## CHAPTER 12

## Multiple Access

## Solutions to Odd-Numbered Review Questions and Exercises

## Review Questions

1. The three categories of multiple access protocols discussed in this chapter are random access, controlled access, and channelization.
2. In controlled access methods, the stations consult one another to find which station has the right to send. A station cannot send unless it has been authorized by other stations. We discuss three popular controlled-access methods: reservation, polling, and token passing.
3. In random access methods, there is no access control (as there is in controlled access methods) and there is no predefined channels (as in channelization). Each station can transmit when it desires. This liberty may create collision.
4. In a random access method, the whole available bandwidth belongs to the station that wins the contention; the other stations needs to wait. In a channelization method, the available bandwidth is divided between the stations. If a station does not have data to send, the allocated channel remains idle.
5. We do not need a multiple access method in this case. The local loop provides a dedicated point-to-point connection to the telephone office.

## Exercises

11. To achieve the maximum efficiency in pure ALOHA, $G=1 / 2$. If we let $\boldsymbol{n s}$ to be the number of stations and $n f s$ to be the number of frames a station can send per second.

$$
\mathrm{G}=\boldsymbol{n} \boldsymbol{s} \times \boldsymbol{n} \boldsymbol{f s} \times \mathrm{T}_{\mathrm{fr}}=100 \times \boldsymbol{n} \boldsymbol{f} \boldsymbol{s} \times 1 \mu \mathrm{~s}=1 / 2 \rightarrow \boldsymbol{n} \boldsymbol{f} \boldsymbol{s}=5 \mathbf{0 0 0} \mathbf{f r a m e s} / \mathbf{s}
$$

The reader may have noticed that the $\mathrm{T}_{\mathrm{fr}}$ is very small in this problem. This means that either the data rate must be very high or the frames must be very small.
13. We can first calculate $T_{\mathrm{fr}}$ and G , and then the throughput.

$$
\begin{gathered}
\mathrm{T}_{\mathrm{fr}}=(1000 \mathrm{bits}) / 1 \mathrm{Mbps}=1 \mathrm{~ms} \\
\mathrm{G}=\boldsymbol{n s} \times \boldsymbol{n f s} \times \mathrm{T}_{\mathrm{fr}}=100 \times 10 \times 1 \mathrm{~ms}=1 \\
\text { For pure ALOHA } \rightarrow \mathrm{S}=\mathrm{G} \times \mathrm{e}^{-2 \mathrm{G}} \approx \mathbf{1 3 . 5 3} \text { percent }
\end{gathered}
$$

This means that each station can successfully send only 1.35 frames per second.
15. Let us find the relationship between the minimum frame size and the data rate. We know that

