

5

Surface Area

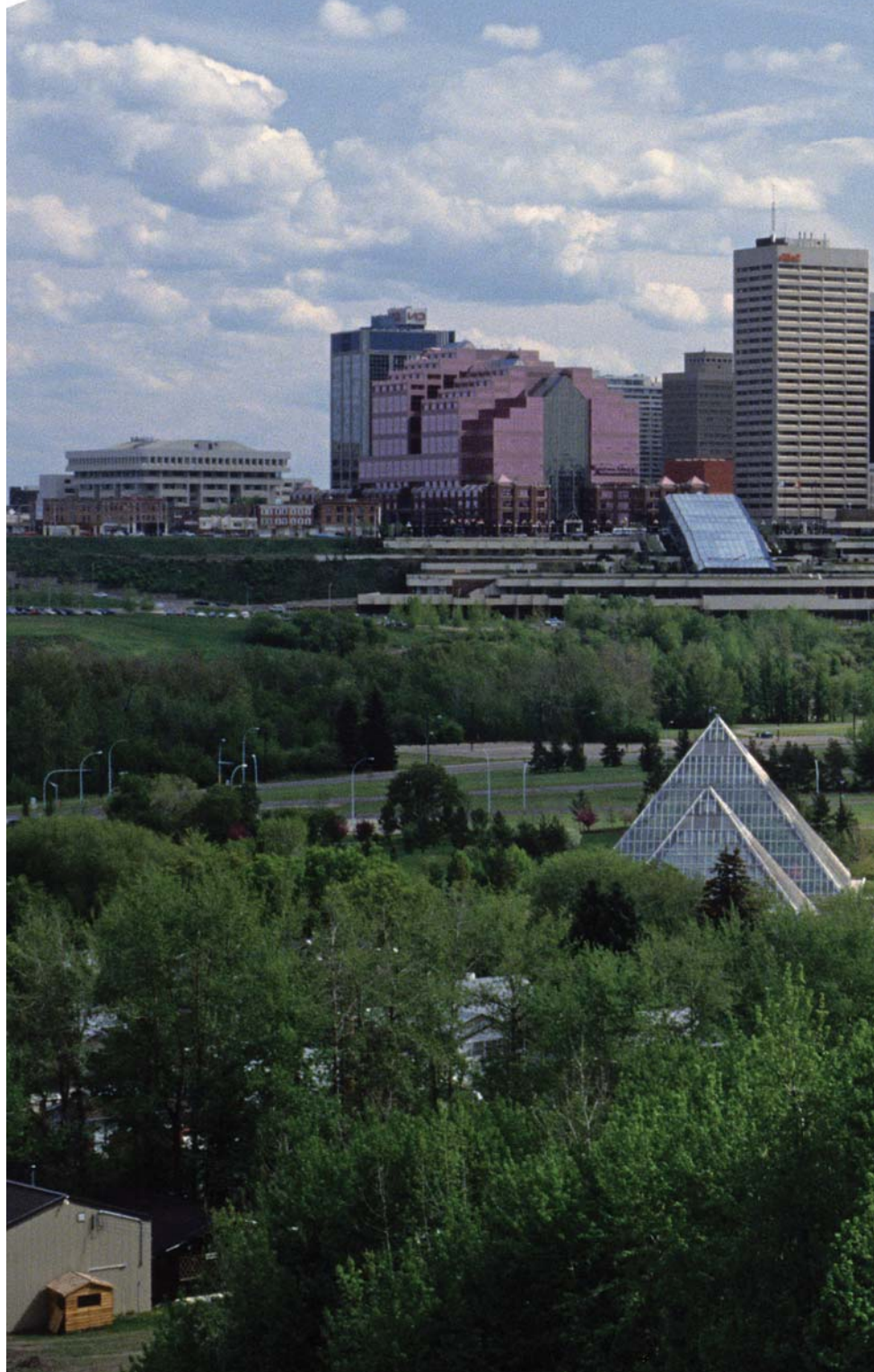
A skyline is a view of the outline of buildings or mountains shown on the horizon. You can see skylines during the day or at night, all over the world. Many cities have beautiful skylines. City planners have to consider much more than just how the skyline will look when they design a city.

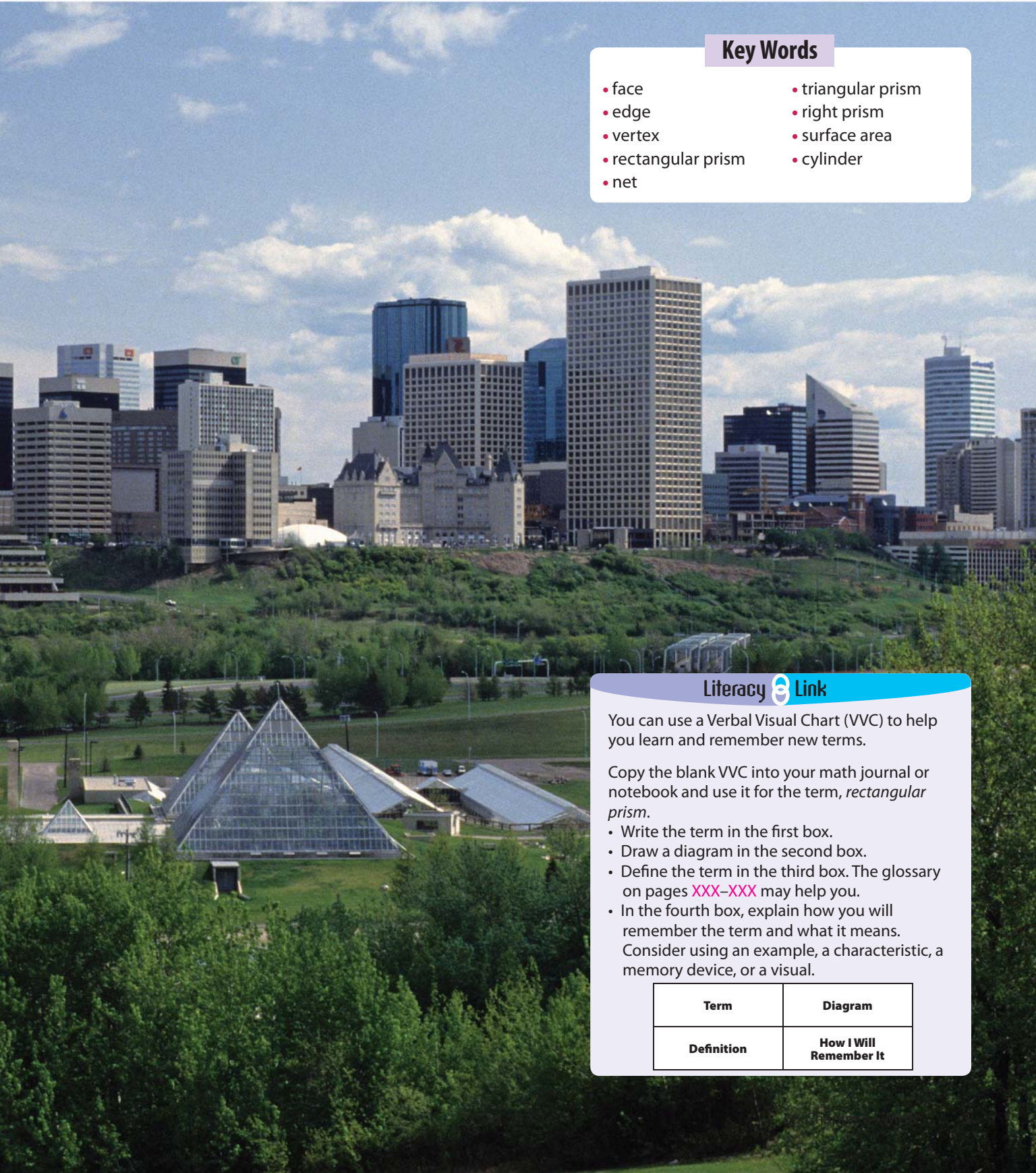
In the skyline shown in the picture, what shapes do you see? What three-dimensional objects can you identify?

In this chapter, you will learn how to draw and build three-dimensional objects and how to calculate their surface areas.

What You Will Learn

- to label and draw views of 3-D objects
- to draw and build nets for 3-D objects
- to calculate the surface area for prisms and cylinders
- to solve problems using surface area





Key Words

- face
- edge
- vertex
- rectangular prism
- net
- triangular prism
- right prism
- surface area
- cylinder

Literacy Link

You can use a Verbal Visual Chart (VVC) to help you learn and remember new terms.

Copy the blank VVC into your math journal or notebook and use it for the term, *rectangular prism*.

- Write the term in the first box.
- Draw a diagram in the second box.
- Define the term in the third box. The glossary on pages **XXX-XXX** may help you.
- In the fourth box, explain how you will remember the term and what it means. Consider using an example, a characteristic, a memory device, or a visual.

Term	Diagram
Definition	How I Will Remember It

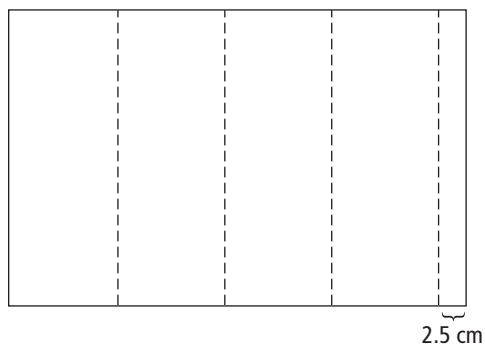
Making The Foldable

Materials

- 11 × 17 sheet of paper
- ruler
- glue or tape
- four sheets of blank paper
- scissors
- stapler

Step 1

Fold over one of the short sides of an 11 × 17 sheet of paper to make a 2.5 cm tab. Fold the remaining portion of paper into quarters.



