligrams $(\mathrm{mg})$ |
| 1 kilogerams $(\mathrm{kg})=1000$ grams |

To change from one metric unit of mass to another, you either multiply or divide.
When changing from a smaller unit to a larger unit, divide.
When changing from a larger unit to a smaller unit, multiply.

## Examples $11325 \mathrm{mg}=$

$\qquad$ g

$$
1325 \div 1000=1.325
$$

$$
1325 \mathrm{mg}=1.325 \mathrm{~g}
$$

$$
\begin{gathered}
276 \mathrm{~kg}=\underline{\mathbf{g}} \\
76 \times 1000=76,000 \\
76 \mathrm{~kg}=76,000 \mathrm{~g}
\end{gathered}
$$

You are changing from a smaller unit (mg) to a larger unit (g), so divide.

Since $1 \mathrm{mg}=1000 \mathrm{~g}$, divide by 1000. Move the decimal point 3 places to the left.

You are changing from a larger unit (kg) to a smaller unit (g), so multiply.
Since $1 \mathrm{~kg}=1000 \mathrm{~g}$, multiply by 1000. Move the decimal point 3 places to the right.

## Complete.

1. $180 \mathrm{mg}=$ $\qquad$ 2. $1600 \mathrm{~g}=\ldots \mathrm{kg}$
2. $1500 \mathrm{~kg}=\longrightarrow \mathrm{g}$
3. $700 \mathrm{mg}=\longrightarrow \mathrm{g}$
4. $8000 \mathrm{~g}=$ $\qquad$ mg
5. $450 \mathrm{~kg}=$ $\qquad$
6. $820 \mathrm{~g}=$ $\qquad$ kg
$\qquad$

## Mass in the Metric System (continued)

## Complete.

9. $5 \mathrm{~kg}=$ $\qquad$
g
10. $4 \mathrm{~g}=$ $\qquad$ mg
11. $3250 \mathrm{mg}=$ $\qquad$
12. $750 \mathrm{~g}=$ $\qquad$ kg
13. $12 \mathrm{~g}=$ $\qquad$ mg
14. $86 \mathrm{~kg}=$ $\qquad$ g
15. $36 \mathrm{~kg}=\square \mathrm{g}$
16. $2.4 \mathrm{~g}=$ $\qquad$ mg
17. $5.35 \mathrm{~g}=$ $\qquad$ mg
18. $86 \mathrm{mg}=$ $\qquad$ g
19. Mr. Chang's truck can carry a payload of 11 kilograms. What is the payload in grams?
20. $3400 \mathrm{mg}=$ $\qquad$
21. $8 \mathrm{~g}=$ $\qquad$ mg
22. $2000 \mathrm{~g}=$ $\qquad$ kg
23. $1400 \mathrm{~g}=$ $\qquad$ kg
24. $3.4 \mathrm{~kg}=$ $\qquad$ g
25. $940 \mathrm{mg}=$ $\qquad$ g  g
26. $850 \mathrm{~g}=$ $\qquad$ kg
27. $3.8 \mathrm{~kg}=$ $\qquad$
28. $10.6 \mathrm{~kg}=\square \mathrm{g}$
29. $140 \mathrm{~kg}=$ $\longrightarrow \mathrm{g}$
30. Jana weighed her dog at 20 kg . What is the weight of her dog in mg ?

## Converting Customary Units to Metric Units

You can use the following chart to convert customary units to metric units.

> | Customary Unit / Metric Unit |
| :---: |
| $1 \mathrm{in} .=2.54 \mathrm{~cm}$ |
| $1 \mathrm{ft}=30.48 \mathrm{~cm}$ or 0.3048 m |
| $1 \mathrm{yd} \approx 0.914 \mathrm{~m}$ |
| $1 \mathrm{mi} \approx 1.609 \mathrm{~km}$ |
| $1 \mathrm{oz}=28.350 \mathrm{~g}$ |
| $1 \mathrm{lb} \approx 454 \mathrm{~g}$ or 0.454 kg |
| $1 \mathrm{fl} \mathrm{oz}=29.574 \mathrm{~mL}$ |
| $1 \mathrm{qt}=0.946 \mathrm{~L}$ |
| $1 \mathrm{gal}=3.785 \mathrm{~L}$ |

