



Curriculum Correlation between *McGraw-Hill Ryerson Principles of Mathematics 9* and The Ontario Curriculum Principles of Mathematics, Grade 9, Academic (MPM1D)

This course enables students to develop an understanding of mathematical concepts related to algebra, analytic geometry, and measurement and geometry through investigation, the effective use of technology, and abstract reasoning. Students will investigate relationships, which they will then generalize as equations of lines, and will determine the connections between different representations of a linear relation. They will also explore relationships that emerge from the measurement of three-dimensional figures and two-dimensional shapes. Students will reason mathematically and communicate their thinking as they solve multi-step problems.

Mathematical process expectations. The mathematical processes are to be integrated into student learning in all areas of this course.

Throughout this course, students will:

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| Problem Solving | <ul style="list-style-type: none">• develop, select, apply, and compare a variety of problem-solving strategies as they pose and solve problems and conduct investigations, to help deepen their mathematical understanding; |
| Reasoning and Proving | <ul style="list-style-type: none">• develop and apply reasoning skills (e.g., recognition of relationships, generalization through inductive reasoning, use of counter-examples) to make mathematical conjectures, assess conjectures, and justify conclusions, and plan and construct organized mathematical arguments; |
| Reflecting | <ul style="list-style-type: none">• demonstrate that they are reflecting on and monitoring their thinking to help clarify their understanding as they complete an investigation or solve a problem (e.g., by assessing the effectiveness of strategies and processes used, by proposing alternative approaches, by judging the reasonableness of results, by verifying solutions); |
| Selecting Tools and Computational Strategies | <ul style="list-style-type: none">• select and use a variety of concrete, visual, and electronic learning tools and appropriate computational strategies to investigate mathematical idea and to solve problems; |
| Connecting | <ul style="list-style-type: none">• make connections among mathematical concepts and procedures, and realer mathematical ideas of situations or phenomena drawn from other contexts (e.g., other curriculum areas, daily life, current events, art and culture, sports); |
| Representing | <ul style="list-style-type: none">• create a variety of representations of mathematical ideas (e.g., numeric, geometric, algebraic, graphical, pictorial representations; onscreen dynamic representations), connect and compare them, and select and apply the appropriate representation to solve problems; |
| Communicating | <ul style="list-style-type: none">• communicate mathematical thinking orally, visually, and in writing, using mathematical vocabulary and a variety of appropriate representations, and observing mathematical conventions. |

The mathematical process expectations are introduced in Chapter 1 of *Principles of Mathematics 9* and then integrated throughout Chapters 2–9.

Number Sense and Algebra

Overall Expectations

By the end of this course, students will:

- ❖ demonstrate an understanding of the exponent rules of multiplication and division, and apply them to simplify expressions
- ❖ manipulate numerical and polynomial expressions, and solve first-degree equations

