# CHAPTER



# **Circle Geometry**

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# **Get Ready**

## **Working With Circles**

•  $\pi \approx 3.14$  • diameter: the distance across the circle, passing through the centre; d = 2r• radius: half the distance across the circle, starting at the centre;  $r = \frac{d}{2}$ • circumference: the distance around the circle;  $C = \pi \times d$  or  $C = 2 \times \pi \times r$ The radius of a circle is 3 cm.  $C = 2 \times \pi \times r$   $C \approx 2 \times 3.14 \times 3$   $C \approx 18.84$ The circumference is about 18.84 cm.



## Working With Angles





Date:

2. Estimate the size of each angle. Then, measure it with a protractor.
a) \_\_\_\_\_\_
b) \_\_\_\_\_\_
b) \_\_\_\_\_\_
c. \_\_\_\_\_
c. \_\_\_\_\_
d. \_\_\_\_\_
<lid. \_\_\_\_\_</li>
d. \_\_\_\_\_
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- right triangle to draw a line from that point
- 4. Draw the perpendicular bisector for each line segment.

a) A B



# Math Link

#### Geometry in Design

The circle is an important shape for Aboriginal people. For example, the medicine wheel was often made by putting large rocks in a circle. Architects, graphic designers, and artists also use circles in their work. Answer the questions to explore circles.

5 cm On tracing paper, use a compass to draw a circle that has a diameter of at least 5 cm. 1. 2. a) Fold the circle in half. Open the paper and draw a line segment along the fold. Make sure each end of the line is on the edge of the circle. b) What is this line called? 3. a) Fold the circle in half again, making a different fold. Open the paper and draw a line segment along the new fold. **b)** Where the 2 lines intersect is called the \_\_\_\_\_ a) Estimate the measure of each of the 4 angles around the centre of the circle: 4. <u>/2:</u> ° <u>\_\_\_\_</u>° ∠3:\_\_\_\_° <u>\_4</u>:\_\_\_\_\_ 0 **b)** Measure each angle with a protractor: ∠1: \_\_\_\_\_° ∠2: \_\_\_\_\_° ∠3:\_\_\_\_\_° ∠4:\_\_\_\_° c) How close was your estimate? d) What is the total measure of these 4 angles? 5. An environmental club wants to use this logo. What kind of triangle is this? Give 1 reason for your answer. Brainstorm some businesses that use circles in their advertisements. 6.

M<sup>®</sup>E 3.

# 10.1 Warm Up

- **1.** Point C is the centre of the circle.
  - a) List the line segments that are radii.
  - **b)** List the line segments that are diameters.
- 2. Calculate the length of *c* in each right triangle. Use the Pythagorean relationship.







# Link the Ideas

Use this information to help you solve circle problems.

#### **Inscribed Angles**

- If 2 inscribed angles share the same arc, they are congruent.
- example:  $\angle RAS = \angle RBS$  because the share the same arc, RS.

Congruent means equal.



#### **Central and Inscribed Angles**

- The measure of the central angle is twice the measure of the inscribed angle that shares the same endpoints on the same arc.
- example: central  $\angle ACB = 2 \times inscribed \angle ADB$  $80^\circ = 2 \times 40^\circ$





#### Name: \_\_\_\_\_

Date: \_\_\_\_\_









### Working Example 3: Use Central and Inscribed Angles to Solve Problems

Jamie photographed his house using a lens with a  $70^{\circ}$  field of view. He wants to take another photo, but he only has a lens with a  $35^{\circ}$  field of view. Where could he stand to take a photo of the whole house?





#### Solution

The diagram shows an inscribed angle where Jamie could stand.



Draw another place where Jamie could stand.

- Draw a chord from the side of the house to a point on the circle. Label the point A.
- Draw another chord from the opposite side of the house to point A. This is an inscribed angle.

#### Show You Know



## . . . . . . . .

# **Check Your Understanding**

# **Communicate the Ideas**

- 1. In the diagram,  $\angle$ BDA measures half of  $\angle$ BCA. Explain why this is true.
- 2. Manny drew the diameter of a circle. Then, he drew an inscribed angle that had the same endpoints as the diameter. What is the measure of the inscribed angle? How do you know?



Date: \_\_\_\_\_

# Practise

**3.** What is the measure of  $\angle ADB$ ?

 $\angle ADB = \angle \_\_$  ÷ \_\_\_\_\_

= \_\_\_\_\_ ÷ \_\_\_\_\_ 82° = \_\_\_\_\_°

**4.** a) What is the measure of  $\angle$ FJG? Give 1 reason for your answer.

∠FJG is an \_\_\_\_\_ angle.

 $\angle$ FJG =  $\angle$ FHG because they share the same \_\_\_\_\_

 $\angle$ FHG is \_\_\_\_\_°. So,  $\angle$ FJG is \_\_\_\_\_°.