Examples $15 \mathrm{ft}=$ $\qquad$ cm
$5 \times 30.48=152.4 \quad 1$ ft $=30.48 \mathrm{~cm}$, so multiply by 30.48.
$5 \mathrm{ft}=152.4 \mathrm{~cm}$
$2 \mathbf{2} \frac{1}{2} \mathbf{~ g a l}=$ $\qquad$ L
$2 \frac{1}{2} \times 3.785=2.5 \times 3.785=9.4625 \quad \mathrm{lgal}=3.785$ L, so multiply by 3.785 .
$2 \frac{1}{2} \mathrm{gal}=9.4625 \mathrm{~L}$
$3 \quad 3.5 \mathrm{lb}=\ldots \mathbf{~ k g}$
$3.5 \times 0.454=1.589 \quad 1 \mathrm{lb} \approx 0.454 \mathrm{~kg}$, so multiply by 0.454 .
$3.5 \mathrm{lb}=1.589 \mathrm{~kg}$

## Complete.

1. 4 in. $=$ $\qquad$ cm
2. $7 \mathrm{oz}=$ $\qquad$ g
3. $2 \mathrm{qt}=$ $\qquad$ L
4. $6 \mathrm{mi}=$ $\qquad$ km
5. $3 \mathrm{gal}=$ $\qquad$ L 6. $16 \mathrm{oz}=$ $\qquad$ g
$\qquad$

## Converting Customary Units to Metric Units (continued)

## Complete.

7. $12 \mathrm{fl} \mathrm{oz}=$ $\qquad$ mL
8. $5 \mathrm{lb}=$ $\qquad$ g
9. $3 \mathrm{yd}=$ $\qquad$ m
10. 1.5 in. $=$ $\qquad$ cm
11. $4 \mathrm{ft}=$ $\qquad$ m
12. $5 \mathrm{qt}=$ $\qquad$ L
13. $12 \mathrm{oz}=$ $\qquad$ g
14. $10 \mathrm{lb}=$ $\qquad$ kg
15. 6 in. $=$ $\qquad$ cm
16. $5.5 \mathrm{ft}=$ $\qquad$ m
17. $2.5 \mathrm{gal}=$ $\qquad$ L 18. $2 \frac{1}{4} \mathrm{mi}=$ $\qquad$ km
18. $6.25 \mathrm{yd}=$ $\qquad$ m
19. $18 \mathrm{lb}=$ $\qquad$ kg
20. $15 \mathrm{fl} \mathrm{oz}=$ $\qquad$ L
21. $3 \frac{1}{8} \mathrm{mi}=$ $\qquad$ km
22. $1 \frac{3}{4} \mathrm{ft}=$ $\qquad$ cm
23. $2.5 \mathrm{qt}=$ $\qquad$ L
24. $10 \mathrm{fl} \mathrm{oz}=$ $\qquad$ mL
25. $15 \mathrm{qt}=$ $\qquad$ L
26. $220 \mathrm{mi}=$ $\qquad$ km
27. $20 \mathrm{yd}=$ $\qquad$ m
28. $20.35 \mathrm{lb}=$ $\qquad$ kg 30. $20 \mathrm{qt}=$ $\qquad$ L
29. $350.5 \mathrm{mi}=$ $\qquad$ km 32. $25 \mathrm{fl} \mathrm{oz}=$ $\qquad$ mL 33. $4.5 \mathrm{lb}=$ $\qquad$ kg

## Converting Metric Units to Customary Units

You can use the following chart to convert customary units to metric units.

