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C Program Name: FEM1D           Length(INCLUDINMG BLANKS):2440 lines
C
C * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
C * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
C * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
C
C
C This is a finite element computer program for the analysis
C of following three model equations and others:
C
C 1. Heat transfer, fluid mechanics, bars, and cables:
C
C     CT.u* + CT.u** - (AX.u')' + CX.u = FX
C
C 2. The Timoshenko beam and circular plate theory:
C
C     CT0.w** - [AX.(w' + s)]' + CX.w = FX
C     CT1.s** - (BX.s')' + AX.(w' + s) = 0
C
C 3. The Euler-Bernoulli beam and circular plate theory:
C
C     CT.w** + (BX.w'')'' + CX.w = FX
C
C In the above equations (' ) and (*) denote differentiations
C with respect to space x and time t, and AX, BX, CX, CT, and
C FX are functions of x only:
C
C     AX = AX0 + AX1.X,   BX = BX0 + BX1.X,   CX = CX0 + CX1.X
C     CT = CT0 + CT1.X,   FX = FX0 + FX1.X + FX2.X.X
C
C In addition to the three model equations, other equations
C (for example, disks, trusses, and frames) can be analyzed by
C the program.
C
C
C
C . . . . .
C . . . . . KEY VARIABLES USED IN THE PROGRAM . . . . .
C . See Table 7.3.2 of the BOOK for a description of the variables. . . .
C . . . . .
C . NDF..... Number of degrees of freedom per node . . .
C . NEQ..... Number of equations in the model (before B. C.) . . .
C . NGP..... Number of Gauss points used in the evaluation of . . .
C . . . . . the element coefficients, ELK , ELF , ELM . . .
C . NHBW..... Half bandwidth of global coefficient matrix GLK . . .
C . NN ..... Number of total degrees of freedom in the element . . .
C . NPE..... Number of nodes per element . . .
C
C
C . . . . .
C . . . . . DIMENSIONS OF VARIOUS ARRAYS IN THE PROGRAM . . .
C . . . . .
C . Values of MXELM,MXNOD, etc. in the PARAMETER statement should . . .
C . . . . . be changed to meet the requirements of problem: . . .
C . . . . .
C . MXELM..... Maximum number of elements in the mesh: . . .
C . MXEBC..... Maximum number of speci. primary deg. of freedom . . .
C . MXMBC..... Maximum number of speci. mixed boundary conditions . . .
C . MXNBC..... Maximum number of speci. secondary deg. of freedom . . .
C . MXNEQ..... Maximum number of equations in the FE model . . .
C . MXNOD..... Maximum number of nodes in the mesh . . .
C
C . . . . .
C . NOTE: The following dimension statement in subroutine JACOBI . . .
C . . . . . should be modified when MXNEQ is greater than 500: . . .
C . . . . . DIMENSION V(500,500),VT(500,500),W(500,500),IH(500) . . .
C . . . . . The value of MXNEQ should be used in place of '500' . . .
C
C
C . . . . .
C . . . . . SUBROUTINES USED IN THE PROGRAM . . .
C . . . . .
C . ASSEMBLE, BOUNDARY, COEFFCNT, CONSTRNT, ECHODATA, EQNSOLVR, . . .
C . EIGNSLVR, JACOBI, MATRXMLT, MESH1D, POSTPROC, REACTION, . . .
C . . . . . SHAPE1D, TIMFORCE, TIMSTRES, TRANSFRM . . .
C
C IMPLICIT REAL*8 (A-H,O-Z)

