## CHAPTER 3

## Data and Signals

## Solutions to Odd-Numbered Review Questions and Exercises

## Review Questions

1. Frequency and period are the inverse of each other. $T=1 / \mathrm{f}$ and $\mathrm{f}=1 / \mathrm{T}$.
2. Using Fourier analysis. Fourier series gives the frequency domain of a periodic signal; Fourier analysis gives the frequency domain of a nonperiodic signal.
3. Baseband transmission means sending a digital or an analog signal without modulation using a low-pass channel. Broadband transmission means modulating a digital or an analog signal using a band-pass channel.
4. The Nyquist theorem defines the maximum bit rate of a noiseless channel.
5. Optical signals have very high frequencies. A high frequency means a short wave length because the wave length is inversely proportional to the frequency $(\lambda=v / f)$, where $v$ is the propagation speed in the media.
6. The frequency domain of a voice signal is normally continuous because voice is a nonperiodic signal.
7. This is baseband transmission because no modulation is involved.
8. This is broadband transmission because it involves modulation.

## Exercises

17. 

a. $\mathbf{f}=\mathbf{1} / \mathbf{T}=1 /(5 \mathrm{~s})=0.2 \mathrm{~Hz}$
b. $\mathbf{f}=\mathbf{1} / \mathbf{T}=1 /(12 \mu \mathrm{~s})=83333 \mathrm{~Hz}=83.333 \times 10^{3} \mathrm{~Hz}=\mathbf{8 3 . 3 3 3} \mathbf{~ K H z}$
c. $\mathbf{f}=\mathbf{1} / \mathbf{T}=1 /(220 \mathrm{~ns})=4550000 \mathrm{~Hz}=4.55 \times 10^{6} \mathrm{~Hz}=4.55 \mathrm{MHz}$
19. See Figure 3.1
21. Each signal is a simple signal in this case. The bandwidth of a simple signal is zero. So the bandwidth of both signals are the same.
23.
a. $(10 / 1000) \mathrm{s}=0.01 \mathrm{~s}$
b. $(8 / 1000) \mathrm{s}=0.008 \mathrm{~s}=\mathbf{8} \mathrm{ms}$

Figure 3.1 Solution to Exercise 19

c. $((100,000 \times 8) / 1000) \mathrm{s}=\mathbf{8 0 0} \mathrm{s}$
25. The signal makes 8 cycles in 4 ms . The frequency is $8 /(4 \mathrm{~ms})=\mathbf{2 ~ K H z}$
27. The signal is periodic, so the frequency domain is made of discrete frequencies. as shown in Figure 3.2.

Figure 3.2 Solution to Exercise 27

29.

Using the first harmonic, data rate $=2 \times 6 \mathrm{MHz}=12 \mathbf{~ M b p s}$
Using three harmonics, data rate $=(2 \times 6 \mathrm{MHz}) / 3=\mathbf{4} \mathbf{~ M b p s}$
Using five harmonics, data rate $=(2 \times 6 \mathrm{MHz}) / 5=2.4 \mathrm{Mbps}$
31. $-10=10 \log _{10}\left(\mathrm{P}_{2} / 5\right) \rightarrow \log _{10}\left(\mathrm{P}_{2} / 5\right)=-1 \rightarrow\left(\mathrm{P}_{2} / 5\right)=10^{-1} \rightarrow \mathrm{P}_{2}=\mathbf{0 . 5} \mathbf{W}$
33. 100,000 bits $/ 5 \mathrm{Kbps}=20 \mathrm{~s}$
35. $1 \mu \mathrm{~m} \times 1000=1000 \mu \mathrm{~m}=\mathbf{1} \mathrm{mm}$
37. We have

$$
4,000 \log _{2}(1+10 / 0.005)=43,866 \mathrm{bps}
$$

39. To represent 1024 colors, we need $\log _{2} 1024=10$ (see Appendix C) bits. The total number of bits are, therefore,

$$
1200 \times 1000 \times 10=12,000,000 \text { bits }
$$

41. We have

## SNR= (signal power)/(noise power).

However, power is proportional to the square of voltage. This means we have

$$
\begin{aligned}
& \text { SNR }=\left[(\text { signal voltage })^{2}\right] /\left[(\text { noise voltage })^{2}\right]= \\
& {[(\text { signal voltage }) /(\text { noise voltage })]^{2}=20^{2}=400}
\end{aligned}
$$

We then have

$$
\mathrm{SNR}_{\mathrm{dB}}=10 \log _{10} \mathrm{SNR} \approx 26.02
$$

43. 

a. The data rate is doubled $\left(\mathrm{C}_{2}=2 \times \mathrm{C}_{1}\right)$.
b. When the SNR is doubled, the data rate increases slightly. We can say that, approximately, $\left(\mathrm{C}_{2}=\mathrm{C}_{1}+1\right)$.
45. We have

> transmission time = (packet length)/(bandwidth) $=$ $(8,000,000$ bits $) /(200,000 \mathrm{bps})=40 \mathrm{~s}$
47.
a. Number of bits $=$ bandwidth $\times$ delay $=1 \mathrm{Mbps} \times 2 \mathrm{~ms}=2000$ bits
b. Number of bits $=$ bandwidth $\times$ delay $=10 \mathrm{Mbps} \times 2 \mathrm{~ms}=\mathbf{2 0 , 0 0 0}$ bits
c. Number of bits $=$ bandwidth $\times$ delay $=100 \mathrm{Mbps} \times 2 \mathrm{~ms}=\mathbf{2 0 0 , 0 0 0}$ bits