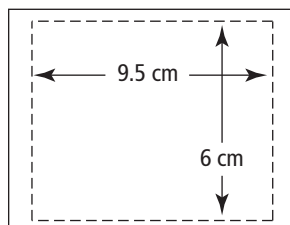
Step 2

Use glue or tape to put the paper together as shown in the diagram. If you use glue, allow it to dry completely.



Step 3

Fold each of four sheets of blank paper into eighths. Trim the edges as shown so that each individual piece is 9.5 cm × 6 cm. Cut off all folded edges.

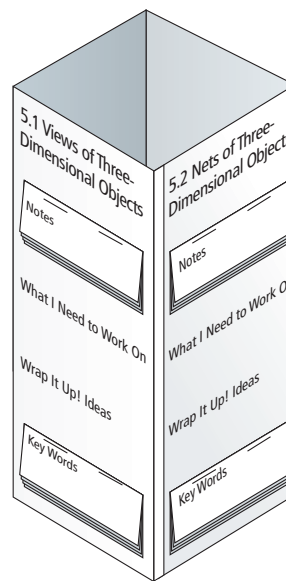


Step 4

Make the paper from Step 3 into eight booklets of 4 pages each.

Step 5

Collapse the Foldable. Title the faces of your Foldable. Then, staple the booklets onto each face, as shown, and add the labels shown.



Using the Foldable

As you work through each section of Chapter 5, take notes on the appropriate face of your Foldable. Include information about the examples and Key Ideas in the Notes section. If you need more room, add sheets of paper to your booklet.

List and define the key words in the Key Words booklet. Use visuals to help you remember the terms.

Keep track of what you need to work on. Check off each item as you deal with it.

As you think of ideas for the Wrap It Up!, record them on that section of each face of your Foldable.

MATH LINK

City Planning

When city planners design communities, they consider the purpose of the buildings, the width of the streets, the placement of street signs, the design and placement of lampposts, and many other items found in a city.

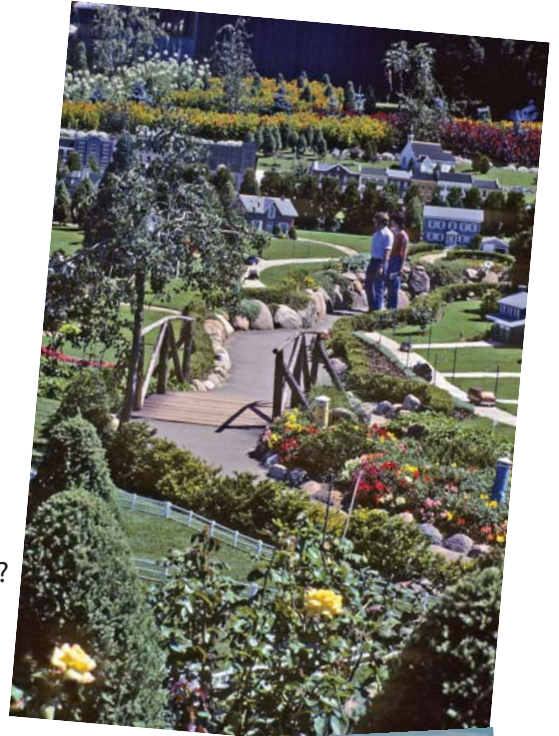
Communication and cooperation are keys to being successful, because city planners have to coordinate and work with many other people.

Imagine that you are a city planner for a miniature community.

Discuss your answers to #1 and #2 with a partner, then share with your class.

- a)** What buildings are essential to a new community?
b) What different shapes are the faces of these buildings?
- What other items are important to include in a community?
- Using grid paper, sketch all or part of an aerial view of a community including the essential buildings your class discussed. Make sure to include roads and any other features that are important.

In this chapter, you will work in groups to create and design a miniature community.



5.1

Views of Three-Dimensional Objects

Focus on...

After this lesson, you will be able to...

- draw and label top, front, and side views of 3-D objects
- build 3-D objects when given top, front, and side views

Materials

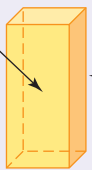
- 20 unit blocks
- masking tape
- isometric dot paper

Literacy Link

To describe a three-dimensional (3-D) object, count its *faces*, *edges*, and *vertices*.

Face: flat or curved surface

Edge: line segment where two faces meet



Vertex: point where three or more edges meet

<Ill 5-1: illustration of two students split view; one girl making an object with unit blocks, one boy making a DIFFERENT object with the same number of unit blocks. Bubbles with dialogue, girl (Sable): "I used ten blocks" (or how ever many is in the picture), boy (Josh): "Sable, what does yours look like if you look at it from the top?">

Sable and Josh are trying to build exactly the same three-dimensional (3-D) object. They each have the same number of blocks, but they cannot see each other's object.

Using a common vocabulary can help Sable and Josh build the same object.

Explore the Math

How can you describe and build three-dimensional objects?

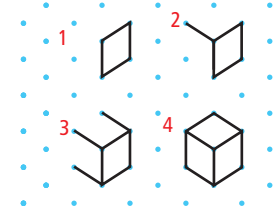
1. Work with a partner. Create a 3-D object using ten unit blocks. Make sure your partner cannot see your object.
2. Describe your completed object to your partner, and have your partner try to build the same object. What key words did you use that were helpful?
3. Decide which faces will be the front and top of your object. Then determine which faces are the bottom, left side, right side, and back. You may wish to label the faces with tape. Then, describe your object to your partner again. Was it easier to describe this time?

4. Using isometric dot paper, draw what your object looks like.

Reflect on Your Findings

5. a) Do you need to know all the views to construct an object? If not, which ones would you use and why?
- b) Explain why you might need to have only one side view, if the top and front views are also given.
- c) Are any other views unnecessary? Are they needed to construct the same object?

Using isometric dot paper makes it easier to draw 3-D shapes. Follow the steps to draw a rectangular solid.



Each view shows two dimensions. When combined, these views create a 3-D diagram.

Example 1: Draw and Label Top, Front, and Side Views

Using blank paper, draw the top, front, and side views of these items. Label each view.

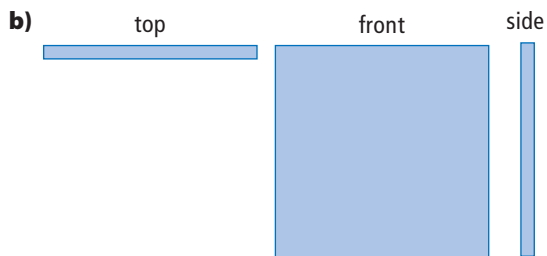
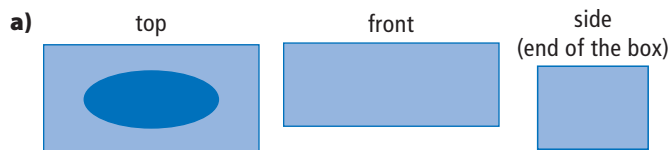
a) Tissue box



b) Compact disk case

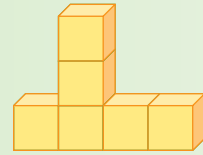


Solution



Show You Know

Using blank paper, draw the top, front, and side views of this object.

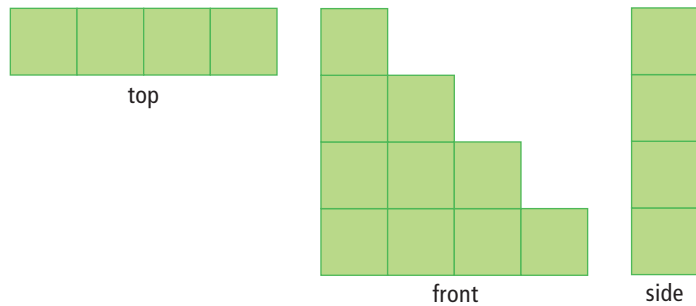


Did You Know?

Architects use top views to draw blueprints for buildings.

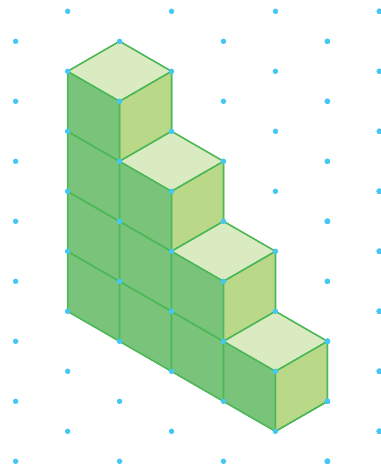
Example 2: Sketch a Three-Dimensional Object When Given Views

These views were drawn for an object made of ten blocks. Sketch what the object looks like.



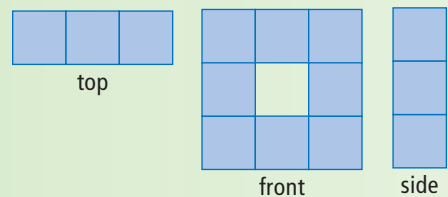
Solution

Use isometric dot paper to sketch the object.