**b)** What is the measure of  $\angle$ FCG? Justify your answer.

 $\angle$ FCG is a \_\_\_\_\_\_ angle.  $\angle$ FCG = \_\_\_\_\_ ×  $\angle$  \_\_\_\_\_ Central angle = 2 × inscribed angle = \_\_\_\_\_ × \_\_\_\_\_° = \_\_\_\_\_° So,  $\angle$ FCG is \_\_\_\_\_°.

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6. All the lights are out, so Jacob and his mother are using flashlights to find the electrical panel. Jacob's flashlight shines light through an angle of 15°. His mother's flashlight shines light through an angle of 30°. On the diagram, show where Jacob should stand so both flashlights shine on the electrical panel.



## Apply

- 7. Point C is the centre of the circle.  $\angle ABD = 38^{\circ}$ 
  - a) What is the measure of  $\angle ACD$ ? Justify your answer.



15°

 $(\bullet)$ 

Κ

Μ

24°

- **b)** What type of triangle is  $\triangle$ ACD? Circle ISOSCELES or EQUILATERAL. Give 1 reason for your answer.
- 8. Point C is the centre.  $\angle KJM = 15^{\circ}$  $\angle JML = 24^{\circ}$

What is the measure of each of the following angles?



| Na  | me:  | Date:                              |
|-----|--|------------------------------------|
| 9.  | In the diagram, $\angle BAD = 34^{\circ}$ and $\angle ADE = 56^{\circ}$ .<br>a) What is the measure of $\angle ABE$ ?<br>Use arc AE. | A 34° G 56° D E                    |
|     | Sentence:  |                                    |
| 10. | Sentence:  | B. D<br>C<br>C<br>C<br>C<br>C<br>B |

# **Math Link** a) Design a piece of art using this circle. Use only inscribed angles and central angles. Include: • at least 3 inscribed angles • at least 2 central angles **b)** Colour 1 central angle blue and 1 inscribed angle red. How are they related?



If AC = 10 cm, then  $AB = \_$  cm.



If AB = 9 cm, then AE =\_\_\_\_ cm.





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# Working Example 2: Use Chord Properties to Solve Problems

Louise wants to drill a hole for an umbrella in a circular table. How can she find the centre?

#### Solution

Step 1: Draw 2 chords on the circle.

Step 2: Find the midpoint (middle) of each chord. Use a ruler or fold the paper.



- *Step 3:* **□** Use a right triangle ruler to draw the perpendicular bisector of each chord.
- Step 4: 
  Put a dot where the 2 perpendicular bisectors cross. This is the centre of the circle.

#### Show You Know

Mark wants to plant a tree in the centre of this flowerbed. Explain how he can find the centre using circle properties. Draw an example on the circle.

# **Check Your Understanding**

#### **Communicate the Ideas**

- 1. The diameter of the circle bisects line AB.
  - **a)** What do you know about  $\angle ADC$ ?
  - **b)** What do you know about AD and DB?

cm

cm

D

2. Explain how to find the centre of the circle using these 2 chords.



# Practise

 CD bisects chord AB. The radius of the circle is 15 cm. Chord AB measures 24 cm. What is the length of CE?

Label the diagram with the measurements you know.



The length of CE is \_\_\_\_\_ cm.

В

| Name: Date: |  |                     |
|-------------|--|---------------------|
| 4.          | The radius CF bisects chord HJ.<br>CG measures 4 mm.<br>Chord HJ measures 14 mm.<br>What is the radius of the circle to the nearest tenth of<br>a millimetre (1 decimal place)?<br>Draw a line from C to J.<br>Write the measurements on the diagram.<br>Formula $\rightarrow$<br>Substitute $\rightarrow$ | H<br>cm G<br>C • cm |

Solve  $\rightarrow$ 

The radius of the circle is \_\_\_\_\_ mm.

5. Hannah wants to draw a circle at the centre of her trampoline. Explain how she can find the centre of her trampoline. Use the diagram to help you.



| ът |       |
|----|-------|
| N  | ame.  |
| ΤN | anne. |

# Apply

The radius of the circle is 17 m. 6. The radius CD is perpendicular to the chord AB. CE measures 8 m. 8 m \_C What is the length of chord AB? D E Are AE and BE equal? Circle YES or NO. . 17 m First, find the length of BE. B Formula  $\rightarrow$ Substitute  $\rightarrow$ Solve  $\rightarrow$  $AB = 2 \times BE$ = 2 × \_\_\_\_\_ = Sentence: D 7. Find the length of x. Round your answer to the nearest tenth (1 decimal place). Use  $\triangle CAE$ . В 3 CA = \_\_\_\_\_ cm CB = CA. Both are radii. CE = \_\_\_\_\_ - \_ = Use the Pythagorean relationship to calculate the length of EA. Formula  $\rightarrow$ Substitute  $\rightarrow$ Solve  $\rightarrow$ 

8. If you know that the radius CD is 5 cm and BC is 3 cm, what is the area of  $\triangle ABD$ ?



CA is also the radius, so the length is \_\_\_\_\_ cm. Label CA on the diagram.