> | Customary Unit / Metric Unit |
| :---: |
| $\begin{array}{c}1 \mathrm{~cm}=0.394 \mathrm{in} . \\ 1 \mathrm{~m}=3.281 \mathrm{ft} \text { or } 1.093 \mathrm{yd} \\ 1 \mathrm{~km} \approx 0.621 \mathrm{mi} \\ 1 \mathrm{~g} \approx 0.035 \mathrm{oz} \\ 1 \mathrm{~kg}=2.205 \mathrm{lb} \mathrm{g} \\ 1 \mathrm{~mL} \approx 0.034 \mathrm{fl} \mathrm{oz} \\ 1 \mathrm{~L}=1.057 \mathrm{qt} \text { or } 0.264 \mathrm{gal}\end{array}$ |

Examples $13 \mathrm{~cm}=$ $\qquad$ in.
$3 \times 0.394=1.182 \quad 1 \mathrm{~cm} \approx 0.394$ in., so multiply by 0.394 .
$3 \mathrm{~cm}=1.182 \mathrm{in}$.
$2 \quad 250 \mathrm{~g}=$ $\qquad$ oz
$250 \times 0.035=8.75 \quad 1 g \approx 0.035 \mathrm{oz}$, so multiply by 0.035 .
$250 \mathrm{~g}=8.75 \mathrm{oz}$
$3 \quad 1.5 \mathrm{~L}=$ $\qquad$ qt
$1.5 \times 1.057=1.5855 \quad l L \approx 1.057$ qt, so multiply by 1.057.
$1.5 \mathrm{~L}=1.5855 \mathrm{qt}$

## Complete.

1. $5 \mathrm{~cm}=$ $\qquad$ in.
2. $787 \mathrm{~g}=$ $\qquad$ oz
3. $4 \mathrm{~L}=$ $\qquad$ qt
4. $8 \mathrm{~km}=$ $\qquad$ mi
5. $2 \mathrm{~L}=$ $\qquad$ gal
6. $300 \mathrm{~g}=$ $\qquad$ oz
7. $155 \mathrm{~mL}=$ $\qquad$ fl oz
8. $9 \mathrm{~km}=$ $\qquad$ mi
9. $4 \mathrm{~m}=$ $\qquad$ yd
$\qquad$

## Converting Metric Units to Customary Units (continued)

Complete.
10. $3.5 \mathrm{~km}=$ $\qquad$ mi
11. $10 \mathrm{~mL}=$ $\qquad$ fl oz 12. $4.5 \mathrm{~L}=$ $\qquad$ gal
13. $7.5 \mathrm{~m}=$ $\qquad$ ft
14. $2.3 \mathrm{~m}=$ $\qquad$ yd 15. $3.5 \mathrm{~L}=$ $\qquad$ qt
16. $260 \mathrm{~mL}=$ $\qquad$ fl oz
17. $14 \mathrm{~kg}=$ $\qquad$ lb 18. $3.25 \mathrm{~m}=$ $\qquad$ ft
19. $24.5 \mathrm{~km}=$ $\qquad$ mi
20. $22 \mathrm{~L}=$ $\qquad$ gal
21. $45 \mathrm{~g}=$ $\qquad$ oz
22. $1.25 \mathrm{~m}=$ $\qquad$ ft 23. $12 \mathrm{~kg}=$ ft $\quad$ 23. $12 \mathrm{~kg}=$ $\qquad$ lb
24. $14 \mathrm{~L}=$ $\qquad$ gal
25. $4.65 \mathrm{~km}=$ $\qquad$ mi
26. $4.8 \mathrm{~cm}=$ $\qquad$ in. 27. $8.5 \mathrm{~L}=$ $\qquad$ qt
28. $40 \mathrm{~mL}=$ $\qquad$ floz
29. $10.9 \mathrm{~L}=$ $\qquad$ gal 30. $280 \mathrm{~km}=$ $\qquad$ mi
31. $8 \mathrm{~m}=$ $\qquad$ yd
32. $15.35 \mathrm{~kg}=$ $\qquad$ lb 33. $10.5 \mathrm{~L}=$ $\qquad$ qt
34. $6 \mathrm{~cm}=$ $\qquad$ in.
35. $15.5 \mathrm{~m}=$ $\qquad$ yd 36. $14 \mathrm{~g}=$ $\qquad$ oz
$\qquad$ qt
38. $50 \mathrm{~kg}=$ $\qquad$ lb 39. $2.8 \mathrm{~m}=$ $\qquad$ ft
$\qquad$

## Adding and Converting Units of Time

| Time |
| :---: |
| 1 hour $(\mathrm{hr})=60$ minutes $(\mathrm{min})$ |
| 1 minute $(\mathrm{min})=60$ seconds |

To add measures of time, add the seconds, add the minutes, and add the hours. Rename if necessary.