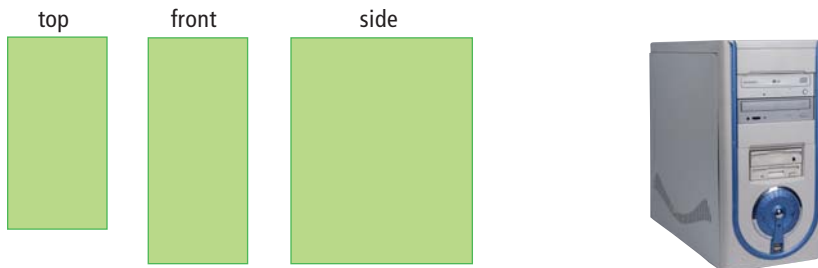
Show You Know

An object is created using eight blocks. It has the following top, front, and side views. Sketch what the object looks like on isometric dot paper.

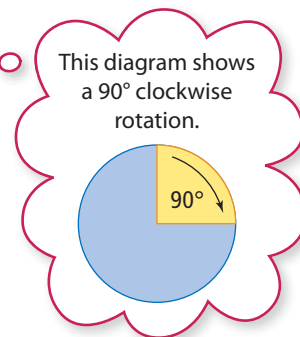


Example 3: Predict and Draw the Top, Front, and Side Views After a Rotation

The diagrams show the top, front, and side views of the computer tower.

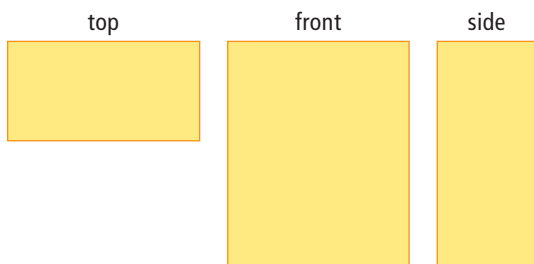


You want to rotate the computer tower 90° clockwise on its base to fit into your new desk. Predict which view you believe will become the front view after the rotation. Then, draw the top, front, and side views after rotating the tower.



Solution

The original side view will become the new front view after the rotation.



Tech Link

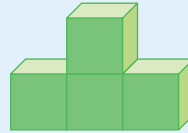
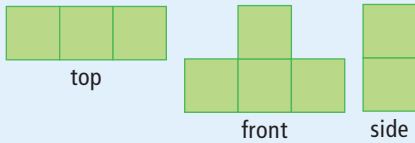
You can use a Draw program to create 3-D objects.

Show You Know

Stand your *MathLinks 8* textbook on your desk. Predict what the top, front, and side views will look like if you rotate it 90° clockwise about its spine. Then, draw the top, front, and side views after rotating the textbook.

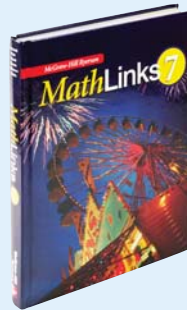
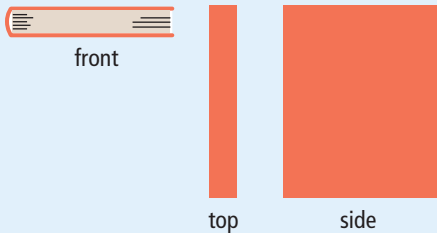
Key Ideas

- A minimum of three views are needed to describe a 3-D object.
- Using the top, front, and side views, you can build or draw a 3-D object.



Communicate the Ideas

1. Raina insists that you need to tell her all six views so she can draw your object. Is she correct? Explain why or why not.
2. Are these views correct? Justify your answer.

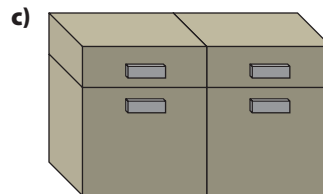
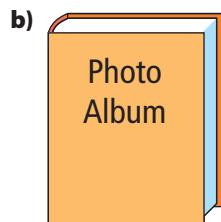
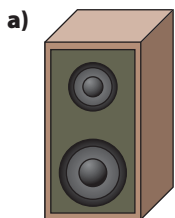


Check Your Understanding

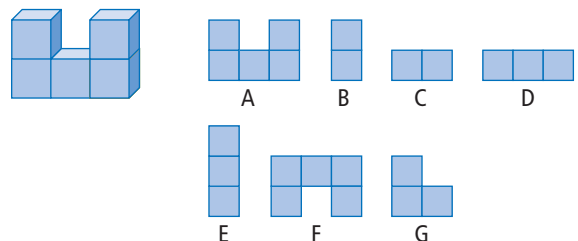
Practise

For help with #3 and #4, refer to Example 1 on page XXX.

3. Sketch and label the top, front, and side views.

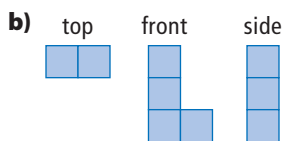


4. Choose the correct top, front, and side view for this object and label each one.



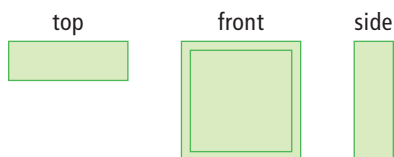
For help with #5, refer to Example 2 on page xxx.

5. Draw each 3-D object using the views below.



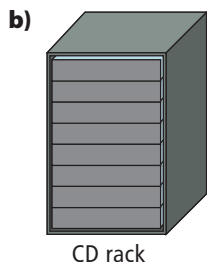
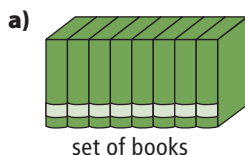
For help with #6 and #7, refer to Example 3 on page xxx.

6. A television set has the following views.



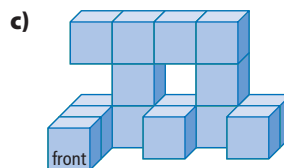
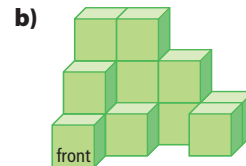
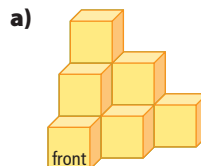
If you turn the television 90° counterclockwise, how would the three views change? Sketch and label each new view.

7. Choose which object has a front view like this after a rotation of 90° clockwise onto its side.



Apply

8. Choose two 3-D objects from your classroom. Sketch the top, front, and side views for each one.
9. Sketch the front, top, and right side views for these solids.



Extend

10. Describe two objects that meet this requirement: When you rotate one object 90° degrees, the top, front, and side views are the same as the top, front, and side views of the other object that was not rotated.
11. An injured bumblebee sits at a vertex of a cube with edge length 1 m. The bee moves along the edges of the cube and comes back to the original vertex without visiting any other vertex twice.
- a) Draw diagrams to show the bumblebee's trip around the cube.
- b) What is the length, in metres, of the longest trip?

MATH LINK

Choose one of the essential buildings that you discussed for your new community on page xxx. Draw and label a front, side, and top view.

5.2

Nets of Three-Dimensional Objects

Focus on...

After this lesson, you will be able to...

- determine the correct nets for 3-D objects
- build 3-D objects from nets
- draw nets for 3-D objects

rectangular prism

- a prism whose bases are congruent rectangles

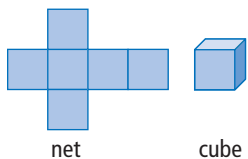


Materials

- grid paper
- scissors
- clear tape
- rectangular prisms (blocks of wood, cardboard boxes, unit blocks)

net

- a two-dimensional shape that, when folded, encloses a 3-D object

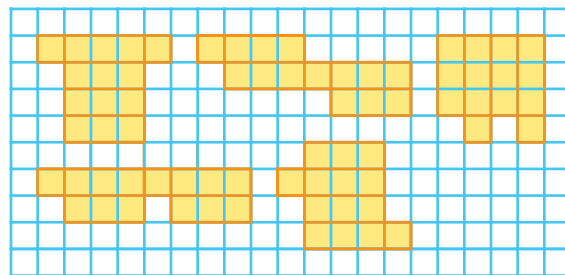
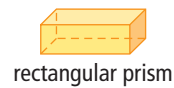


Shipping containers help distribute materials all over the world. Items can be shipped by boat, train, or transport truck to any destination using these containers. Shipping containers are right **rectangular prisms**. Why do you think this shape is used?

Explore the Math

How do you know if a net can build a right rectangular prism?

Here are a variety of possible **nets** for a right rectangular prism.



1. Draw each net on grid paper.

Literacy Link

A *right prism* has sides that are perpendicular to the bases of the prism.

2. Predict which nets will form a right rectangular prism.
3. Cut each net out along the outside edges and fold along the inside edges, taping the cut edges to try to form a right rectangular prism.
4. Do all the nets create right rectangular prisms?
5. Place a right rectangular prism (such as a small cardboard box) on a piece of blank paper. “Roll” the prism onto its faces, trace each face, and try to draw another correct net. Your net should be different from the examples you have already made.

Reflect on Your Findings

6. a) Compare the net you drew with those of three of your classmates. What is the same and different about your nets?
- b) Is there more than one way to draw a net for a 3-D object? Explain your answer.

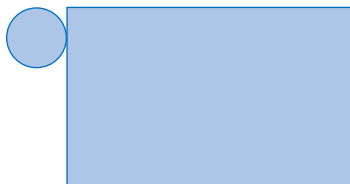
Example 1: Draw a Net for a Three-Dimensional Object

A company asks you to create an umbrella stand for large beach umbrellas. Draw the net for the umbrella stand.