Specific Expectations

	Chapter/Section	Pages
<i>Operating With Exponents</i>		
By the end of this course, students will:		
NA1.01 substitute into and evaluate algebraic expressions involving exponents (i.e., evaluate expressions involving natural-number exponents with rational-number bases [e.g. evaluate $\left(\frac{3}{2}\right)^3$ by hand and $(9.83)^3$ by using a calculator]);	3.1, 3.2, throughout chapters 8 and 9	104–118 412–519
NA1.02 describe the relationship between the algebraic and geometric representations of a single-variable term up to degree three [i.e., length, which is one dimensional, can be represented by x ; area, which is two dimensional, can be represented by $(x)(x)$ or x^2 ; volume, which is three dimensional, can be represented by $(x)(x)(x)$, $(x^2)(x)$, or x^3];	3.1, 3.2	104–118
NA1.03 derive, through the investigation and examination of patterns, the exponent rules for multiplying and dividing monomials, and apply these rules in expressions involving one and two variables with positive exponents;	3.3	119–129
NA1.04 extend the multiplication rule to derive and understand the power of a power rule, and apply it to simplify expressions involving one and two variables with positive exponents.	3.3	119–129
<i>Manipulating Expressions and Solving Equations</i>		
By the end of this course, students will:		
NA2.01 simplify numerical expressions involving integers and rational numbers, with and without the use of technology;	throughout all chapters	
NA2.02 solve problems requiring the manipulation of expressions arising from applications of percent, ratio, rate, and proportion;	throughout all chapters	
NA2.03 relate their understanding of inverse operations to squaring and taking the square root, and apply inverse operations to simplify expressions and solve equations;	3.1, 3.2, 4.4	104–118, 220–229
NA2.04 add and subtract polynomials with up to two variables using a variety of tools;	3.4, 3.5, 3.6	130–159
NA2.05 multiply a polynomial by a monomial involving the same variable [e.g., $2x(x + 4)$, $2x^2(3x^2 - 2x + 1)$], using a variety of tools (e.g., algebra tiles, diagrams, computer algebra systems, paper and pencil);	3.7	160–169
NA2.06 expand and simplify polynomial expressions involving one variable, using a variety of tools;	3.7 throughout Ch 6	160–169, 292–355
NA2.07 solve first-degree equations, including equations with fractional coefficients, using a variety of tools (e.g., computer algebra systems, paper and pencil) and strategies (e.g., the balance analogy, algebraic strategies);	4.1, 4.2, 4.3	186–210
NA2.08 rearrange formulas involving variables in the first degree, with and without substitution (e.g., in analytic geometry, in measurement);	4.4 throughout Ch 6 and Ch 8	220–229, 292–355, 412–473

	Chapter/Section	Pages
NA2.09 solve problems that can be modelled with first-degree equations, and compare algebraic methods to other solution methods.	4.5	220–229

Linear Relations

Overall Expectations

By the end of this course, students will:

- ❖ apply data-management techniques to investigate relationships between two variables;
- ❖ demonstrate an understanding of the characteristics of a linear relation;
- ❖ connect various representations of a linear relation.

Specific Expectations

	Chapter/Section	Pages
<i>Using Data Management to Investigate Relationships</i>		
By the end of this course, students will:		
RE1.01 interpret the meanings of points on scatter plots or graphs that represent linear relations, including scatter plots or graphs in more than one quadrant [e.g., on a scatter plot of height versus age, interpret the point (13, 150) as representing a student who is 13 years old and 150 cm tall; identify points on the graph that represent students who are taller and younger than this student];	2.3, 2.5, 2.6	56–67, 77–94
RE1.02 pose problems, identify variables, and formulate hypotheses associated with relationships between two variables;	2.1, 2.5, 2.6	42–47, 77–94
RE1.03 design and carry out an investigation or experiment involving relationships between two variables, including the collection and organization of data, using appropriate methods, equipment, and/or technology (e.g., surveying; using measuring tools, scientific probes, the Internet) and techniques (e.g., making tables, drawing graphs);	2.2, 2.3, 2.6	48–67, 88–94
RE1.04 describe trends and relationships observed in data, make inferences from data, compare the inferences with hypotheses about the data, and explain any differences between the inferences and the hypotheses (e.g., describe the trend observed in the data. Does a relationship seem to exist? Of what sort? Is the outcome consistent with your hypothesis? Identify and explain any outlying pieces of data. Suggest a formula that relates the variables. How might you vary this experiment to examine other relationships?).	2.1, 2.3, 2.4, 2.5, 2.6	42–47, 56–94
<i>Understanding Characteristics of Linear Relations</i>		
By the end of this course, students will:		
RE2.01 construct tables of values, graphs, and equations, using a variety of tools (e.g., graphing calculators, spreadsheets, graphing software, paper and pencil), to represent linear relations derived from descriptions of realistic situations;	Throughout Ch 2, Ch 4, Ch 5, Ch 6	38–99, 182–359
RE2.02 construct tables of values, scatter plots, and lines or curves of best fit as appropriate, using a variety of tools (e.g., spreadsheets, graphing software, graphing calculators, paper and pencil), for linearly related and non-linearly related data collected from a variety of sources (e.g., experiments, electronic secondary sources, patterning with concrete materials);	2.3, 2.4, 2.5, 2.6, 5.1, 5.2, 5.5, 5.6	56–94, 238–253, 272–287
RE2.03 identify, through investigation, some properties of linear relations (i.e., numerically, the first difference is a constant, which represents a constant rate of change; graphically, a straight line represents the relation), and apply these properties to determine whether a relation is linear or non-linear;	2.5, 5.4, 5.5, 5.6	77–87, 264–287