Example Add 4 hours $\mathbf{2 5}$ minutes $\mathbf{4 0}$ seconds and $\mathbf{5}$ hours $\mathbf{3 0}$ minutes $\mathbf{2 5}$ seconds.
4 h $25 \min 40 \mathrm{~s}$


## Rename each of the following.

1. $14 \mathrm{~min} 85 \mathrm{~s}=$ $\qquad$ $\min 25 \mathrm{~s}$
2. $8 \mathrm{~h} 65 \mathrm{~min}=9 \mathrm{~h}$ $\qquad$ $\min$
3. $3 \mathrm{~h} 19 \mathrm{~min} 67 \mathrm{~s}=3 \mathrm{~h}$ $\qquad$ $\min 7 \mathrm{~s}$
4. $6 \mathrm{~h} 68 \mathrm{~min} 25 \mathrm{~s}=$ $\qquad$ h $\qquad$ $\min 25 \mathrm{~s}$
5. $7 \mathrm{~h} 105 \min 15 \mathrm{~s}=$ $\qquad$ h $\qquad$ $\min 15 \mathrm{~s}$
6. $4 \mathrm{~h} 99 \mathrm{~min} 80 \mathrm{~s}=$ $\qquad$ h $\qquad$ min $\qquad$ s
7. $1 \mathrm{~h} 76 \min 91 \mathrm{~s}=$ $\qquad$ h $\qquad$ min $\qquad$ s
8. $7 \mathrm{~h} 88 \mathrm{~min} 60 \mathrm{~s}=$ $\qquad$ h $\qquad$ min $\qquad$ s
$\qquad$

## Adding and Converting Units of Time (continued)

## Add. Rename if necessary.

9. $\begin{array}{r}35 \min 45 \mathrm{~s} \\ +\quad 12 \min 12 \mathrm{~s} \\ \hline\end{array}$
10. 6 h 50 min
$+3 \mathrm{~h} 17 \mathrm{~min}$
11. 9 h 45 min 10 s
$+3 \mathrm{~h} 30 \mathrm{~min} 50 \mathrm{~s}$
12. 1 h 55 min 12 s
$+3 \mathrm{~h} 25 \mathrm{~min} 34 \mathrm{~s}$
13. $\quad 11 \mathrm{~h} 33 \mathrm{~min} 6 \mathrm{~s}$
$+5 \mathrm{~h} 36 \mathrm{~min} 29 \mathrm{~s}$
14. 6 h 10 min 47 s
$+2 \mathrm{~h} 51 \mathrm{~min} 28 \mathrm{~s}$
15. 7 h 30 min 52 s
$+3 \mathrm{~h} 45 \mathrm{~min} 40 \mathrm{~s}$
16. 9 h 10 min 45 s
$+3 \mathrm{~h} 55 \mathrm{~min} 30 \mathrm{~s}$

An atlas gives average travel times. Use this information to answer Exercises 17-19.
17. What is the average travel time from Baton

Rouge to Tallahassee going through Mobile?

| Average Travel Times |  |
| :--- | :--- |
| Baton Rouge to Mobile | 4 h 40 min |
| Mobile to Tallahassee | 5 h 50 min |
| Tallahassee to Jacksonville | 3 h 35 min |

18. What is the average travel time from Mobile to Jacksonville going through Tallahassee?
19. What is the average travel time from Baton Rouge to Jacksonville going through Mobile and Tallahassee?
20. Wesley Paul set an age group record in the 1977 New York Marathon.

He ran the race in 3 hours 31 seconds. He was 8 years old at the time. If he ran 2 hours 58 minutes 48 seconds in practice the day before the race, for how long did Wesley run on both days?

## Line Graphs

The diagram shows the parts of a graph.