Solution

Visualize what the umbrella stand would look like if you could cut it open and flatten it. The net has one circle and a rectangle. When the rectangle is curved around the circle, the net will form a cylinder with an open top. The width of the rectangle is equal to the circumference of the circle.



Show You Know

Draw a net for an unopened soup can.

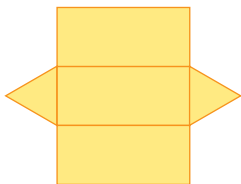
Strategies

Change Your Point of View

Refer to page xxx.

Example 2: Build a Three-Dimensional Object From a Given Net

Before going to leadership camp, your group needs to put a tent together. Can this net be folded to form the shape of a tent?



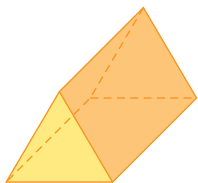
Strategies

Model It

Refer to page xxx.

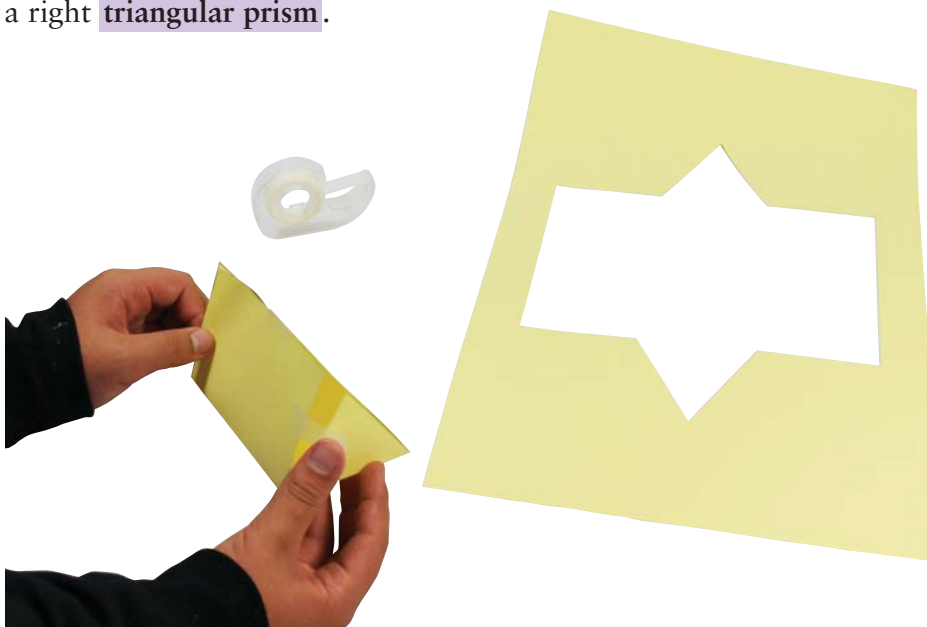
triangular prism

- a prism with two triangular bases each the same size and shape



Solution

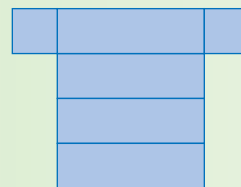
Trace the net onto paper. Cut along the outside edges and fold along the inside edges. Tape the cut edges together to try to build a right **triangular prism**.



The net can be folded to form the shape of a tent.

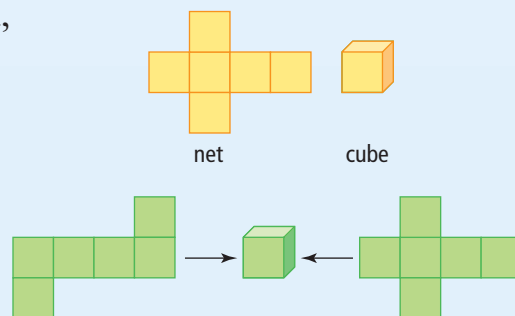
Show You Know

Build a 3-D object using this net. What object does it make?



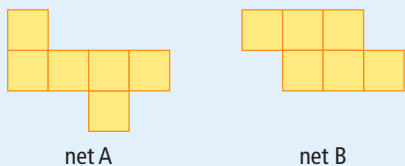
Key Ideas

- A net is a two-dimensional shape that, when folded, encloses a three-dimensional object.
- The same 3-D object can be created by folding different nets.
- You can draw a net for an object by visualizing what it would look like if you cut along the edges and flattened it out.



Communicate the Ideas

1. Both of these nets have six faces, like a cube. Will both nets form a cube? Justify your answer.



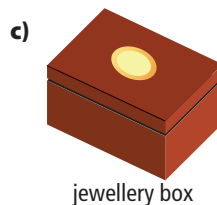
2. Patricia is playing the lead role in the school musical this year. She missed Math class while she was performing. She cannot figure out if a net will build the correct 3-D object, and asks you for help after school. Show how you would help her figure out this problem.

Check Your Understanding

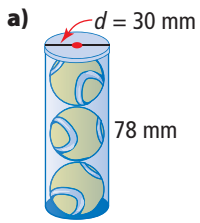
Practise

For help with #3 to #5, refer to Example 1 on page xxx.

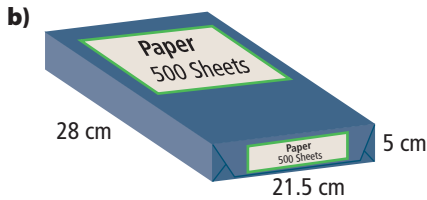
3. Sketch a net for each object.



4. Draw the net for each object. Label the measurements on the net.



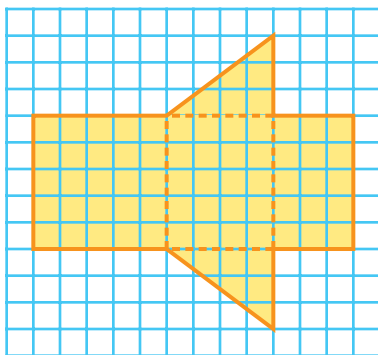
Did You Know?
A ream describes a quantity of approximately 500 sheets of paper.



5. Draw a net on grid paper for a rectangular prism with the following measurements: length is six units, width is four units, and height is two units.

For help with #6 and #7, refer to Example 2 on page xxx.

6. a) Draw the net on grid paper, as shown. Cut along the outside edges of the net and fold to form a 3-D object.

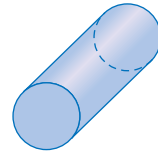


b) What is this object called?

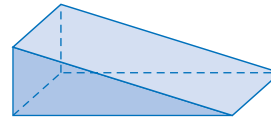
7. Match each solid with its net. Copy the nets, then try to create the 3-D objects.



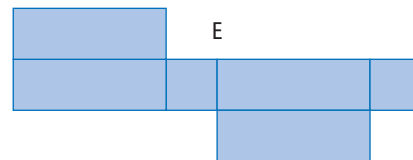
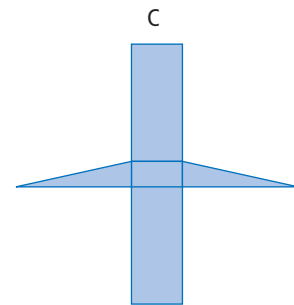
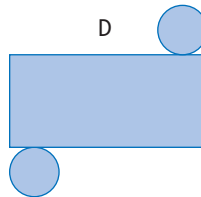
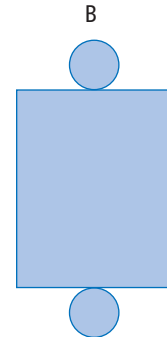
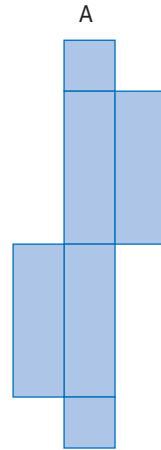
rectangular prism



cylinder



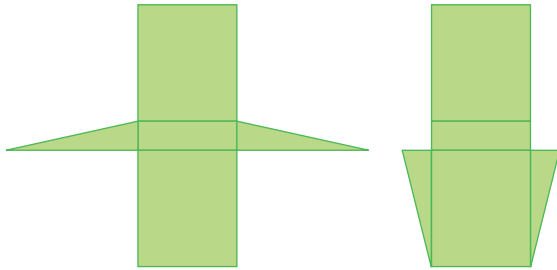
triangular prism



Apply

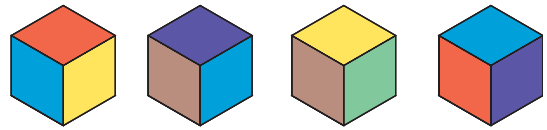
- A box of pens measures 15.5 cm by 7 cm by 2.5 cm. Draw a net for the box on a piece of centimetre grid paper. Then, cut it out and fold it to form the box.
- You are designing a new mailbox. Draw a net of your creation. Include all measurements.

10. Angela designed two nets.



- a) Enlarge both nets on grid paper, and build the 3-D objects they form.
b) What object does each net form?

12. The six sides of a cube are each a different colour. Four of the views are shown below.



What colour is on the opposite side of each of these faces?

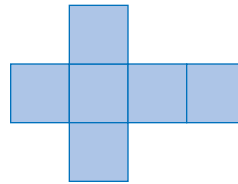
- a) purple
b) blue
c) red

Extend

11. Hannah and Dakota design a spelling board game. They use letter tiles to create words. Tiles may be stacked (limit of four) on top of letters already used for a word on the board to form a new word.