BC = \_\_\_\_\_ cm

 $\Delta ABC$  is a \_\_\_\_\_\_ triangle. Find the length of AB.

 $Formula \rightarrow$ 

Substitute  $\rightarrow$ 

Solve  $\rightarrow$ 

| Area of ∆ABD:                                 |             |
|---|-------------|
|   | h = DC + BC |
| $Formula \rightarrow A = b \times h \div 2 -$ | =_+_        |
| Substitute $\rightarrow$                      | =           |
|   |             |

Solve  $\rightarrow$ 

# **Math Link** A mandala is a piece of art framed inside a circle. The North American Plains Indians and Tibetan Buddhists create mandalas. Create a mandala using the example as a guide a) by following the pattern. You want to display your mandala. How much room will you need? b) □ Find the centre using 2 chords and the perpendicular bisector of each. Mark it with a black dot. □ What is the radius? \_\_\_\_\_ cm □ What is the diameter? \_\_\_\_\_ cm □ Calculate the circumference. $C = \pi \times d$ = \_\_\_\_\_ × \_\_\_\_\_

=\_\_\_\_\_

You will need about \_\_\_\_\_ cm to display your mandala.

# 10.3 Warm Up

1. Name the triangles using the words from the box.



isosceles triangle (2 equal sides) equilateral triangle (3 equal sides)

> The 2 bottom angles in an isosceles triangle

> > are equal.

 $^{\circ} + ^{\circ} = 180^{\circ}$ 



b)

b)

 $x + _{----}$ 

right triangle

2. List the chords in the circle.



- 3. Find the measure of the unknown angle in each triangle.
  - a) x 52°





*x* = \_\_\_\_\_°





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# **10.3 Tangents to a Circle**

#### tangent (to a circle)

• a line that touches a circle at exactly 1 point

#### FOLDABLES Study Tool

#### point of tangency

• the point where the tangent line touches the circle

# Link the Ideas

#### Tangent to a Circle

• A tangent to a circle is perpendicular (at a 90° angle) to the radius at the point of tangency (where it touches the circle).

#### **Tangent Chord Relationship**

• If you draw a chord from the point of tangency through the centre of the circle, this chord is the diameter.





#### Working Example 1: Determine Angle Measures in a Circle With a Tangent Line

F

50

AB is tangent to the circle at point D. BE contains the diameter FE.  $\angle ABE = 50^{\circ}$ 

Remember, CF, CD, and CE are all radii.

(a) What is the measure of  $\angle BDC$ ? Justify your answer.

#### Solution

Radius CD is tangent to the circle at point \_\_\_\_\_. So, CD is perpendicular to line segment AB.

 $\angle$ BDC is \_\_\_\_\_°.

| <ul> <li>b) What is the measure of the central angle ∠DCE? Justify your answer.</li> <li>Solution</li> <li>The sum of the angles in a triangle is°.</li> </ul> | A D 50°<br>F B |
|--|----------------|
| In $\triangle BCD$ , $\angle CBD + \angle BDC + \angle DCB = \°$   | E              |
| $\_\_\_\circ + \_\_\_\circ + \angle DCB = \_\_\_\circ$   |                |
| $\_\\circ + \angle DCB = \_\\circ$   |                |
| $\angle DCB = \underline{\qquad \circ} - \underline{\qquad \circ}$   |                |
| $\angle DCB = \_\°$  |                |
| $\angle$ ECB is a straight angle that measures°.   |                |
| $\angle$ DCB and $\angle$ DCE make a straight angle.   |                |
| $\angle DCE + \angle DCB = 180^{\circ}$  |                |
| $\angle DCE + \° = 180^\circ$  |                |
| $\angle DCE = 180^\circ - 40^\circ$  |                |
| $\angle DCE = \\circ$  |                |
|  |                |
| $\succ$ c) What type of triangle is $\triangle$ CDE? Justify your answer.  |                |
| Solution   |                |
| CD and CE are both radii of the circle, so they are equal.   |                |
| A triangle with 2 equal sides is a(n) triangle.  |                |
| (equilateral, isosceles, or scalene)   |                |



|            | Show You Know  |
|------------|--|
| Lin<br>Lin | e segment AF is tangent to the circle at point E.<br>e segment DF contains the diameter DB.<br>$FE = 34^{\circ}$ |
| a)         | What is the measure of $\angle CEF$ ? Show how you know.   |
|            | AF is tangent to the circle at point   |
|            | Radius CE is to the line segment AF. $F$   |
|            | So, $\angle CEF = \underline{\qquad}^{\circ}$ .  |
| b)         | What is the measure of $\angle$ ECF? Show how you know.<br>Use $\triangle$ CEF.                                  |
|            | $\angle CEF + \angle \_\_\_ + \angle \_\_\_ = 180^{\circ}$   |
|            | ° +° + ∠ =°  |
|            | <u> </u>   |
| c)         | What is the measure of $\angle$ EDF? Show how you know.  |
|            | $\angle$ EDF is equal to $\angle$ EDB.   |
|            | $\angle$ is an inscribed angle and $\angle$ ECB is the central angle.  |
|            | $\angle EDC = \angle ECB \div 2$   |
|            | $\angle EDC = \underline{\qquad}^{\circ} \div 2$   |
|            | $\angle EDC = \°$  |
|            | Therefore, ∠EDF is°.   |



-b) What is the length of chord BE? Justify your answer.