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PARAMETER  (MXELM=250 , MXNEQ=500 , MXEBC=20 , MXNBC=20 , MXMBC=20 ,
*           MXNOD=250 , MXMPC=5)
DIMENSION DCAX (MXELM, 2) , DCBX (MXELM, 2) , DCCX (MXELM, 2) , DCFX (MXELM, 3)
DIMENSION GU0 (MXNEQ) , GU1 (MXNEQ) , GU2 (MXNEQ) , GPU (MXNEQ) , DX (MXNOD)
DIMENSION IBDY (MXEBC) , ISPV (MXEBC, 2) , ISSV (MXNBC, 2) , INBC (MXMBC, 2)
DIMENSION IMC1 (MXMPC, 2) , IMC2 (MXMPC, 2) , VMPC (MXMPC, 4)
DIMENSION ICON (9) , VCON (9) , TRM (MXNEQ, MXNEQ)
DIMENSION GLM (MXNEQ, MXNEQ) , GLF (MXNEQ) , GLX (MXNOD) , NOD (MXELM, 4)
DIMENSION CS (MXELM) , SN (MXELM) , CNT (MXELM) , SNT (MXELM) , XB (MXELM)
DIMENSION EGNVAL (MXNEQ) , EGNVEC (MXNEQ, MXNEQ) , GLK (MXNEQ, MXNEQ)
DIMENSION PR (MXELM) , SE (MXELM) , SL (MXELM) , SA (MXELM) , SI (MXELM)
DIMENSION HF (MXELM) , VF (MXELM) , PF (MXELM) , F3 (MXELM) , TITLE (20)
DIMENSION UREF (MXMBC) , VSPV (MXEBC) , VSSV (MXNBC) , VNBC (MXMBC)
COMMON /STF1/ ELK(9,9) , ELM(9,9) , ELF(9) , ELX(4) , ELU(9) , ELV(9) , ELA(9)
COMMON /STF2/ A1,A2,A3,A4,A5,AX0,AX1,BX0,BX1,CX0,CX1,CT0,CT1,FX0,
*             FX1,FX2
COMMON /IO/ IN, IT

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P R E P R O C E S S O R U N I T

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C
C
C
C
C
IN=5
IT=6
open (in,file=' ')
open (it,file=' ')
NT=0
NSSV=0
JVEC=1
TIME=0.0D0
TOLRNS=1.0D-06
CALL ECHODATA(IN, IT)
C
READ (IN, 300) TITLE
READ (IN, *) MODEL,NTYPE,ITEM
READ (IN, *) IELEM,NEM
READ (IN, *) ICONT,NPRNT
C
IF (MODEL.GE.3) THEN
  NPE=2
  IF (MODEL.EQ.4 .AND. NTYPE.GE.1) THEN
    NDF=3
  ELSE
    NDF=2
  ENDIF
  IF (MODEL.EQ.4 .AND. NTYPE.EQ.2) THEN
    IELEM=1
  ELSE
    IELEM=0
  ENDIF
ELSE
  IF (MODEL.EQ.2) THEN
    NDF=2
    IF (NTYPE.GT.1) IELEM=1
  ELSE
    NDF=1
  ENDIF
  NPE=IELEM+1
ENDIF
C
Data input for BAR-LIKE and BEAM problems (MODEL=1, 2, AND 3)
C
IF (MODEL.NE.4) THEN
  IF (ICONT.NE.0) THEN
    NNM = NEM*(NPE-1)+1
    NEM1=NEM + 1
    READ (IN, *) (DX(I), I=1,NEM1)
    CALL MESH1D(NEM,NPE,NOD,MXELM,MXNOD,DX,GLX)
    READ (IN, *) AX0,AX1
    READ (IN, *) BX0,BX1
    READ (IN, *) CX0,CX1
    IF (ITEM.LT.3) THEN
      READ (IN, *) FX0,FX1,FX2
    ENDIF
  ELSE