- a) Draw a 3-D picture of what these stacked tiles might look like.
b) Draw a top view that illustrates the stacked tiles for people reading the instructions.

13. How many possible nets can create a cube? Sketch all of them. The first one is done for you.



MATH LINK

When buildings are designed, it is important to consider engineering principles, maximum and minimum height requirements, and budget.

- a) Create a 3-D sketch of two buildings for your miniature community, one that is a prism and one that is a cylinder.
b) Draw a net of each building, including all possible measurements needed to build your miniature.



5.3

Surface Area of a Prism

Focus on...

After this lesson, you will be able to...

- link area to surface area
- find the surface area of a right prism



Most products come in some sort of packaging. You can help conserve energy and natural resources by purchasing products that

- are made using recycled material
- use recycled material for packaging
- do not use any packaging

What other ways could you reduce packaging?

Explore the Math

Materials

- empty cardboard box (cereal box, granola box, snack box, etc.)
- scissors
- ruler
- scrap paper

Literacy Link

The dimensions of an object are measures such as length, width, and height.

How much cardboard is needed to make a package?

1. Choose an empty cardboard box.
 - a) How many faces does your box have?
 - b) Identify the shape of each face.
2. Cut along the edges of the box and unfold it to form a net.



Exclude overlapping flaps.

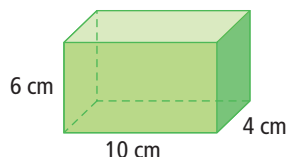
3. What are the dimensions and area of each face?
4. How can you find the amount of material used to make your cardboard box?

Reflect on Your Findings

5. a) How did you use the area of each face to calculate the total amount of material used to make your cardboard box?
- b) Can you think of a shorter way to find the total area without having to find the area of each face? Explain your method.

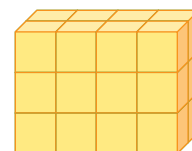
Example 1: Calculate the Surface Area of a Right Rectangular Prism

- a) Draw the net of this right rectangular prism.
- b) What is the area of each face?
- c) What is the **surface area** of the prism?



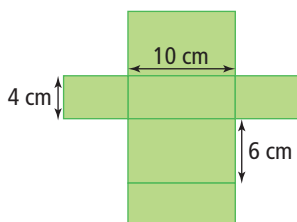
surface area

- the number of square units needed to cover a 3-D object
- the sum of the areas of all the faces of an object

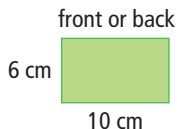


Solution

a)



- b) The right rectangular prism has faces that are three different sizes.

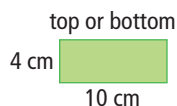


$$A = l \times w$$

$$A = 10 \times 6$$

$$A = 60$$

The area of the front or back is 60 cm^2 .

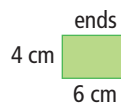


$$A = l \times w$$

$$A = 10 \times 4$$

$$A = 40$$

The area of the top or bottom is 40 cm^2 .



$$A = l \times w$$

$$A = 6 \times 4$$

$$A = 24$$

The area of each end is 24 cm^2 .

Area is measured in square units. For example, square centimetres, square metres, etc.

- c) The total surface area is the sum of the areas of all the faces.

The front and back have the same area:

$$A = 60 \times 2$$

$$A = 120$$

The top and bottom have the same area:

$$A = 40 \times 2$$

$$A = 80$$

The two ends have the same area:

$$A = 24 \times 2$$

$$A = 48$$

$$\begin{aligned} \text{Total surface area} &= (\text{area of front and back}) + (\text{area of top and bottom}) \\ &\quad + (\text{area of ends}) \\ &= 120 + 80 + 48 \\ &= 248 \end{aligned}$$

The surface area of the right rectangular prism is 248 cm^2 .

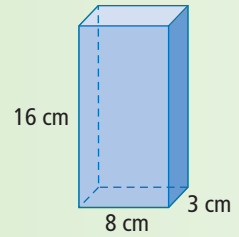
You could add the areas you calculated first. $60 + 40 + 24 = 124$

Each area is the same as the area of one other face, so you could then multiply the total by two. $124 \times 2 = 248$



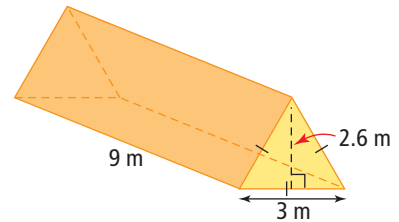
Show You Know

What is the surface area of this right rectangular prism?



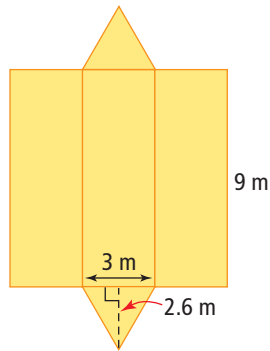
Example 2: Calculate the Surface Area of a Right Triangular Prism

- Draw the net of this right triangular prism.
- What is the area of each face?
- What is the total surface area?



Solution

a)



Strategies

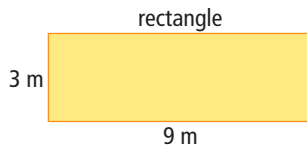
Draw a Diagram

Refer to page xxx.

Literacy Link

An equilateral triangle has three equal sides and three equal angles. Equal sides are shown on diagrams by placing tick marks on them.

- The bases of the prism are equilateral triangles. The sides of the prism are rectangles.

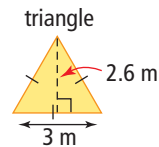


$$A = l \times w$$

$$A = 9 \times 3$$

$$A = 27$$

The area of one rectangle is 27 m^2 .



$$A = (b \times h) \div 2$$

$$A = (3 \times 2.6) \div 2$$

$$A = 7.8 \div 2$$

$$A = 3.9$$

The area of one triangle is 3.9 m^2 .

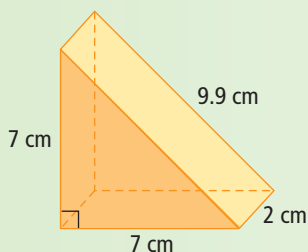
- c) You must add the areas of all faces to find the surface area.
 This right triangular prism has five faces.
 There are three rectangles of the same size and two triangles of the same size.

$$\begin{aligned} \text{Total surface area} &= (3 \times \text{area of rectangle}) + (2 \times \text{area of triangle}) \\ &= (3 \times 27) + (2 \times 3.9) \\ &= 81 + 7.8 \\ &= 88.8 \end{aligned}$$

The surface area of the right triangular prism is 88.8 m².

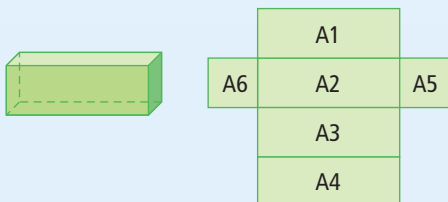
Show You Know

Find the surface area of this triangular prism.



Key Ideas

- Surface area is the sum of the areas of all the faces of a 3-D object.



Surface Area = $A1 + A2 + A3 + A4 + A5 + A6$,
 where $A1$ represents the area of rectangle 1, $A2$ represents the area of rectangle 2, etc.

Communicate the Ideas

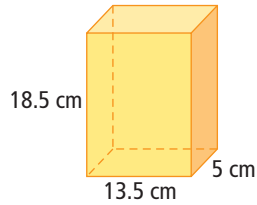
1. Write a set of guidelines that you could use to find the surface area of a prism. Share your guidelines with a classmate.
2. A right rectangular prism has six faces. Why do you have to find the area of only three of the faces to be able to find the surface area. Use pictures and words to explain your thinking.

Check Your Understanding

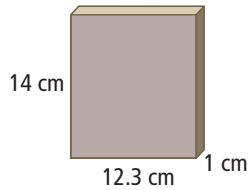
Practise

For help with #3 and #4, refer to Example 1 on page xxx.

3. Find the surface area of this right rectangular prism to the nearest tenth of a square centimetre.

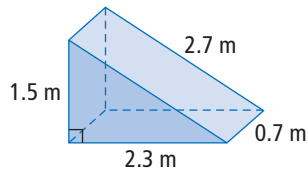


4. Find the surface area of this CD case.



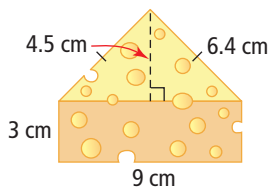
For help with #5 to #7, refer to Example 2 on page xxx.

5. Calculate the surface area of this ramp in the shape of a right triangular prism. Give your answer to the nearest tenth of a square metre.



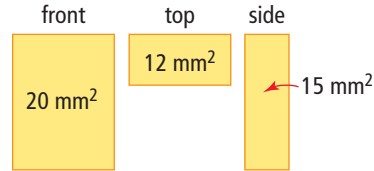
Apply

6. Cheese is sometimes packaged in a triangular box. How much cardboard would you need to cover this piece of cheese if you do not include overlapping? Calculate your answer to the nearest tenth of a square centimetre.

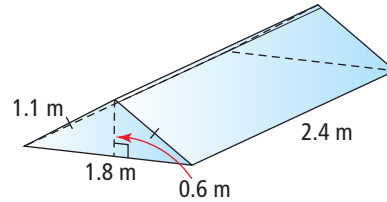


The tick marks on the two sides of the triangle indicate that these sides are equal.