	Chapter/Section	Pages
RE2.04 compare the properties of direct variation and partial variation in applications, and identify the initial value (e.g., for a relation described in words, or represented as a graph or an equation) ;	5.1, 5.2	238–253
RE2.05 determine the equation of a line of best fit for a scatter plot, using an informal process (e.g., using a movable line in dynamic statistical software; using a process of trial and error on a graphing calculator; determining the equation of the line joining two carefully chosen points on the scatter plot).	2.5, , 5.1, 5.5, 5.6, 7.3	77–87, 238– 245, 272–287, 384–393 ?
<i>Connecting Various Representations of Linear Relations</i>		
By the end of this course, students will:		
RE3.01 determine values of a linear relation by using a table of values, by using the equation of the relation, and by interpolating or extrapolating from the graph of the relation;	2.4, throughout Chapter 5	68–76, 234–291
RE3.02 describe a situation that would explain the events illustrated by a given graph of a relationship between two variables;	2.6, 5.1, 5.2, 5.4, 6.1, 6.2	88–94, 238–253, 272–278, 294–314
RE3.03 determine other representations of a linear relation, given one representation (e.g., given a numeric model, determine a graphical model and an algebraic model; given a graph, determine some points on the graph and determine an algebraic model);	2.5, 2.6, 5.1, 5.2, 5.5, 5.6	77–94, 236–253, 272–287
RE3.04 describe the effects on a linear graph and make the corresponding changes to the linear equation when the conditions of the situation the graph and equation represent are varied (e.g., given a partial variation graph and an equation representing the cost of producing a yearbook, describe how the graph changes if the cost per book is altered, describe how the graph changes if the fixed costs are altered, and make the corresponding changes to the equation).	5.1, 5.2	238–253

Analytic Geometry

Overall Expectations

By the end of this course, students will:

- ❖ determine the relationship between the form of an equation and the shape of its graph with respect to linearity and non-linearity;
- ❖ determine, through investigation, the properties of the slope and y-intercept of a linear relation;
- ❖ solve problems involving linear relations.

Specific Expectations

	Chapter/Section	Pages
<i>Investigating Relationships Between the Equation of a Relation and the Shape of its Graph</i>		
By the end of this course, students will:		
AG1.01 determine, through investigation, the characteristics that distinguish the equation of a straight line from the equations of nonlinear relations (e.g., use a graphing calculator or graphing software to graph a variety of linear and non-linear relations from their equations; classify the relations according to the shapes of their graphs; connect an equation of degree one to a linear relation);	5.5, 6.1	272–278, 296–307
AG1.02 identify, through investigation, the equation of a line in any of the forms $y = mx + b$, $Ax + By + C = 0$, $x = a$, $y = b$;	6.1, 6.2	296–314