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C
C      Read GLX, NOD, and element-wise continuous coefficients [DC.X]
C
C          READ(IN,*)NNM
C          DO 10 N=1,NEM
C              READ(IN,*) (NOD(N,I),I=1,NPE), GLX(N)
C              READ(IN,*) (DCAX(N,I),I=1,2)
C              READ(IN,*) (DCBX(N,I),I=1,2)
C              READ(IN,*) (DCCX(N,I),I=1,2)
C          10     READ(IN,*) (DCFX(N,I),I=1,3)
C          ENDIF
C      ELSE
C
C          Input data for plane TRUSS or FRAME structures (MODEL=4)
C
C          READ(IN,*)NNM
C          IF(NTYPE.NE.0)THEN
C              DO 20 N=1,NEM
C                  READ(IN,*) PR(N),SE(N),SL(N),SA(N),SI(N),CS(N),SN(N)
C                  READ(IN,*) HF(N),VF(N),PF(N),XB(N),CNT(N),SNT(N)
C          20     READ(IN,*) (NOD(N,I),I=1,2)
C          ELSE
C              DO 30 N=1,NEM
C                  READ(IN,*) SE(N),SL(N),SA(N),CS(N),SN(N),HF(N)
C          30     READ(IN,*) (NOD(N,I),I=1,2)
C          ENDIF
C          READ(IN,*) NCON
C          IF(NCON.NE.0)THEN
C              DO 35 I=1, NCON
C                  READ(IN,*) ICON(I),VCON(I)
C              ENDIF
C          ENDIF
C          NEQ=NNM*NDF
C
C          Read data on BOUNDARY CONDITIONS of three kinds: Dirichlet (PV)
C          Neumann (SV), and Newton's (MIXED) types
C
C          READ(IN,*) NSPV
C          IF(NSPV.NE.0)THEN
C              DO 40 NB=1,NSPV
C                  IF(ITEM.GT.2)THEN
C                      READ(IN,*) (ISPV(NB,J),J=1,2)
C                  ELSE
C                      READ(IN,*) (ISPV(NB,J),J=1,2),VSPV(NB)
C                  ENDIF
C          40     CONTINUE
C          ENDIF
C
C          IF(ITEM.LE.2)THEN
C              READ(IN,*) NSSV
C              IF(NSSV.NE.0)THEN
C                  DO 50 IB=1,NSSV
C                      READ(IN,*) (ISSV(IB,J),J=1,2),VSSV(IB)
C          50     ENDIF
C          ENDIF
C
C          READ(IN,*) NNBC
C          IF(NNBC.NE.0)THEN
C              DO 60 I=1, NNBC
C                  READ(IN,*) (INBC(I,J),J=1,2),VNBC(I),UREF(I)
C          60     ENDIF
C
C          Read data on multi-point constraints
C
C          READ(IN,*) NMPC
C          IF(NMPC.NE.0)THEN
C              DO 65 I=1, NMPC
C                  READ(IN,*) (IMC1(I,J),J=1,2),(IMC2(I,J),J=1,2),(VMPC(I,J),J=1,4)
C          65     ENDIF
C
C          IF(ITEM .NE. 0)THEN
C
C              Input data here for TIME-DEPENDENT problems
C
C              IF(ITEM.LE.3)THEN
C                  READ(IN,*) CT0,CT1

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ENDIF
IF(ITEM.LE.2) THEN
  READ(IN,*) DT,ALFA,GAMA
  READ(IN,*) INCOND,NTIME,INTVL
  A1=ALFA*DT
  A2=(1.0-ALFA)*DT
  IF(INCOND.NE.0) THEN
    READ(IN,*) (GU0(I),I=1,NEQ)
  ELSE
    DO 70 I=1,NEQ
      GU0(I)=0.0
  ENDIF
70
  IF(ITEM.EQ.2) THEN
    A3=2.0/GAMA/(DT*DT)
    A4=A3*DT
    A5=1.0/GAMA-1.0
    IF(INCOND.NE.0) THEN
      READ(IN,*) (GU1(I),I=1,NEQ)
    ELSE
      DO 80 I=1,NEQ
        GU1(I)=0.0
        GU2(I)=0.0
    ENDIF
80
  ENDIF
ENDIF
ENDIF
C
C -----
C   E   N   D       O   F       T   H   E       I   N   P   U   T       D   A   T   A
C -----
C Compute the half BANDWIDTH of the coefficient matrix GLK
C
NHBW=0.0
DO 90 N=1,NEM
DO 90 I=1,NPE
DO 90 J=1,NPE
  NW=(IABS(NOD(N,I)-NOD(N,J))+1)*NDF
90 IF(NHBW.LT.NW) NHBW=NW
C
C -----
C   P   R   I   N   T       T   H   E       I   N   P   U   T       D   A   T   A
C -----
C
WRITE(IT,530)
WRITE(IT,310)
WRITE(IT,530)
WRITE(IT,300) TITLE
WRITE(IT,320) MODEL,NTYPE
WRITE(IT,350) IELEM,NDF,NEM,NEQ,NHBW,NSPV,NSSV,NNBC,NMPC
C
  IF(ITEM.NE.0) THEN
    IF(ITEM.LE.2) THEN
      WRITE(IT,330)
      WRITE(IT,390) CT0,CT1,ALFA,GAMA,DT,NTIME,INTVL
      IF(INCOND.NE.0) THEN
        WRITE(IT,370)
        WRITE(IT,540) (GU0(I),I=1,NEQ)
      IF(ITEM.EQ.2) THEN
        WRITE(IT,380)
        WRITE(IT,540) (GU1(I),I=1,NEQ)
      ENDIF
    ENDIF
    ELSE
      WRITE(IT,340)
      IF(ITEM.LE.3) THEN
        WRITE(IT,400) CT0,CT1
      ENDIF
    ENDIF
  ENDIF
C
  IF(NSPV.NE.0) THEN
    WRITE(IT,480)
    DO 100 IB=1,NSPV
    IF(ITEM.LE.2) THEN
      WRITE(IT,490) (ISPV(IB,J),J=1,2),VSPV(IB)
    ELSE