## Solve.

1. Make a line graph for this set of data.

| Number of Votes Expected |  |
| :---: | :---: |
| Date | Number of Votes |
| $3 / 15$ | 18 |
| $3 / 30$ | 11 |
| $4 / 15$ | 15 |
| $4 / 30$ | 9 |

2. Make a line graph for this set of data.

| Evans Family Electric Bill |  |
| :---: | :---: |
| Month | Amount |
| March | $\$ 129.90$ |
| April | $\$ 112.20$ |
| May | $\$ 105.00$ |
| June | $\$ 88.50$ |

$\qquad$
$\qquad$

## Line Graphs (continued)

Refer to the following table for Exercises 1-2.

## Recorded Number of

 Hurricanes by Month| Month | No. of Hurricanes |
| :---: | :---: |
| June | 23 |
| July | 36 |
| Aug. | 149 |
| Sept. | 188 |
| Oct. | 95 |
| Nov. | 21 |


3. Complete the line graph for the data in the table.

Month
4. After which month does the number of hurricanes start to decrease?

Use the data in the table to complete the line graph.
5. Temperatures on 2/15

| Time | Temperature |
| :---: | :---: |
| 9:00 A.M. | $32^{\circ} \mathrm{F}$ |
| 11:00 A.M. | $35^{\circ} \mathrm{F}$ |
| 1:00 P.M. | $38^{\circ} \mathrm{F}$ |
| 3:00 P.M. | $42^{\circ} \mathrm{F}$ |
| 5:00 P.M. | $39^{\circ} \mathrm{F}$ |

Solve. Use the line graph.
6. During which hour did the most rainfall occur?
7. How many inches of rain fell between 4 P.M. and 6 P.м.?
8. How many inches of rain fell between 3 P.M. and 8 P.m.?

Temperatures on 2/15


Monday's Total Rainfall

$\qquad$
$\qquad$

## Histograms

A histogram uses bars to display numerical data that have been organized into equal intervals.
Example The table shows the percent of people in several age groups who are not covered by health insurance. Make a histogram of the data.


| Age | Percent |
| :---: | :---: |
| under 18 | $12.4 \%$ |
| $18-24$ | $28.9 \%$ |
| $25-34$ | $20.9 \%$ |
| $35-44$ | $15.5 \%$ |
| $45-54$ | $14.0 \%$ |
| $55-64$ | $12.9 \%$ |
| over 65 | $1.2 \%$ |

## Make a histogram of the data below.

1. 

| Pieces of <br> Junk Mail | Frequency |
| :---: | :---: |
| $0-4$ | 25 |
| $5-9$ | 35 |
| $10-14$ | 50 |
| $15-19$ | 40 |
| $20-24$ | 15 |

Frequency of Junk Mail

2.

| Time Spent Surfing <br> the Web <br> (in hours per day) | Frequency |
| :---: | :---: |
| $0-1$ | 20 |
| $2-3$ | 18 |
| $4-5$ | 2 |
| $6-7$ | 1 |

Time Spent Surfing Web
$\qquad$
$\qquad$

## Histograms (continued)

Use the histogram at the right to answer each question.
3. How many students took the algebra test?
4. Which grade has the most test scores?
5. Which grades have the same number of test scores?

6. How many more students earned $85-89$ than earned $80-84$ ?
7. Make a frequency table of the algebra scores.

A survey was taken that asked people their height in inches. The data are shown below.

| 68 | 69 | 72 | 64 | 74 | 56 | 62 | 58 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 69 | 65 | 70 | 59 | 71 | 67 | 66 | 64 |
| 73 | 78 | 70 | 52 | 61 | 68 | 67 | 66 |

8. Make a frequency table and histogram of the data. Use the intervals 51-55, 56-60, 61-65, 66-70, 71-75, and 76-80.
9. How many heights are in the $66-70$ interval?
10. How many people in the survey are taller than 5 feet?
11. How many people in the survey are shorter than 5 feet?
12. What interval has the greatest number of heights?
13. How many people were surveyed?

## Probability

The probability of an event is the ratio of the number of ways an event can occur to the number of possible outcomes.

$$
\text { probability of an event }=\frac{\text { number of ways the event can occur }}{\text { number of possible outcomes }}
$$

Example On the spinner below, there are ten equally likely outcomes. Find the probability of spinning a number less than 5.