 $\Delta$ BCE is an equilateral triangle. So, BE is the length of a radius.

diameter BD = \_\_\_\_ mm

BC is the radius of the circle, which is half the diameter.

 $BC = BD \div 2$ 

 $BC = \_$   $\div 2$ 

BC = \_\_\_\_\_

BC = BE = CE

Therefore, BE = \_\_\_\_\_ mm.

-c) What is the measure of the inscribed angle  $\angle BED$ ?

#### Solution



D

 $\angle BCD = \_$ °. It is the diameter and the central angle.

 $\angle$ BED is an inscribed angle, so it is \_\_\_\_\_\_ the size of the central angle.

 $\angle BED = \angle BCD \div 2$ 

 $\angle BED = \____\circ \div 2$ 

 $\angle BED = \___^\circ$ 

Therefore,  $\angle BED$  is \_\_\_\_\_°.

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| Name: |  |
|-------|--|
|-------|--|

d) What is the length of chord DE? Round your answer to the nearest millimetre. Justify your answer.

#### Solution



Find the length of DE using the \_\_\_\_\_\_ relationship in  $\Delta$ BDE.



The length of DE is \_\_\_\_\_ mm, to the nearest mm.

| PQ i<br>QR<br>PQ =<br>ΔQC | is tangent to the circle at point Q.<br>is a diameter of the circle.<br>= 9 mm; $PR = 41$ mm<br>CS is an equilateral triangle.      | C 41 mm  |
|---------------------------|---|--|
| a) V<br>J                 | What is the length of diameter QR?b)Justify your answer.  | What is the length of chord QS?<br>How do you know?                                  |
| ]                         | PQ is to QR,  | Diameter QR = mm   |
| S                         | so $\angle PQR$ is°<br>$\Delta RQP$ is a right triangle.  | Radius QC = $\_$<br>$\Delta$ QCS is an equilateral triangle, so all sides are equal. |
|                           | QK + QP = KP  | Therefore, if QC is mm,  |
|                           |   | then QS is mm.   |
|                           |   |  |
|                           |   |  |
| r.                        | The length of diameter QR is mm.  |  |
| c) '                      | What is the length of RS? Show how you know.  |  |
| 2                         | $\angle$ RCQ is the central angle.<br>$\angle$ RSQ is an inscribed angle, so $\angle$ RSQ =<br>$\triangle$ RSQ is a right triangle. | °.   |
|                           | $RS^2 + $   |  |
|                           |   |  |
|                           |   |  |
|                           |   |  |

#### Date:

## \_Working Example 3: Solve Problems With Tangents to Circles

A speed skater is practising on a circular track with a radius of 40 m. He falls and slides 22 m off the track in a line tangent to the circle. How far is he from the centre of the rink?

#### Solution

In the diagram, the skater fell at point A and slid to point B.

Since AB is \_\_\_\_\_\_ to the circle, it is perpendicular to the radius AC.

Use the Pythagorean relationship to find the length of BC. BC shows how far the skater is from the centre of the rink.



22 m A 40 m C



-The speed skater is approximately \_\_\_\_\_ m from the centre of the rink.

#### Show You Know

Callan is flying his model airplane. The wire breaks just before he lands it. The control wire is 10 m long. The plane lands 74 m from Callan. Label the diagram. How far did the plane travel after the wire broke? Label the diagram. Round your answer the nearest tenth of a metre (1 decimal place). The plane travelled \_\_\_\_\_\_ m after the wire broke.

# **Check Your Understanding**

#### **Communicate the Ideas**

 Elliot says that AB is tangent to the circle because it touches the circle at 1 point. Is he correct? Circle YES or NO. Give 1 reason for your answer.



2. If BC is the radius, is AB tangent to the circle? Circle YES or NO. Give 1 reason for your answer.



- 3. Line segment JK is tangent to the circle at point H. GH is the diameter and  $\angle CGL = 10^{\circ}$ .
  - a)  $\triangle CGL$  is an \_\_\_\_\_\_\_ triangle. (equilateral *or* isosceles)

Give 1 reason for your answer.



**b)** What is the measure of  $\angle$ HCL?

 $\angle$ HCL and  $\angle$ HGL have the same arc, \_\_\_\_\_.

∠HCL is the \_\_\_\_\_ angle.

∠HGL is the \_\_\_\_\_ angle.