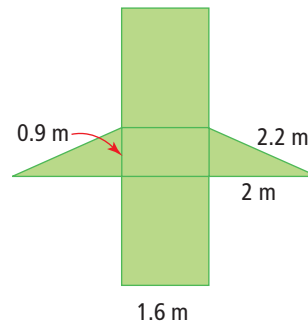
7. Given the area of each face of a right rectangular prism, what is the surface area?



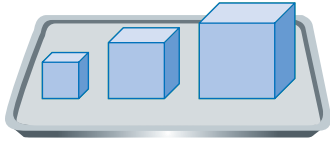
8. Paco builds a glass greenhouse.



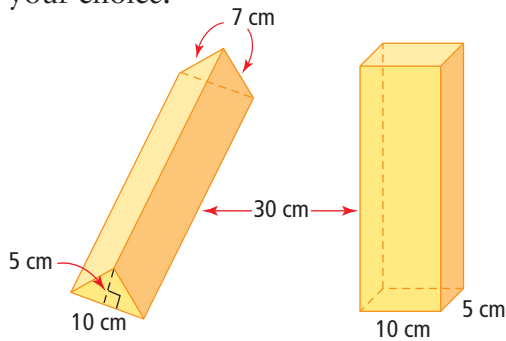
- How many glass faces does the greenhouse have?
 - How much glass does Paco need to buy?
9. What is the minimum amount of material needed to make the cover of this textbook if there is no overlap? Give your answer to the nearest square millimetre.
10. Jay wants to make a bike ramp. He draws the following sketch. What is the surface area of the ramp?



11. Dallas wants to paint three cubes. The cubes measure $1\text{ m} \times 1\text{ m} \times 1\text{ m}$, $2\text{ m} \times 2\text{ m} \times 2\text{ m}$, and $3\text{ m} \times 3\text{ m} \times 3\text{ m}$, respectively. What total surface area will Dallas paint if he decides not to paint the bottoms of the three cubes?



12. Tadika has a gift to wrap. Both of these containers will hold her gift. Which container would allow her to use the least amount of wrapping paper? Explain your choice.



Extend

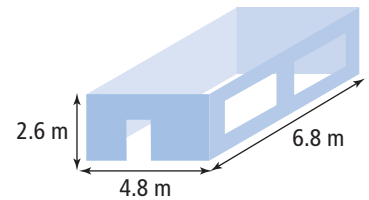
13. A square cake pan measures 30 cm on each side and is 5 cm deep. Cody wants to coat the inside of the pan with non-stick oil. If a single can of non-stick oil covers an area of $400\,000\text{ cm}^2$, how many pans can be coated with a single can?

14. Ethan is hosting games night this weekend. He bought ten packages of playing cards. Each package measures $9\text{ cm} \times 6.5\text{ cm} \times 1.7\text{ cm}$. He wants to build a container to hold all ten packages of cards.

- a) What are the minimum inside dimensions of the container?
b) Is there more than one kind of container that would work? Draw diagrams to help explain your answer.

15. a) If the edge length of a cube is doubled, find the ratio of the old surface area to the new surface area.
b) What happens if the edge length of a cube is tripled? Is there a pattern?

16. Shelby wants to paint the walls and ceiling of a rectangular room.



Type of Paint	Size of Paint Can	Cost
Wall paint	4 L	\$24.95
	1 L	\$7.99
Ceiling paint	4 L	\$32.95

One litre of paint covers 9.5 m^2 .

- a) What is the least amount of paint Shelby can buy to paint the room (subtract 5 m^2 for the door and windows)?
b) How much will the paint cost, including the amount of tax charged in your region?

MATH LINK

For the prism-shaped building you created in the Math Link on page XXX, how much material do you need to cover the exterior walls and the roof of the building?

5.4

Surface Area of a Cylinder

Focus on...

After this lesson, you will be able to...

- find the surface area of a cylinder



Glow sticks work because of a chemical reaction. There are two solutions in separate compartments inside the stick. Once you bend the stick, the two solutions mix. This mixture creates a new solution that gives off light. The colour of the glow stick depends on the dye in the mixture. How might you determine how much plastic would be needed to make a glow stick to fit around your wrist?

Explore the Math

cylinder

- a three-dimensional object with two parallel and congruent circular bases



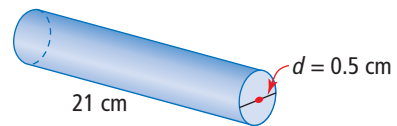
cylinder

Tech Link

If your calculator has a π key, you can use it to get a more accurate answer.

How do you find the surface area of a right cylinder?

- Draw the net of a glow stick. Use the actual dimensions from the diagram shown.
- List the shapes that make up your net.
- a) Copy and complete the table.



Use 3.14 as an approximate value for π .

The radius of a circle is one half the diameter.

Area Formula	Measurements	
Circle: $A = \blacksquare \times \blacksquare$	$\pi = 3.14$	$r = \blacksquare$
Rectangle: $A = \blacksquare \times \blacksquare$	$l = \blacksquare$	$w = \blacksquare$

- What measurement are you missing to calculate the area of each shape? Use your piece of paper as a model of a glow stick to help you visualize what might be missing.
- How can you use what you know about circles to help you find the missing measurement?

4. a) The cylinder has two identical circles, one at each end.
What is the area of each circle?
- b) What is the area of the rectangle?
- c) The total surface area is the sum of the areas of all the shapes.
What is the surface area of the glow stick? Include the units in your final answer.

Reflect on Your Findings

5. a) How would you find the surface area of any right cylinder?
- b) What type of units do you use to measure surface area?

Example 1: Determine the Surface Area of a Right Cylinder

- a) Estimate the surface area of the can.
- b) What is the surface area of the can? Express your answer to the nearest hundredth of a square centimetre?



Solution

The surface area of the can is found by adding the areas of the two circular bases and the rectangular side that surrounds them.

The width, w , of the rectangle is the height of the can.

The length, l , of the rectangle is equal to the circumference of the circle.

- a) To estimate, use approximate values: $d \approx 8$ cm, $w \approx 10$ cm, $\pi \approx 3$.

$$\begin{aligned} \text{Area of circle} &= \pi \times r^2 \\ &\approx 3 \times 4 \times 4 \\ &\approx 48 \end{aligned}$$

r^2 means
 $r \times r$

The radius of a circle
is half the diameter.

$$\text{There are two circles: } 2 \times 48 = 96$$

The area of the two circles is approximately 96 cm^2 .

$$\begin{aligned} \text{Area of rectangle} &= l \times w \\ &= (\pi \times d) \times w && \text{Replace } l \text{ with the formula for the} \\ &\approx 3 \times 8 \times 10 && \text{circumference of a circle.} \\ &\approx 240 \end{aligned}$$

The area of the rectangle is approximately 240 cm^2 .

$$\begin{aligned} \text{Estimated surface area} &= \text{area of two circles} + \text{area of rectangle} \\ &\approx 96 + 240 \\ &\approx 340 \end{aligned}$$

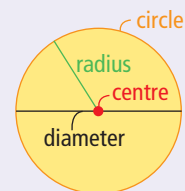
The estimated surface area is 340 cm^2 .

Did You Know?

Pop cans are cylinders. The world's largest Coke™ can is located in Portage la Prairie, Manitoba.



Literacy Link



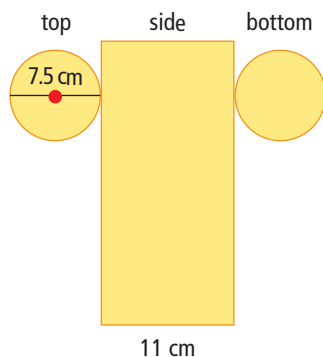
The formula for the circumference of a circle is $C = \pi \times d$ or $C = 2 \times \pi \times r$.

Strategies**Draw a Diagram**

Refer to page xxx.

b) Method 1: Use a Net

Draw the net and label the measurements.



The diameter of the circle is 7.5 cm.

Determine the radius.

$$7.5 \div 2 = 3.75$$

The radius of the circle is 3.75 cm.

Find the area of one circle.

$$A = \pi \times r^2$$

$$A \approx 3.14 \times 3.75^2$$

$$A \approx 44.15625$$

The area of one circle is approximately 44.15625 cm².Use 3.14 as an approximate value for π .

Find the area of two circles.

$$2 \times 44.15625 = 88.3125$$

The area of both circles is approximately 88.3125 cm².

Find the area of the rectangle using the circumference of the circle.

$$A = l \times w$$

$$A = (\pi \times d) \times w \quad \text{Replace } l \text{ with the formula for the circumference of a circle.}$$

$$A \approx 3.14 \times 7.5 \times 11$$

$$A \approx 259.05$$

The area of the rectangle is approximately 259.05 cm².

Calculate the total surface area.

$$\text{Total surface area} = 88.3125 + 259.05$$

$$= 347.3625$$

The total surface area is approximately 347.36 cm².

Round your answer at the end of the calculation.

Method 2: Use a Formula.

Use this formula to find the total surface area of any cylinder.

$$\begin{aligned} S.A. &= 2 \times (\pi \times r^2) + (\pi \times d \times h) \\ S.A. &\approx 2 \times (3.14 \times 3.752) + (3.14 \times 7.5 \times 11) \\ S.A. &\approx 88.3125 + 259.05 \\ S.A. &\approx 347.3625 \end{aligned}$$

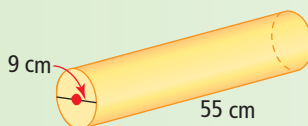
The total surface area is 347.36 cm², to the nearest hundredth.