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        WRITE(IT,490) (ISPV(IB,J),J=1,2)
    ENDIF
100    CONTINUE
    ENDIF
C
    IF(NSSV.NE.0)THEN
        WRITE(IT,500)
        DO 110 IB=1,NSSV
110        WRITE(IT,490) (ISSV(IB,J),J=1,2),VSSV(IB)
    ENDIF
C
    IF(NNBC.NE.0)THEN
        WRITE(IT,510)
        DO 120 I=1,NNBC
120        WRITE(IT,490) (INBC(I,J),J=1,2),VNBC(I),UREF(I)
    ENDIF
C
    IF(NMPC.NE.0)THEN
        WRITE(IT,515)
        DO 125 I=1, NMPC
125        WRITE(IT,495) (IMC1(I,J),J=1,2),(IMC2(I,J),J=1,2),
*                           (VMPC(I,J),J=1,4)
    ENDIF
C
    IF(MODEL.NE.4)THEN
        IF(ICONT.EQ.1)THEN
            WRITE(IT,410)
            WRITE(IT,540) (GLX(I),I=1,NNM)
            WRITE(IT,420)
            IF(MODEL.NE.3)THEN
                WRITE(IT,440) AX0,AX1,BX0,BX1,CX0,CX1,FX0,FX1,FX2
            ELSE
                WRITE(IT,445) AX0,AX1,BX0,BX1,CX0,CX1
            ENDIF
        ELSE
            DO 130 N=1,NEM
            WRITE(IT,430) N,GLX(N)
130        WRITE(IT,440) (DCAX(N,I),I=1,2),(DCBX(N,I),I=1,2),
*                           (DCCX(N,I),I=1,2),(DCFX(N,I),I=1,3)
            ENDIF
        ELSE
            DO 140 N=1,NEM
            WRITE(IT,460) N
            IF(NTYPE.NE.0)THEN
                WRITE(IT,450) PR(N),SE(N),SL(N),SA(N),SI(N),CS(N),SN(N),
*                               HF(N),VF(N),PF(N),XB(N),CNT(N),SNT(N),
*                               (NOD(N,I),I=1,2)
            ELSE
                WRITE(IT,470) SE(N),SL(N),SA(N),CS(N),SN(N),HF(N),
*                               (NOD(N,I),I=1,2)
            ENDIF
        ENDIF
140    CONTINUE
    ENDIF
C
C          |           P R O C E S S O R   U N I T           |
C
C      TIME MARCHING scheme begins here. For ITEM=2, initial conditions
C      on second derivatives of the solution are computed in the program
C
    IF(ITEM.NE.0)THEN
        IF(ITEM.EQ.1)THEN
            NT=NT+1
            TIME=TIME+DT
        ENDIF
    ENDIF
C
    IF(ITEM.GE.3)NHBW=NEQ
C
C      Initialize global matrices and vectors
C
150 DO 160 I=1,NEQ
    GLF(I)=0.0
    DO 160 J=1,NHBW