 $\angle$ HCL =  $\angle$ HGL × \_\_\_\_\_

=\_\_\_\_\_

# Practise

- 4. AB is tangent to the circle at point D. BE contains the diameter EF.  $\angle ABE = 60^{\circ}$ 
  - a) What is the measure of  $\angle BDC$ ? Justify your answer.

Radius DC is \_\_\_\_\_\_ to tangent AB.

So,  $\angle$ BDC is \_\_\_\_\_°.

**b)** What is the measure of  $\angle DCE$ ? Justify your answer.

The sum of the angles in a triangle is \_\_\_\_\_°.

 $\angle BDC + \angle DBC + \angle DCB = \____°$ 

 $\_\_\circ + \_\_\circ + \angle DCB = \_\_\circ$ 

 $\angle DCB = \___^\circ$ 





А

 $\angle$ DCB and  $\angle$ DCE make a straight angle.

 $\angle DCB + \angle DCE = 180^{\circ}$ 

° + \_\_\_\_° = 180°

 $\angle DCE =$ 

- c) What type of triangle is  $\Delta CDE?$  \_
- **d)** What is the measure of  $\angle$ DEC? How do you know?
  - Use the arc DF.  $\angle$  DEF is an \_\_\_\_\_ angle.
  - $\angle DCF$  is the \_\_\_\_\_ angle.
  - If  $\angle$ DCF measures \_\_\_\_\_°, then  $\angle$ DEF is half of that.

![](_page_36_Figure_23.jpeg)

- 5. AB is tangent to the circle at point B. BD is a diameter of the circle. AB = 6 mAD = 10 m $\Delta BCE$  is an equilateral triangle.
  - a) What is the length of diameter BD? Justify your answer.

![](_page_37_Figure_4.jpeg)

∠ABD is \_\_\_\_\_° because AB

is \_\_\_\_\_ to BD.

Formula  $\rightarrow$ 

Substitute  $\rightarrow$ 

Solve  $\rightarrow$ 

c) What is the measure of the inscribed angle∠BED?

![](_page_37_Picture_11.jpeg)

∠BCD is \_\_\_\_\_°. ∠BED is an inscribed angle.

![](_page_37_Figure_13.jpeg)

 $\angle BED = \_$  ÷ \_\_\_\_\_

∠BED = \_\_\_\_\_

So,  $\angle BED$  is \_\_\_\_\_°.

![](_page_37_Figure_17.jpeg)

**b)** What is the length of chord BE? Justify your answer.

![](_page_37_Figure_19.jpeg)

 $\Delta BCE$  is an equilateral triangle.

![](_page_37_Figure_21.jpeg)

 $BC = BD \div$ 

radius BC = \_\_\_\_\_ ÷ \_\_\_\_\_

BC = BE = CE

So, BE = \_\_\_\_\_ m.

**d)** What is the length of chord DE to the nearest metre? Justify your answer.

![](_page_37_Figure_27.jpeg)

Use  $\triangle DEB$ .

Formula  $\rightarrow$ 

Substitute  $\rightarrow$ 

Solve  $\rightarrow$ 

The length of DE is \_\_\_\_\_ m.

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- 6. A dog is on a leash tied to a pole in the backyard. The leash is 5 m long. The back of the house is tangent to the circle at the edge of the house.
  - a) What is the distance from the pole to the cat door?

Formula  $\rightarrow$ 

Substitute  $\rightarrow$ 

Solve  $\rightarrow$ 

![](_page_38_Picture_7.jpeg)

The distance from the pole to the cat door is \_\_\_\_\_ m.

b) How close can the dog get to the cat door?Find the distance from the edge of the circle to the cat door.

The radius is from the centre of the circle to any point on the edge of the circle.

| • • |       |
|-----|-------|
| N   | ame.  |
| ΤN  | anne. |

# Apply

Find the length of x in the diagram. Line *l* is tangent to the circle. Write your answer to the nearest tenth (1 decimal place).

x is the same length as side \_\_\_\_\_ of  $\Delta$ FEG.

ΔFEG is a \_\_\_\_\_\_ triangle.

![](_page_39_Figure_6.jpeg)

| Va | me:  |                          | Date:                 |
|----|--|--------------------------|-----------------------|
| 3. | Find the measure of $\angle$ QRT.<br>SP is tangent to the circle at point S.<br>RS is perpendicular to SP.<br>$\angle$ SPQ = 74° |                          | Q<br>Q<br>R<br>S<br>S |
|    | ΔPSQ is a  | triangle, so ∠PSQ is°.   |                       |
|    | The 3 angles in a triangle add up to $_{-}$  | °.                       |                       |
|    | $\angle PQS + \_\_\_ + \_\_\_ = \_\_$  | o                        |                       |
|    |  |                          |                       |
|    | $\angle POS$ is an inscribed angle to the ce   | ntral angle ∠TRS.        |                       |
|    | So, $\angle TRS = \angle POS \times$   |                          |                       |
|    | $\angle TRS = \°$  |                          |                       |
|    | $\angle QRS = $  | QRS is a straight angle. |                       |
|    | $\angle QRT + \angle TRS = \°$   |                          |                       |
|    | $\langle ORT + = ^{\circ}$   |                          |                       |
|    | ZQIU +   |                          |                       |
|    | $\angle QRT - \_\_ ° - \_$   | o                        |                       |
|    | $\angle QRT - \underline{\qquad} = \underline{\qquad}^{\circ} - \underline{\qquad}$ $\angle QRT = \underline{\qquad}^{\circ}$    | o                        |                       |

9. The circles are exactly the same size. Line *l* is tangent to both circles. The radius is 5 cm. What is the perimeter of the rectangle? Label the diagram to show your explanation.