	Chapter/Section	Pages
AG1.03 express the equation of a line in the form $y = mx + b$, given the form $Ax + By + C = 0$.	6.2	308–314
<i>Investigating the Properties of Slope</i>		
By the end of this course, students will:		
AG2.01 determine, through investigation, various formulas for the slope of a line segment or to determine the slope of a line segment or a line; (e.g., $m = \frac{\text{rise}}{\text{run}}$ $m = \frac{\text{the change in } y}{\text{the change in } x}$ or $m = \frac{\Delta y}{\Delta x}$, $m = \frac{y_2 - y_1}{x_2 - x_1}$ and use the formulas to determine the slope of a line segment or a line;	5.3, 5.4, 5.6	254–263
AG2.02 identify, through investigation with technology, the geometric significance of m and b in the equation $y = mx + b$;	6.1, 6.3 Use Technology, 6.4	296–307, 323–329?
AG2.03 determine, through investigation, connections among the representations of a constant rate of change of a linear relation (e.g., the cost of producing a book of photographs is \$50, plus \$5 per book, so an equation is $C = 50 + 5p$; a table of values provides the first difference of 5; the rate of change has a value of 5, which is also the slope of the corresponding line; and 5 is the coefficient of the independent variable, p , in this equation);	5.1, 5.2, 5.4, 5.6	238–253, 264–271, 279–287
AG2.04 identify, through investigation, properties of the slopes of lines and line segments (e.g., direction, positive or negative rate of change, steepness, parallelism, perpendicularity), using graphing technology to facilitate investigations, where appropriate.	6.1, 6.4 <5.3>	296–307, 323–329, <254–263>
<i>Using the Properties of Linear Relations to Solve Problems</i>		
By the end of this course, students will:		
AG3.01 graph lines by hand, using a variety of techniques (e.g., graph $y = x - 4$ using the y -intercept and slope; graph $2x + 3y = 6$ using the x - and y -intercepts);	Throughout Ch 6	292–355
AG3.02 determine the equation of a line from information about the line (e.g., the slope and y -intercept; the slope and a point; two points on a line);	<6.4>, 6.5, 6.6	330–343
AG3.03 describe the meaning of the slope and y -intercept for a linear relation arising from a realistic situation (e.g., the cost to rent the community gym is \$40 per evening, plus \$2 per person for equipment rental; the vertical intercept, 40, represents the \$40 cost of renting the gym; the value of the rate of change, 2, represents the \$2 cost per person), and describe a situation that could be modelled by a given linear equation (e.g., the linear equation $M = 50 + 6d$ could model the mass of a shipping package, including 50 g for the packaging material, plus 6 g per flyer added to the package);	<5.1, 5.2, 5.4, 5.6> throughout Ch 6	<238–253, 264–271, 279–287> 330–343
AG3.04 identify and explain any restrictions on the variables in a linear relation arising from a realistic situation (e.g., in the relation $C = 50 + 25n$, C is the cost of holding a party in a hall and n is the number of guests; n is restricted to whole numbers of 100 or less, because of the size of the hall, and C is consequently restricted to \$50 to \$2550);	5.1, 5.2 6.2, 6.3, 6.7	238–253, 308–322 344–351
AG3.05 determine graphically the point of intersection of two linear relations, and interpret the intersection point in the context of an application.	6.7	344–351

Measurement and Geometry

Overall Expectations

By the end of this course, students will:

- ❖ determine, through investigation, the optimal values of various measurements;
- ❖ solve problems involving the measurements of two-dimensional shapes and the surface areas and volumes of three-dimensional figures;
- ❖ verify, through investigation facilitated by dynamic geometry software, geometric properties and relationships involving two-dimensional shapes, and apply the results to solving problems.