Numbers less than 5 are 1, 2, 3, and 4. There are 10 possible outcomes.

Probability of number less than $5=\frac{4}{10}$ or $\frac{2}{5}$.


The probability of spinning a number less than 5 is $\frac{2}{5}$.

A box of crayons contains 3 shades of red, 5 shades of blue, and 2 shades of green. If a child chooses a crayon at random, find the probability of choosing each of the following.

1. a green crayon
2. a blue crayon
3. a red crayon
4. a crayon that is not red
5. a red or blue crayon
6. a red or green crayon

## Probability (continued)

A card is chosen at random from a deck of 52 cards. Find the probability of choosing each of the following.
7. a red card
8. the jack of diamonds
9. an ace
10. a black 10
11. a heart
12. not a club
A cooler contains 2 cans of grape juice, 3 cans of grapefruit juice, and 7 cans of orange juice. If a person chooses a can of juice at random, find the probability of choosing each of the following.
13. grapefruit juice
14. orange juice
15. grape juice
16. orange or grape juice
17. not orange juice
18. not grape juice

Businesses use statistical surveys to predict customers' future buying habits. A department store surveyed 200 customers on a Saturday in December to find out how much each customer spent on their visit to the store. Use the results at the right to answer Exercises 19-21.
19. What is the probability that a customer will spend less than $\$ 2.00$ ?
20. What is the probability that a customer will

| Amount Spent | Number of <br> Customers |
| :---: | :---: |
| Less than \$2 | 14 |
| $\$ 2-\$ 4.99$ | 36 |
| $\$ 5-\$ 9.99$ | 42 |
| $\$ 10-\$ 19.99$ | 32 |
| $\$ 20-\$ 49.99$ | 32 |
| $\$ 50-\$ 99.99$ | 22 |
| $\$ 100$ or more | 22 | spend less than $\$ 10.00$ ?

21. What is the probability that a customer will spend between $\$ 20.00$ and $\$ 100.00$ ?
$\qquad$
$\qquad$
$\qquad$
22. How many more students earned $85-89$ than earned $80-84$ ?
23. Make a frequency table of the algebra scores.
24. How many more students earned $85-89$ than earned $80-84$ ?
25. Make a frequency table of the algebra scores.
26. $\frac{3}{4}, \frac{2}{5}, \frac{5}{8}, \frac{1}{2}$
27. $\frac{1}{3}, \frac{2}{7}, \frac{3}{14}, \frac{1}{6}$
28. $\frac{11}{12}, \frac{5}{6}, \frac{3}{4}, \frac{9}{16}$
29. $\frac{7}{8}, \frac{4}{5}, \frac{3}{4}, \frac{9}{10}$
30. $\frac{1}{2}, \frac{3}{5}, \frac{2}{7}, \frac{5}{9}$
31. $\frac{2}{3}, \frac{4}{9}, \frac{5}{6}, \frac{7}{12}$
32. $\frac{7}{15}, \frac{3}{5}, \frac{5}{12}, \frac{1}{2}$
33. $\frac{4}{5}, \frac{2}{3}, \frac{11}{35}, \frac{7}{9}$
34. $\frac{1}{3}, \frac{2}{5}, \frac{3}{12}, \frac{3}{10}$
35. $\frac{1}{10}, \frac{2}{3}, \frac{1}{12}, \frac{5}{6}$
36. 0.525
37. 0.45
38. $0.333 \ldots$
39. 0.43
40. 0.8
41. $0.1212 \ldots$
42. 0.345
43. 0.1862
44. $0.4555 \ldots$
45. 0.345
46. 0.1862
47. $0.4555 \ldots$
48. 0.345
49. 0.1862
50. $0.4555 \ldots$
51. 0.66
52. 0.08
53. 0.75
54. 0.001
55. 1.19
56. 0.72
57. 0.136
58. 4.02
59. 0.36
60. 0.18
61. 0.09
62. 0.2
63. 0.625
64. 0.007
65. 1.4
66. 0.093

[^0]:    Send all inquiries to:
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