![](_page_41_Picture_3.jpeg)

|     |  |        |   | A.        |                |  |
|-----|--|--------|---|-----------|----------------|--|
| Fiı | Find the measures of the following from your design. |        |   |           |                |  |
| Ch  | ords:  | Radii: | D | iameters: | Tangent Lines: |  |

# **Chapter Review**

#### Key Words

For #1 to #6, unscramble the letters. Use the clues to help you.

- 1. ICBNEIRSD EALNG \_\_\_\_\_\_\_ an angle formed by 2 chords that have a common endpoint (2 words)

- 4. CRHDO \_\_\_\_\_\_\_\_\_ a line segment that has both endpoints on the circle

#### 10.1 Exploring Angles in a Circle, pages xx-xx

- 7. Find the measure of each angle.
  - **a**) ∠ABD = \_\_\_\_\_°
  - b) ∠ACD

 $\angle ACD = 2 \times \_$ 

8. What are the measures of the unknown angles *x* and *y*?

a) 
$$\angle x = \underline{\qquad} \div 2$$

=

**b**) ∠y

![](_page_42_Figure_19.jpeg)

2/19

![](_page_43_Figure_0.jpeg)

 $AE = AB \times 2$ 

=\_\_\_\_×2

=\_\_\_\_\_

AE is \_\_\_\_\_ m.

radius CG = \_\_\_\_\_

 $EG^2 + EC^2 = CG^2$ 

C

12. Chord FG measures 18 cm. The diameter measures 22 cm. What is the length of EC?
ΔCEG is a right triangle.
EG = \_\_\_\_\_\_

r = d ÷ 2

- 10.3 Tangents to a Circle, pages xx-xx
- **13.** What is the measure of  $\angle$ FCG if DE is tangent to the circle?

If DE is tangent to the circle, then  $\angle$ EGC is \_\_\_\_\_°. In  $\triangle$ ECG,  $\angle$ GEC +  $\angle$ EGC +  $\angle$ ECG = 180°

 $43^{\circ} + \underline{\qquad}^{\circ} + \angle EGC = 180^{\circ}$ 

![](_page_44_Picture_7.jpeg)

 $\angle ECG + \angle FCG = 180^\circ$ , because  $\angle ECG$  is a \_\_\_\_\_

 $\_\__{o} + \angle FCG = 180^{\circ}$ 

The measure of  $\angle$ FCG is \_\_\_\_\_°.

**14.** If AB is tangent to the circle at B, what is the length of the radius?

Find the length of DB using the Pythagorean relationship.

$$AB^2 + DB^2 = AD^2$$

![](_page_45_Figure_5.jpeg)

diameter DB = \_\_\_\_ mm

radius DC = \_\_\_\_\_ mm

**15.** Jasmine was flying a remote-control airplane when it lost signal at a point tangent to the circle. It flew along this tangent until it crashed. How far did the plane travel before it crashed? Round your answer to 1 decimal.

![](_page_45_Figure_9.jpeg)

Date:

# **Practice Test**

#### For #1 and #2, choose the best answer.

- **1.** Which statement is true?
  - A A central angle is smaller than an inscribed angle with the same end points.
  - C An inscribed angle that has the same endpoints as the diameter is always 90°.
- 2. What is the measure of the inscribed angle?
  - A 25°

**C** 100°

#### *Complete the statement in #3.*

**3.** If AB is tangent to the circle, the measure of  $\angle$ BCD is \_\_\_\_\_

#### **Short Answer**

4. What is the length of radius *x*? Round your answer to the nearest tenth of a centimetre (1 decimal place).

![](_page_46_Picture_14.jpeg)

Use the \_\_\_\_\_\_ relationship to find the distance.

![](_page_46_Figure_16.jpeg)

**B** Two inscribed angles are never equal in size.

**B** 50°

**D** 200°

0

**D** If a bisector of a chord passes through the centre, the bisector is not perpendicular to the chord.

![](_page_46_Figure_19.jpeg)

![](_page_47_Figure_0.jpeg)

- a) What is the measure of  $\angle ADB$ ? How do you know?
- **b)** What is the measure of  $\angle ACB$ ? How do you know?

7. This diagram shows the water level inside a pipe. The diameter of the pipe is 34 mm. What is the distance from the centre of the pipe to the water level *x*?