Specific Expectations

<i>Investigating the Optimal Values of Measurements</i>		
By the end of this course, students will:		
MG1.01 determine the maximum area of a rectangle with a given perimeter by constructing a variety of rectangles, using a variety of tools (e.g., geoboards, graph paper, toothpicks, a pre-made dynamic geometry sketch), and by examining various values of the area as the side lengths change and the perimeter remains constant;	9.1, 9.2	478–490
MG1.02 determine the minimum perimeter of a rectangle with a given area by constructing a variety of rectangles, using a variety of tools (e.g., geoboards, graph paper, a premade dynamic geometry sketch), and by examining various values of the side lengths and the perimeter as the area stays constant;	9.1, 9.2	478–490
MG1.03 identify, through investigation with a variety of tools (e.g. concrete materials, computer software), the effect of varying the dimensions on the surface area [or volume] of square-based prisms and cylinders, given a fixed volume [or surface area];	9.3, 9.6	491–497, 510–515
MG1.04 explain the significance of optimal area, surface area, or volume in various applications (e.g., the minimum amount of packaging material; the relationship between surface area and heat loss);	9.3, 9.4, 9.5, 9.6	491–515
MG1.05 pose and solve problems involving maximization and minimization of measurements of geometric shapes and figures (e.g., determine the dimensions of the rectangular field with the maximum area that can be enclosed by a fixed amount of fencing, if the fencing is required on only three sides).	Throughout Ch 9	474–519
<i>Solving Problems Involving Perimeter, Area, Surface Area, and Volume</i>		
By the end of this course, students will:		
MG2.01 relate the geometric representation of the Pythagorean theorem and the algebraic representation $a^2 + b^2 = c^2$;	8.1	418–425
MG2.02 solve problems using the Pythagorean theorem, as required in applications (e.g., calculate the height of a cone, given the radius and the slant height, in order to determine the volume of the cone);	8.3, 8.4, 8.5	436–456
MG2.03 solve problems involving the areas and perimeters of composite two-dimensional shapes (i.e., combinations of rectangles, triangles, parallelograms, trapezoids, and circles);	8.2	426–435

<p>MG2.04 develop, through investigation (e.g., using concrete materials), the formulas for the volume of a pyramid, a cone, and a sphere (e.g., use three-dimensional figures to show that the volume of a pyramid [or cone] is 1/3 the volume of a prism [or cylinder] with the same base and height, and therefore that $V_{pyramid} = \frac{V_{prism}}{3}$ or $V_{pyramid} = \frac{(\text{area of base})(\text{height})}{3}$);</p>	<p>8.5, 8.6, 8.7</p>	<p>451–469</p>
<p>MG2.05 determine, through investigation, the relationship for calculating the surface area of a pyramid (e.g., use the net of a square based pyramid to determine that the surface area is the area of the square base plus the areas of the four congruent triangles);</p>	<p>8.3</p>	<p>436–443</p>
<p>MG2.06 solve problems involving the surface areas and volumes of prisms, pyramids, cylinders, cones, and spheres, including composite figures.</p>	<p>8.3, 8.4, 8.5, 8.6, 8.7</p>	<p>436–469</p>
<p><i>Investigating and Applying Geometric Relationships</i></p>		
<p>By the end of this course, students will:</p>		
<p>MG3.01 determine, through investigation using a variety of tools (e.g., dynamic geometry software, concrete materials), and describe the properties and relationships of the interior and exterior angles of triangles, quadrilaterals, and other polygons, and apply the results to problems involving the angles of polygons;</p>	<p>7.1, 7.2, 7.3</p>	<p>364–393</p>
<p>MG3.02 determine, through investigation using a variety of tools (e.g., dynamic geometry software, paper folding), and describe some properties of polygons (e.g., the figure that results from joining the midpoints of the sides of a quadrilateral is a parallelogram; the diagonals of a rectangle bisect each other; the line segment joining the midpoints of two sides of a triangle is half the length of the third side), and apply the results in problem solving (e.g., given the width of the base of an A-frame tree house, determine the length of a horizontal support beam that is attached half way up the sloping sides);</p>	<p>7.4, 7.5</p>	<p>394–407</p>
<p>MG3.03 pose questions about geometric relationships, investigate them, and present their findings, using a variety of mathematical forms (e.g., written explanations, diagrams, dynamic sketches, formulas, tables);</p>	<p>Throughout Ch 7</p>	<p>360–411</p>
<p>MG3.04 illustrate a statement about a geometric property by demonstrating the statement with multiple examples, or deny the statement on the basis of a counter-example, with or without the use of dynamic geometry software.</p>	<p>Throughout Ch 7</p>	<p>360–411</p>