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```

IF (ITEM.GE.3) THEN
  GLM(I,J)=0.0
ENDIF
160 GLK(I,J)=0.0
C
C      Do-loop for ELEMENT CALCULATIONS and ASSEMBLY
C
DO 200 NE = 1, NEM
IF (MODEL.NE.4) THEN
  IF (ICONT.NE.1) THEN
    AX0=DCAX(NE,1)
    AX1=DCAX(NE,2)
    BX0=DCBX(NE,1)
    BX1=DCBX(NE,2)
    CX0=DCCX(NE,1)
    CX1=DCCX(NE,2)
    FX0=DCFX(NE,1)
    FX1=DCFX(NE,2)
    FX2=DCFX(NE,3)
  ENDIF
C
  L=0
  DO 180 I=1,NPE
    NI=NOD(NE,I)
    IF (ICONT.EQ.1) THEN
      ELX(I)=GLX(NI)
    ELSE
      ELX(1)=0.0
      ELX(2)=0.5*GLX(NE)
      ELX(NPE)=GLX(NE)
    ENDIF
    IF (ITEM.EQ.1 .OR. ITEM.EQ.2) THEN
      LI=(NI-1)*NDF
      DO 170 J=1,NDF
        LI=LI+1
        L=L+1
        ELU(L)=GU0(LI)
        IF (ITEM.EQ.2 .AND. NT.GT.0) THEN
          ELV(L)=GU1(LI)
          ELA(L)=GU2(LI)
        ENDIF
      170 CONTINUE
    ENDIF
  180 CONTINUE
C
  CALL COEFFCNT(IELEM,ITEM,MODEL,NDF,NPE,TIME,NTYPE,NE,F3,MXELM)
ELSE
  CALL TRANSFRM(MXELM,NE,NTYPE,PR,SE,SL,SA,SI,CS,SN,CNT,SNT,
*                  HF,VF,PF,XB)
ENDIF
C
IF (NPRNT .NE.0) THEN
  NN = NPE*NDF

  IF (NPRNT .LE.2) THEN
    IF (NE.LE.5 .AND. NT.LE.1) THEN
      WRITE(IT,550)
      DO 190 I=1,NN
        WRITE(IT,540) (ELK(I,J),J=1,NN)
    190 IF (ITEM.GE.3) THEN
      WRITE(IT,360)
      DO 195 I=1,NN
        WRITE(IT,540) (ELM(I,J),J=1,NN)
    195 ELSE
      WRITE(IT,560)
      WRITE(IT,540) (ELF(I),I=1,NN)
    ENDIF
    ENDIF
  ENDIF
ENDIF
C
C      Assemble element matrices
C
CALL ASSEMBLE(NOD,MXELM,MXNEQ,NDF,NPE,NE,ITEM,GLK,GLM,GLF)
C
200 CONTINUE

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```

C
C Call subroutine CONSTRNT to impose constraint boundary conditions,
C for example, inclined support conditions
C
IF (MODEL.EQ.4) THEN
  IF (NCON.NE.0) THEN