![](_page_48_Figure_3.jpeg)

Use your designs from 1 of the Math Links on pages xx, xx, or xx. Add any missing properties.

Inscribed angle

#### **Key Word Builder** Match the key words with the correct definition. Then, circle them in the word search. a part of the circumference of a circle \_\_\_\_\_ 1. 2. an angle created by 2 radii of a circle (2 words) a line segment that has both endpoints on a circle \_\_\_\_\_ 3. the distance around a circle \_\_\_\_\_ 4. the distance across a circle, through the centre \_\_\_\_\_ 5. an angle created by 2 chords that have a common endpoint (2 words) 6. the point in the middle of a line \_\_\_\_ 7. a line that divides a line segment in half and is at a 90° to it (2 words) 8. formula used to find the unknown length of a right triangle \_\_\_\_\_ 9. **10.** half the distance across the circle starting at the centre **11.** means more than 1 radius \_\_\_\_ **12.** a line that touches a circle at exactly 1 point \_\_\_\_\_ radius central angle chord circumference arc diameter inscribed angle radii midpoint perpendicular bisector Pythagorean relationship tangent S Α S Т Α Т Ι Μ Μ Ν E А Р I G А Ν R L Е G Р Η U Е Ν R А L Η Ι Н Е I S U Е Е I I Е Ι А Ι D Ι Ι Т С R Е E P R Ù Ι R С Ι С U R L Ι D R R В Μ Е С Е С С R Т G А Ι Ν Е А Р А Е R А Т R С U Е Е U Е Е Η Т D U Е R С Т С Е А Ν R Μ А Ι А Ι А Р Y Т Η А G Ο R E А Ν R Е L Α Т Ι 0 Ν S Η Ι Р S С S F С С G R Е G R А Е I А Ν А R D R А А Μ Р Р Е Р С F Е Е 0 D R С Η С Ι R U Е R Ν С Μ Ν R R S Р R Ι Η С Ν Р С Ι Е G Ν С Ι Е Ν R R 0 R С С S Ι L L R Е 0 U R 0 U В Ν Ι Р R Ν Т Ν 0 G Е В S 0 0 Е S D D R L Е А Ι Е Ι А В Ο Р S G Ν S С R Ι В Е R С R Р D Ι Ι Ν Ε D А Ν G L Η U Ν Ι Р С С Е Ν С Е Ν Т R L Ν G L Е D С R Η Е А А S Е F Р Μ R I R Η D В R R Р S А R R S Ι Е S Ο Е Е Е Т R D А A R Ν А Ι Ε D Ι А Μ Е R Ν D Е T I A Р А I Ι Т L С S D М Е Η S С С R U R Т Ι R R D Р U R Р Т Е Е Т Р Т D G 0 Р F Е Ν А А I А А R D U S R Т Ν 0 Η С U Е S Т С 0 0 R L Ν R S Р Т Μ Ι D 0 Ι Ν Т S Е Ν С А Е Ι С С Е Е Т L Μ Y Т Т Ν С R С U 0 D R R R Е Ι Ι D Р Ν Ν Ι Ν А S Р С G R R 0 R U А R R А D Ι Ι R Ι Ε Η Ν Т L В I С Т Т U D Ν L А А D R G Μ G А В A Μ А С 0

# Challenges

## **Dream Catcher**

Many Aboriginal peoples know the legend of the Dream Catcher. According to the legend, the good dreams go through the web and the bad dreams get tangled in the web and disappear.

A Dream Catcher looks like a spider web with 8 points connected to the ring. You be the artist.

- 1. Using Dream Catcher BLM, draw 8 equally spaced markings on the circle.
  - Draw a diameter on the circle.
  - □ Find the perpendicular bisector of the diameter.
  - □ Bisect each angle you create.
- 2. Draw the first row of webbing by joining each point on the circle to the point next to it with a straight line.
- 3. Draw the second row of webbing by connecting the midpoint of each chord to the midpoint of the chord next to it.
- **4.** Use 2 colours to show a central and an inscribed angle. Label each angle measure.
- 5. Continue drawing the rows of webbing until you get about 5 cm from the centre.

How many rows did you draw? \_\_\_\_\_

6. How is your drawing similar to an actual Dream Catcher?

#### Materials

- Dream Catcher BLM
- 1 ruler, protractor, and right triangle per student
- coloured pencils

![](_page_50_Picture_18.jpeg)

#### Answers

#### Get Ready, pages xx–xx

**1.** a) 15.7 cm b) 11.618 cm

**2.** Estimates may vary. **a)** 25°, 25° **b)** 100°, 105°

![](_page_51_Figure_4.jpeg)

#### Math Link, page x

- 2. b) diameter
- 3. b) centre
- 4. a) Estimates may vary. Example: 90° b) 90° c) Answers will vary. Example: My estimate was the same. d) 360°
- 5. equilateral; the sides are all the same length and the angles are equal
- 6. Answers will vary. Examples: Oakley, Starbucks Coffee ®

#### 10.1 Warm Up, page x

**1.** a) AC, BC, FC, EC, DC b) AE, BD

**2.** a) 13 cm b) 5 cm

**3.** a) 36 b) 100 c) 4 d) 7 e) 90 f) 45

- 10.1 Exploring Angles in a Circle, pages xx—xx
- Working Example 1: Show You Know

**a)** 55° **b)** 110°

Working Example 2: Show You Know

**a)** 90° **b)** 13 cm

Working Example 3: Show You Know

Answers may vary.