This formula incorporates each shape and its area formula to find the surface area.

$$\begin{array}{l} 2 \times (\pi \times r^2) + (\pi \times d) \times h \\ \text{two circles} \quad \text{circle area} \quad \text{rectangle area} \\ \text{formula} \quad \text{formula (length is the} \\ \text{circumference of a circle;} \\ \text{width is the height of} \\ \text{the cylinder)} \end{array}$$

Show You Know

Calculate the surface area of this cylinder to the nearest tenth of a square centimetre.



Literacy Link

The abbreviation S.A. is often used as a short form for surface area.

Example 2: Use the Surface Area of a Cylinder

Calculate the surface area of this totem pole, including the two circular bases. The pole stands 2.4 m tall and has a diameter of 0.75 m. Give your answer to the nearest hundredth of a square metre.

Solution

The cylinder has two circular bases.

The area of one circle is:

$$\begin{aligned} A &= \pi \times r^2 \\ A &\approx 3.14 \times 0.375^2 \end{aligned}$$

$$r = d \div 2$$

The area of the circle is approximately 0.4415625 m².

There are two circles, so the area of both circles is approximately 0.883125 m².

Calculate the total surface area.

$$\begin{aligned} S.A. &\approx 0.883125 + 5.652 \\ S.A. &\approx 6.535125 \end{aligned}$$

The total surface area is approximately 6.54 m².

The side of the cylinder is a rectangle.

The area of the rectangle is:

$$\begin{aligned} A &= (\pi \times d) \times h \\ A &\approx 3.14 \times 0.75 \times 2.4 \\ A &\approx 5.652 \end{aligned}$$

The area of the rectangle is approximately 5.652 m².

Replace one dimension with the formula for the circumference of a circle.



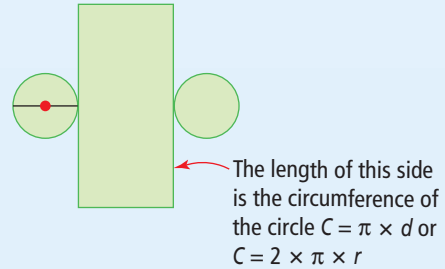
This metal totem pole was created by Todd Baker, Squamish Nation. It represents the Birth of the Bear Clan, with the princess of the clan on the top half and the bear on the bottom half.

Show You Know

Calculate the surface area of a cylindrical waste basket without a lid that measures 28 cm high and 18 cm in diameter. Give your answer to the nearest square centimetre.

Key Ideas

- The surface area of a cylinder is the sum of the areas of its faces.
- A net of a cylinder is made up of one rectangle and two circles.
- To find one of the dimensions of the rectangle, calculate the circumference of the circle.



Communicate the Ideas

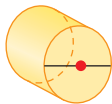
1. What are the similarities and differences between finding the surface area of a prism and finding the surface area of a cylinder?
2. Explain why you need to find the circumference of a circle to find the surface area of a cylinder.

Check Your Understanding

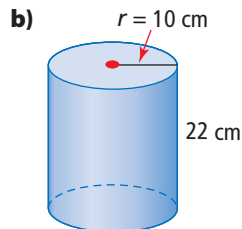
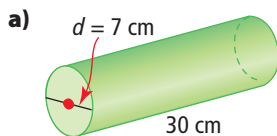
Practise

For help with #3 to #7, refer to Examples 1 and 2 on pages xxx–xxx.

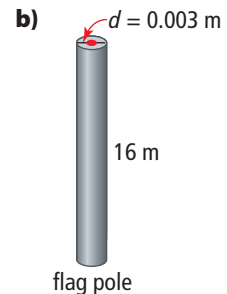
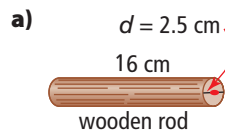
3. a) Draw a net for this cylinder.
b) Sketch a different net for this cylinder.



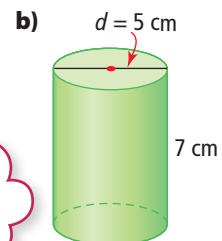
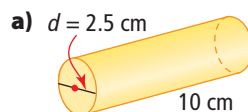
4. Estimate the surface area of each cylinder. Then, calculate each surface area to the nearest tenth of a square centimetre.



5. Find the surface area of each object to the nearest tenth of a square unit.



6. Use the formula $S.A. = 2 \times (\pi \times r^2) + (\pi \times d \times h)$ to calculate the surface area of each object. Give each answer to the nearest hundredth of a square unit.

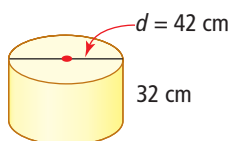


You can simplify the formula:
 $S.A. = 2 \times (\pi \times r^2) + (\pi \times d \times h)$
 $= 2\pi r^2 + \pi dh$

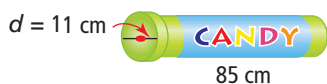
7. Do you prefer to find the surface area of a cylinder by using the sum of the area of each face or by using a formula? Give at least two reasons for your choice.

Apply

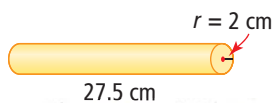
8. Anu wants to re-cover the cylindrical stool in his bedroom. How much material does he need if there is no overlap?



9. Kaitlyn and Hakim each bought a tube of candy. Both containers cost the same amount. Which container required more plastic to make?



10. Paper towel is rolled around a cardboard tube. Calculate the outside surface area of the tube.



Did You Know?

Each person produces about 1.59 kg of trash each day. Most of this is paper products.

Extend

11. If each tennis ball has a diameter of 7 cm, calculate the amount of material needed to make a can that holds three tennis balls.



12. Coins can be stored in a plastic wrapper similar to a cylinder. A roll of dimes contains 50 coins. Each dime has a diameter of 17.5 mm and a thickness of 1 mm. Calculate the minimum surface area of the plastic wrapper.
13. A paint roller in the shape of a cylinder with a radius of 4 cm and a length of 21 cm is rolled vertically on a wall.
- What is the length and width of the wet path after ten complete rolls?
 - What area does the paint cover?

MATH LINK

For the cylindrical building you created in the Math Link on page XXX, how much material do you need to cover the exterior walls and the roof of the building?

Did You Know?

Douglas J. Cardinal, one of the world's most acclaimed architects, uses his European, Blackfoot, and Ojibwa roots when designing buildings. He is known for his design of The Canadian Museum of Civilization in Gatineau, Québec, as well as a number of buildings in Western Canada, such as Telus World of Science in Edmonton and First Nations University of Canada in Regina.

Key Words

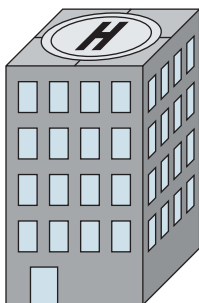
Unscramble the letters for each puzzle in #1 to #6.
Use the clues to help you solve the puzzles.

1. E T N
a flat diagram that you can fold to make a 3-D object
2. U S F A R E C E R A A
the sum of the areas of the faces of an object (2 words)
3. I R H T G R P M S I
a prism whose sides are perpendicular to its bases (2 words)
4. E C N I Y D R L
a 3-D object with two parallel circular bases
5. I R A G N R U A L T S I M R P
a 3-D object with two parallel triangular bases (2 words)
6. L E U C A A N R G T R I R M S P
a 3-D object with two parallel rectangular bases (2 words)

5.1 Views of Three-Dimensional Objects, pages xxx-xxx

7. Draw and label the top, front, and side views for these objects.

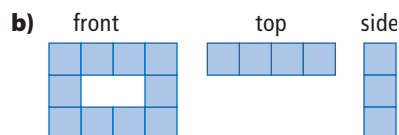
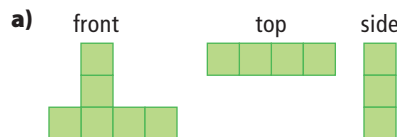
a)



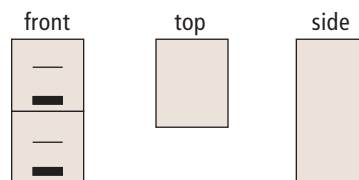
b)



8. Using isometric paper, draw each 3-D object from the views given.



9. A filing cabinet is in the far corner of an office. Shay is redecorating the room and wants to turn the cabinet 90° clockwise. Here are the views before the turn:

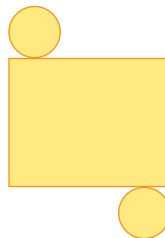


- a) How does each view change after the turn?
- b) Draw and label the top, front, and side views of the filing cabinet after it is turned.

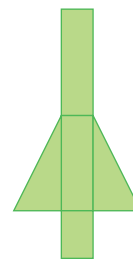
5.2 Nets of Three-Dimensional Objects, pages xxx-xxx

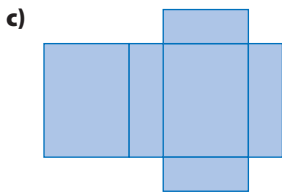
10. Name the object formed by each net.

a)

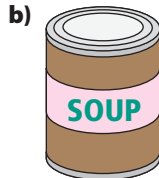
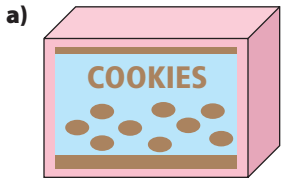


b)





11. Draw the net for each object.

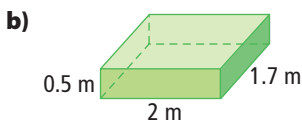
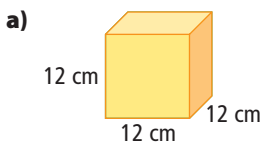


12. Using two pieces of grid paper, create a pencil box and lid. Draw a net, cut it out, fold it, and build your pencil box. Make sure new pencils fit in it!