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\(\mathrm{T}_{\mathrm{fr}}=(\) frame size \() /(\) data rate \()=2 \times \underset{\substack{\mathrm{T}_{\mathrm{p}} \\ \text { or }}}{\mathrm{T}^{2}} \times 2 \times\) distance \(/\) (propagation speed)
    \((\) frame size \()=[2 \times(\) distance \() /(\) propagation speed \()] \times(\) data rate \()]\)
    or
    (frame size) \(=\mathbf{K} \times\) (data rate)
```

This means that minimum frame size is proportional to the data rate ( K is a constant). When the data rate is increased, the frame size must be increased in a network with a fixed length to continue the proper operation of the CSMA/CD. In Example 12.5, we mentioned that the minimum frame size for a data rate of 10 Mbps is 512 bits. We calculate the minimum frame size based on the above proportionality relationship

| Data rate $=10 \mathrm{Mbps}$ | $\rightarrow$ | minimum frame size $=\mathbf{5 1 2}$ bits |
| :--- | :--- | :--- |
| Data rate $=100 \mathrm{Mbps}$ | $\rightarrow$ | minimum frame size $=\mathbf{5 1 2 0}$ bits |
| Data rate $=1 \mathrm{Gbps}$ | $\rightarrow$ | minimum frame size $=\mathbf{5 1 , 2 0 0}$ bits |
| Data rate $=10 \mathrm{Gbps}$ | $\rightarrow$ | minimum frame size $=\mathbf{5 1 2 , 0 0 0}$ bits |

17. We have $t_{1}=0$ and $t_{2}=3 \mu \mathrm{~s}$
a. $\mathrm{t}_{3}-\mathrm{t}_{1}=(2000 \mathrm{~m}) /\left(2 \times 10^{8} \mathrm{~m} / \mathrm{s}\right)=10 \mu \mathrm{~s} \rightarrow \mathrm{t}_{3}=10 \mu \mathrm{~s}+\mathrm{t}_{1}=10 \mu \mathrm{~s}$
b. $\mathrm{t}_{4}-\mathrm{t}_{2}=(2000 \mathrm{~m}) /\left(2 \times 10^{8} \mathrm{~m} / \mathrm{s}\right)=10 \mu \mathrm{~s} \rightarrow \mathrm{t}_{4}=10 \mu \mathrm{~s}+\mathrm{t}_{2}=\mathbf{1 3} \mu \mathrm{s}$
c. $\mathrm{T}_{\mathrm{fr}(\mathrm{A})}=\mathrm{t}_{4}-\mathrm{t}_{1}=13-0=13 \mu \mathrm{~s} \rightarrow$ Bits $_{\mathrm{A}}=10 \mathrm{Mbps} \times 13 \mu \mathrm{~s}=130$ bits
d. $\mathrm{T}_{\mathrm{fr}(\mathrm{C})}=\mathrm{t}_{3}-\mathrm{t}_{2}=10-3=07 \mu \mathrm{~s} \rightarrow$ Bits $_{\mathrm{C}}=10 \mathrm{Mbps} \times 07 \mu \mathrm{~s}=70$ bits
18. See Figure 12.1.

Figure 12.1 Solution to Exercise 19

$$
\mathrm{W}_{8}=\left[\begin{array}{llllllll}
+1 & +1 & +1 & +1 & +1 & +1 & +1 & +1 \\
+1 & -1 & +1 & -1 & +1 & -1 & +1 & -1 \\
+1 & +1 & - & -1 & +1 & + & -1 & -1 \\
+1 & -1 & -1 & +1 & +1 & -1 & -1 & +1 \\
& & & & & & & \\
+1 & +1 & +1 & +1 & -1 & -1 & -1 & -1 \\
+1 & -1 & + & -1 & -1 & +1 & -1 & +1 \\
+1 & +1 & -1 & -1 & -1 & -1 & +1 & +1 \\
+1 & -1 & -1 & +1 & -1 & +1 & +1 & -1
\end{array}\right]
$$

21. 

Third Property: we calculate the inner product of each row with itself:

| Row 1•Row 1 | $[+1+1+1+1]$ | $\bullet$ | $[+1+1+1+1]$ | $=+1+1+1+1=4$ |
| :--- | :--- | :--- | :--- | :--- |
| Row 2•Row 2 | $[+1-1+1-1]$ | $\bullet$ | $[+1-1+1-1]$ | $=+1+1+1+1=4$ |
| Row 3•Row 1 | $[+1+1-1-1]$ | $\bullet$ | $[+1+1-1]$ | $=+1+1+1+1=4$ |
| Row 4 $\bullet$ Row 4 | $[+1-1-1+1]$ | $\bullet$ | $[+1-1-1]$ | $=+1+1+1+1=4$ |

Fourth Property: we need to prove 6 relations:

| Row 1•Row 2 | $[+1+1+1+1]$ | $\bullet$ | $[+1-1+1-1]$ | $=+1-1+1-1=\mathbf{0}$ |
| :--- | :--- | :--- | :--- | :--- |
| Row 1•Row 3 | $[+1+1+1+1]$ | $\bullet$ | $[+1+1-1-1]$ | $=+1+1-1-1=\mathbf{0}$ |
| Row 1•Row 4 | $[+1+1+1+1]$ | $\bullet$ | $[+1-1-1+1]$ | $=+1-1-1+1=\mathbf{0}$ |
| Row 2•Row 3 | $[+1-1+1-1]$ | $\bullet$ | $[+1+1-1-1]$ | $=+1-1-1+1=\mathbf{0}$ |
| Row 2•Row 4 | $[+1-1+1-1]$ | $\bullet$ | $[+1-1-1+1]$ | $=+1+1-1-1=\mathbf{0}$ |
| Row 3 $\bullet$ Row 4 | $[+1+1-1-1]$ | $\bullet$ | $[+1-1-1+1]$ | $=+1-1+1-1=\mathbf{0}$ |

23. Figure 12.2 shows the encoding, the data on the channel, and the decoding.

Figure 12.2 Solution to Exercise 23

25. We can say:

## Polling and Data Transfer

Frame 1 for all four stations: $4 \times[$ poll + frame + ACK) $]$
Frame 2 for all four stations: $4 \times$ [poll + frame + ACK) $]$
Frame 3 for all four stations: $4 \times$ [poll + frame + ACK)]

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Frame 4 for all four stations: \(4 \times\) [poll + frame + ACK) \(]\)
Frame 5 for all four stations: \(4 \times\) [poll + frame + ACK)]
Polling and Sending NAKs
Station 1: [poll + NAK]
Station 2: [poll + NAK]
Station 3: [poll + NAK]
Station 4: [poll + NAK]
Total Activity:
24 polls +20 frames +20 ACKs +4 NAKs \(=21536\) bytes
We have 1536 bytes of overhead which is 512 bytes more than the case in Exercise
23. The reason is that we need to send 16 extra polls.
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