![](_page_51_Picture_22.jpeg)

The inscribed angle is half the central angle since it shares the same arc. Communicate the Ideas

**1.**  $\angle$ BCA is a central angle and shares the same arc, AB, with  $\angle$ BDA.

**2.** 90° because the inscribed angle is half the central angle  $(180 \div 2 = 90)$ . **Practise** 

**3.** 41°

- **4. a)** 23° **b)** 46°
- **5.** a) 90° b) 8 cm
- 6. Answers may vary.

![](_page_51_Picture_30.jpeg)

**7. a)** 76° **b)** ISOSCELES; AC and CD are both radii, so they are equal. **8. a)** 15° **b)** 24° **c)** 48° **d)** 30°

**9. a)** 56° **b)** 90°

10. Answers will vary. No. The inscribed angle is  $110^\circ$ , so  $\Delta$  ADB is not a right triangle.

10.1 Math Link, page x

a) Answers will vary.b) The central angle is twice the inscribed angle.10.2 Warm Up, page x

![](_page_51_Figure_36.jpeg)

**3.** 3 cm

**4.** a) 5 cm b) 4.5 cm

10.2 Exploring Chord Properties, pages xx-xx

Working Example 1: Show You Know

8 cm

Working Example 2: Show You Know

![](_page_51_Picture_43.jpeg)

Draw 2 chords. Draw the perpendicular bisectors of each chord. The point where the perpendicular bisectors meet is the centre.

#### Communicate the Ideas

- **1.** a)  $\angle$ ADC is 90°. b) AD and DB are equal.
- **2.** Draw 2 chords. Find the midpoint of each chord. Draw the perpendicular bisector of each chord. Mark with a dot the point where the perpendicular bisectors meet.
- **3.** 9 cm
- 4.8.1 mm
- **5.** Draw 2 chords. Draw the perpendicular bisectors of each chord. The point where the perpendicular bisectors meet is the centre.

#### Apply

- **6.** 30 m
- **7.** 5.2 cm
- **8.** 16 cm<sup>2</sup>

10.2 Math Link, page x

Answers will vary.

10.3 Warm Up, page x

1. a) equilateral b) right c) isosceles d) isosceles

- **2.** AB, ED
- **3. a)** 38° **b)** 100°

**4.** a)  $x = 115^{\circ}$  b)  $x = 138^{\circ}$ 

10.3 Tangents to a Circle, pages xx–xx

Working Example 1: Show You Know

**a)** 90° **b)** 56° **c)** 28°

#### Working Example 2: Show You Know

**a)** 40 mm **b)** 20 mm **c)** 34.6 mm

#### Working Example 3: Show You Know

73.3 m

#### Communicate the Ideas

**1.** No. The tangent must be outside the circle.

**2.** No.  $\angle$ CBA would be 90° if AB was tangent.

#### Practise

3. a) Isosceles. CG and CJ are both radii, so they are equal. b)  $20^\circ$ 

**4.** a) 90° b) 150° c) isosceles d) 15°

**5.** a) 8 m b) 4 m c) 90° d) 7 m

6. a) 15.8 m b) 10.8 m

#### Apply

7.12 cm

**8.** 148°

**9.** 30 cm

#### 10.3 Math Link, page x

Answers will vary.

#### Chapter Review, pages xx-xx

1. inscribed angle 2. central angle 3. radius 4. chord 5. perpendicular bisector 6. tangent

**7. a)** 24° **b)** 48°

**8. a)** 48° **b)** 48°

**9.** 90°

**10.** 18°

**11.** 48 m

12. 6.3 cm

**13.** 133°

14.6 mm

#### **15.** 130.8 m

#### Practice Test, pages xx-xx

**1.** C **2.** B **3.**  $36^{\circ}$  **4.** 9.4 cm **5.**  $50^{\circ}$  **6. a**)  $41^{\circ}$ . Inscribed angles with the same arc are equal. **b**)  $82^{\circ}$ . The measure of the central angle is twice the measure of the inscribed angle on the same arc.

7.13.7 mm

Math Link: Wrap It Up!, page x

Answers will vary.

#### Key Word Builder, page x

1. arc 2. central angle 3. chord 4. circumference 5. diameter 6. inscribed angle 7. midpoint 8. perpendicular bisector 9. Pythagorean relationship 10. radius 11. radii 12. tangent

#### Challenges, page x

Answers will vary.