    CALL CONSTRNT (NEQ,NHBW,NDF,NCON,ICON,VCON,GLK,GLM,GLF,TRM,MXNEQ)
    ENDIF
  ENDIF

C
C Impose multi-point constraints using the penalty method
C
IF (NMPC.NE.0) THEN
  IF (NPRNT.EQ.2) THEN
    WRITE (IT,570)
    DO 201 I=1,NEQ
      WRITE (IT,540) (GLK(I,J),J=1,NHBW)
    ENDIF
    VMAX=0.0
    DO 204 I=1,NEQ
      DO 204 J=I,NHBW
        VALUE=DABS(GLK(I,J))
        IF (VALUE.GT.VMAX) THEN
          VMAX=VALUE
        ENDIF
    204 CONTINUE
    PNLTY=VMAX*1.0E4
    DO 205 NC=1,NMPC
      NDOF1=(IMC1(NC,1)-1)*NDF+IMC1(NC,2)
      NDOF2=(IMC2(NC,1)-1)*NDF+IMC2(NC,2)
      GLK(NDOF1,1)=GLK(NDOF1,1)+PNLTY*VMPC(NC,1)*VMPC(NC,1)
      GLK(NDOF2,1)=GLK(NDOF2,1)+PNLTY*VMPC(NC,2)*VMPC(NC,2)
      GLF(NDOF1)=GLF(NDOF1)+PNLTY*VMPC(NC,1)*VMPC(NC,3)
      GLF(NDOF2)=GLF(NDOF2)+PNLTY*VMPC(NC,2)*VMPC(NC,3)
      IF (NDOF1.GT.NDOF2) THEN
        NW=NDOF1-NDOF2+1
        GLK(NDOF2,NW)=GLK(NDOF2,NW)+PNLTY*VMPC(NC,1)*VMPC(NC,2)
        GLF(NDOF1)=VMPC(NC,4)
      ELSE
        NW=NDOF2-NDOF1+1
        GLK(NDOF1,NW)=GLK(NDOF1,NW)+PNLTY*VMPC(NC,1)*VMPC(NC,2)
        GLF(NDOF2)=VMPC(NC,4)
      ENDIF
    205 CONTINUE
  ENDIF

C
IF (NPRNT.EQ.2) THEN
C
C Print assembled coefficient matrices if required
C
  WRITE (IT,570)
  DO 210 I=1,NEQ
    WRITE (IT,540) (GLK(I,J),J=1,NHBW)
    IF (ITEM.GE.3) THEN
      WRITE (IT,575)
      DO 215 I=1,NEQ
        WRITE (IT,540) (GLM(I,J),J=1,NHBW)
    215 ELSE
      WRITE (IT,580)
      WRITE (IT,540) (GLF(I),I=1,NEQ)
    ENDIF
  ENDIF

C
C Call subroutine BOUNDARY to impose essential, natural and Newton's
C type boundary conditions on the primary and secondary variables.
C
CALL BOUNDARY(NEQ,NEQR,NHBW,NSPV,NSSV,NNBC,NDF,DT,ITEM,ALFA,IBDY,
*           ISPV,ISSV,INBC,UREF,VSPV,VSSV,VNBC,GLK,GLM,GLF,GU0,
*           MXEBC,MXNBC,MXMBC,MXNEQ)

IF (NPRNT.EQ.2) THEN
C
C Print assembled coefficient matrices if required
C

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        WRITE (IT,570)
        DO 211 I=1,NEQ
211      WRITE (IT,540) (GLK(I,J),J=1,NHBW)
      ENDIF

C
C      IF (ITEM.GE.3) THEN
C
C      Call subroutine EIGNSLVR to solve for the eigenvalues and eigenvectors
C
C      CALL EGNSOLVR (NEQR,GLK,GLM,EGNVAL,EGNVEC,JVEC,NROT,MXNEQ)
C
C      WRITE (IT,690) NROT
C      DO 230 NVEC=1,NEQR
C      FRQNCY=DSQRT(EGNVAL(NVEC))
C      WRITE (IT,700) NVEC,EGNVAL(NVEC),FRQNCY
230      WRITE (IT,540) (EGNVEC(I,NVEC),I=1,NEQR)
          STOP
      ENDIF

C      IRES = 0
C
C      Call subroutine EQNSOLVR to solve the finite-element equations
C
C      CALL EQNSOLVR (MXNEQ,MXNEQ,NEQ,NHBW,GLK,GLF,IRES)
C
C      IF (ITEM.EQ.0) THEN
C          WRITE (IT,590)
C          WRITE (IT,540) (GLF(NI),NI=1,NEQ)
C      ELSE
C          IF (NT.EQ.0) THEN
C              DO 240 I=1,NEQ
240          GU2(I)=GLF(I)
              NT=NT+1
              TIME=TIME+DT
              GOTO 150
          ENDIF

