

**Study Guide and Intervention**

Alg1 3.0

**Solving Open Sentences Involving Absolute Value**

**Absolute Value Equations** When solving equations that involve absolute value, there are two cases to consider.

**Case 1:** The value inside the absolute value symbols is positive.

**Case 2:** The value inside the absolute value symbols is negative.

**Example 1** Solve  $|x + 4| = 1$ . Then graph the solution set.

Write  $|x + 4| = 1$  as  $x + 4 = 1$  or  $x + 4 = -1$ .

$$x + 4 = 1 \quad \text{or} \quad x + 4 = -1$$

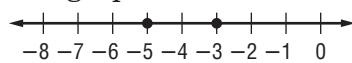
$$x + 4 - 4 = 1 - 4 \quad x + 4 = -1$$

$$x = -3 \quad x + 4 - 4 = -1 - 4$$

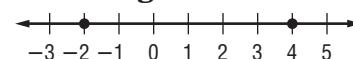
$$x = -5$$

The solution set is  $\{-5, -3\}$ .

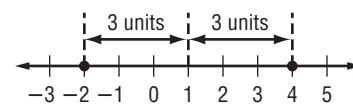
The graph is shown below.



**Example 2** Write an equation involving absolute value for the graph.



Find the point that is the same distance from  $-2$  as it is from  $4$ .



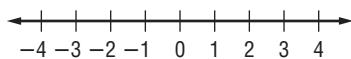
The distance from  $1$  to  $-2$  is  $3$  units. The distance from  $1$  to  $4$  is  $3$  units.

So,  $|x - 1| = 3$ .

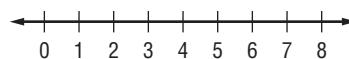
**Exercises**

Solve each open sentence. Then graph the solution set.

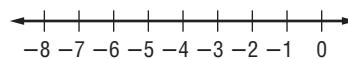
1.  $|y| = 3$



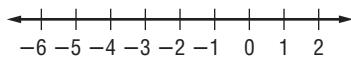
2.  $|x - 4| = 4$



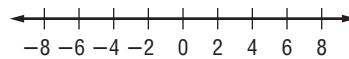
3.  $|y + 3| = 2$



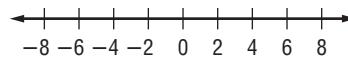
4.  $|b + 2| = 3$



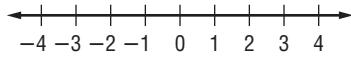
5.  $|w - 2| = 5$



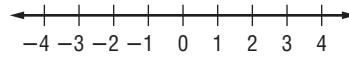
6.  $|t + 2| = 4$



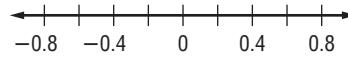
7.  $|2x| = 8$



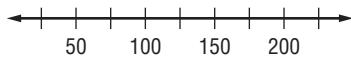
8.  $|5y - 2| = 7$



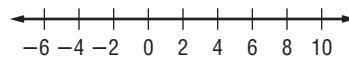
9.  $|p - 0.2| = 0.5$



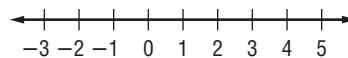
10.  $|d - 100| = 50$



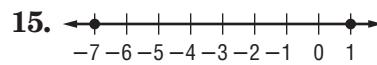
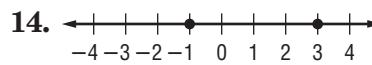
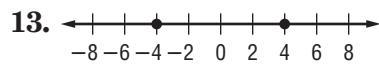
11.  $|2x - 1| = 11$



12.  $\left|3x + \frac{1}{2}\right| = 6$



For each graph, write an open sentence involving absolute value.



# Study Guide and Intervention

## Solving Open Sentences Involving Absolute Value

**Absolute Value Equations** When solving equations that involve absolute value, there are two cases to consider.

**Case 1:** The value inside the absolute value symbols is positive.

**Case 2:** The value inside the absolute value symbols is negative.

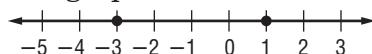
**Example 1** Solve  $|x + 1| = 2$ . Then graph the solution set.

Write  $|x + 1| = 2$  as  $x + 1 = 2$  and  $x + 1 = -2$ .

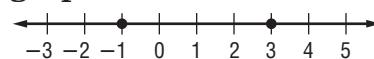
$$\begin{array}{ll} x + 1 = 2 & \text{or} \\ x + 1 - 1 = 2 - 1 & x + 1 - 1 = -2 - 1 \\ x = 1 & x = -3 \end{array}$$

The solution set is  $\{-3, 1\}$ .

The graph is shown below.



**Example 2** Write an equation involving absolute value for the graph.



Find the point that is the same distance from  $-1$  as it is from  $3$ .

The distance from  $1$  to  $-1$  is  $2$  units.

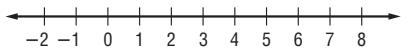
The distance from  $1$  to  $3$  is  $2$  units.

$$\text{So, } |x - 1| = 2$$

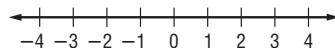
### Exercises

Solve each open sentence. Then graph the solutions set.

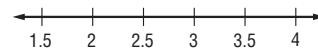
1.  $|w - 3| = 4$



2.  $|2k - 3| = 1$



3.  $|x - 3.2| = 0.8$



For each graph, write an open sentence involving absolute value.