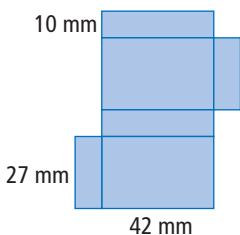
5.3 Surface Area of a Prism, pages xxx–xxx

For #13 to #16, calculate the surface area to the nearest tenth of a square unit.

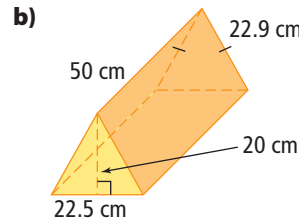
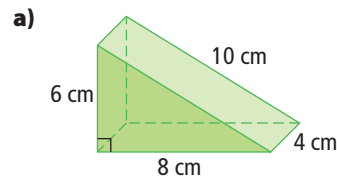
13. What is the surface area of each object?



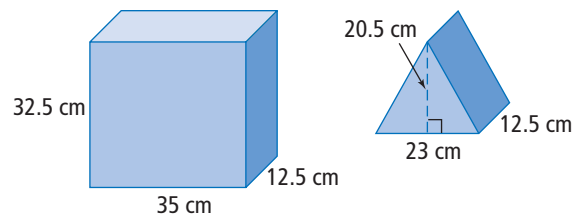
14. Using the measurements shown on the net of the rectangular prism, calculate the surface area.



15. Find the surface area of each triangular prism.



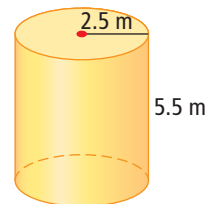
16. Liza had two more gifts left to wrap when she ran out of paper. Approximately how much more wrapping paper does she need to finish wrapping her gifts? Assume no overlap.



5.4 Surface Area of a Cylinder, pages xxx–xxx

For #17 to #19, calculate the surface area to the nearest tenth of a square unit.

17. Determine the surface area of the cylinder.



18. The pencil sharpener on Kay's desk has a diameter of 3.4 cm and is 7 cm tall. Calculate the surface area.

19. The circumference of a container's lid is 157 cm. If the container is 102 cm tall, what is the surface area of the container?

For #1 to #5, choose the best answer.

1. The top view of this container shows a

- A circle
B square
C triangle
D rectangle

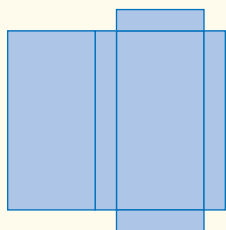


2. One face on a cube has an area of 49 cm^2 . What is the surface area of the cube?

- A 343 cm^2
B 294 cm^2
C 196 cm^2
D 154 cm^2

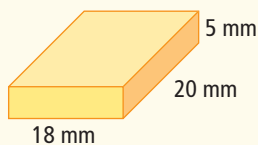
3. What three-dimensional object has a net like this one?

- A cube
B cylinder
C triangular prism
D rectangular prism



4. What is the surface area of this box?

- A 550 mm^2
B 900 mm^2
C 1100 mm^2
D 1800 mm^2

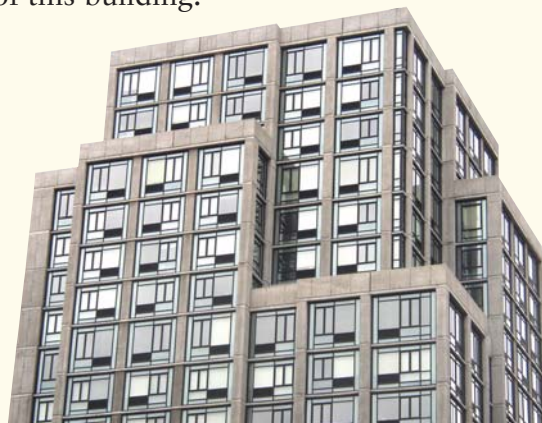


5. What is the surface area of a cylinder that is 30.5 cm long and has a radius of 3 cm, to the nearest hundredth of a square centimetre?

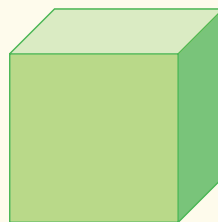
- A 274.50 cm^2 B 603.19 cm^2
C 631.14 cm^2 D 688.01 cm^2

Short Answer

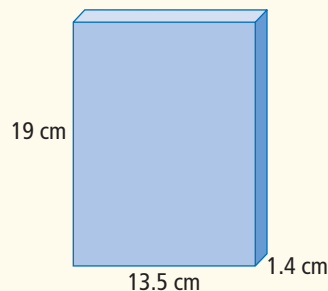
6. Sketch the top, front, and side views of this building.



7. An object may have more than one net. Draw three different nets for this cube.



8. A DVD case is made of a plastic covering that measures 19 cm long, 13.5 cm wide, and 1.4 cm thick. Calculate the surface area to the nearest tenth of a square centimetre.



9. The surface area of a cube is 1014 cm^2 . Find the length of any side of the cube.

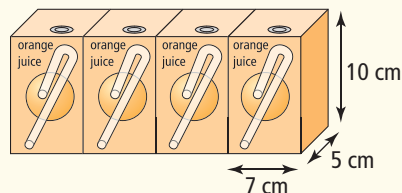
Extended Response

10. a) Sketch a three-dimensional object you can build using two of these triangular prisms.

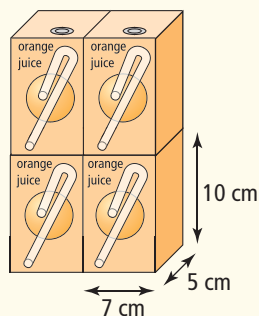


- b) Draw the front view, top view, and side view of your object.
- c) Draw a net for your object.
11. Ken and Arika are comparing their cylinders. Arika's cylinder is twice as tall as Ken's, but is only half the diameter. Ken's cylinder has a height of 18 cm and a diameter of 9 cm. Whose cylinder has the greater surface area?

12. Single-serving juice boxes measure 10 cm by 7 cm by 5 cm. A manufacturer wants to shrink wrap four boxes together for sale. Which of the following arrangements of the boxes will use the least amount of plastic wrap? Show how you know.



Arrangement 1



Arrangement 2

WRAP IT UP!

It is time to create your miniature community!

Work together to finalize one aerial view for your community. You may choose to start with one that you created on page XXX.

Include the following in your diagram and description:

- All the buildings designed by you and your group members.
- A 3-D sketch, net, and surface area calculations for one new building for each member of your group. The new designs should include at least one prism and cylinder. Check each other's work before submitting.
- Streets to navigate through the city.
- Environmental considerations such as water source, parks, etc.



Math Games

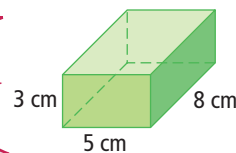
Let's Face It!

1. Play *Let's Face It!* with a partner or in a small group. These are the rules:
 - Remove the jacks, queens, kings, aces, and jokers from the deck of cards.
 - Take turns dealing the cards. It does not matter who deals first.
 - Shuffle the cards and deal three cards, face up, to each player.
 - Use the values of the cards as the dimensions, in centimetres, of a rectangular prism.
 - Calculate the surface area of your rectangular prism using pencil and paper.
 - Each player who calculates the surface area of their prism correctly scores a point. (You will need to check each other's work.)
 - The player with the rectangular prism that has the greatest surface area scores an extra point for that round. If there is a tie, each of the tied players scores an extra point.
 - The first player to reach ten points wins the game. If more than one player earns ten points in the same game, these players continue playing until one of them pulls ahead.
2. Play a different version of *Let's Face It!* by modifying the rules as follows:
 - Deal only two cards to each player and use them to describe the size of a right cylinder. The first card gives the radius of each circle, in centimetres. The second card gives the height of the cylinder, in centimetres.
 - Use a calculator to determine the surface area of your cylinder, to the nearest hundredth of a square centimetre.
 - Award points and decide the winner in the same way as before.

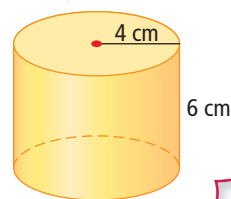
Materials

- deck of playing cards per pair or small group
- calculator per student

My cards are a 5 of clubs, a 3 of hearts, and an 8 of spades. My rectangular prism has edges of 5 cm, 3 cm, and 8 cm.



I was dealt a 4 of clubs and then a 6 of clubs. The radius of each circle is 4 cm. The height of the cylinder is 6 cm.



Challenge in Real Life

Design a Bedroom

Have you ever wondered what it would be like to completely design a room? Suppose you were given the opportunity to create the kind of space that a person your age would appreciate and make good use of.

You be the interior designer. Your first project is to create a design for a bedroom that is 4 m wide by 5 m long, and is 2.5 m high.

- Draw the top view of the room and place at least three objects in the room.
 - Draw the top, front, and side views of at least three objects you put in the room. Identify the 3-D shape that each object closely resembles.
- Painting your room is the next step. Determine the amount of paint you need to cover the walls and ceiling of your room.
 - One can of the paint you are going to use covers $10 \text{ m}^2/\text{L}$. How many cans do you need?