C      Compute and print current values of GU0, GU1, and GU2
C
C      DO 250 I=1,NEQ
C      IF (ITEM.EQ.2) THEN
C          ACCLRN=A3*(GLF(I)-GU0(I))-A4*GU1(I)-A5*GU2(I)
C          GU1(I)=GU1(I)+A2*GU2(I)+A1*ACCLRN
C          GU2(I)=ACCLRN
C          GPU(I)=GU0(I)
C      ELSE
C          GPU(I)=GU0(I)
C      ENDIF
250      GU0(I)=GLF(I)

C      DIFF=0.0
C      SOLN=0.0
C      DO 260 I=1,NEQ
260      SOLN=SOLN+GU0(I)*GU0(I)
      DIFF=DIFF+(GLF(I)-GPU(I))**2
      PRCNT=DSQRT(DIFF/SOLN)
      IF (PRCNT.LE.TOLRNS) THEN
          WRITE (IT,640)
          WRITE (IT,540) (GPU(I),I=1,NEQ)
          WRITE (IT,540) (GU0(I),I=1,NEQ)
          STOP
      ELSE
          IF (INTVL.LE.0) INTVL=1
          NTEN=(NT/INTVL)*INTVL
          IF (NTEN.EQ.NT) THEN
              WRITE (IT,600) TIME, NT
              WRITE (IT,590)
              WRITE (IT,540) (GU0(I),I=1,NEQ)
              IF (ITEM.NE.1) THEN
                  IF (NPRNT.LT.4) THEN
                      WRITE (IT,645)
                      WRITE (IT,540) (GU1(I),I=1,NEQ)
                      WRITE (IT,646)
                      WRITE (IT,540) (GU2(I),I=1,NEQ)
                  ENDIF
              ENDIF
          ENDIF
      ENDIF

```

```

        ENDIF
        NT=NT+1
        TIME=TIME+DT
    ELSE
        NT=NT+1
        TIME=TIME+DT
        GOTO 150
    ENDIF
ENDIF
C
C
C
C
C
    | P O S T - P R O C E S S O R U N I T |
C
IF (NMPC.EQ.0) THEN
    IF (NPRNT.LE.1) THEN
        IF (MODEL.EQ.1) THEN
            WRITE (IT,530)
        ELSE
            IF (MODEL.EQ.4) THEN
                WRITE (IT,630)
            ENDIF
            WRITE (IT,520)
        ENDIF
    ELSE
        IF (MODEL.EQ.1) THEN
            WRITE (IT,647)
        IF (NTYPE.EQ.0) THEN
            WRITE (IT,610)
        ELSE
            WRITE (IT,620)
        ENDIF
    ENDIF
C
    IF (MODEL.EQ.2 .OR. MODEL.EQ.3) THEN
        WRITE (IT,647)

        IF (NTYPE.EQ.0) THEN
            WRITE (IT,650)
        ELSE
            WRITE (IT,660)
        ENDIF
    ENDIF
C
    IF (MODEL.EQ.4) THEN
        IF (NTYPE.EQ.0) THEN
            WRITE (IT,680)
        ELSE
            WRITE (IT,670)
        ENDIF
    ENDIF
C
    IF (MODEL.EQ.1) THEN
        WRITE (IT,530)
    ELSE
        WRITE (IT,520)
    ENDIF
C
    IF (MODEL.LE.3) THEN
        CALL POSTPROC(DCAX,DCBX,DCCX,F3,GLF,GLX,NOD,ICONT,IELEM,NPE,
        *               MODEL,NTYPE,ITEM,MXELM,MXNEQ,MXNOD,NEM,NDF)
    ELSE
        CALL REACTION(MXELM,MXNEQ,NDF,NEM,NOD,NPE,NTYPE,PR,GLF,
        *               SE,SL,SA,SI,CS,SN,CNT,SNT,HF,VF,PF,XB)
    ENDIF
C
    IF (MODEL.EQ.1) THEN
        WRITE (IT,530)
    ELSE
        WRITE (IT,520)
    ENDIF
ENDIF
ELSE

```

```

C      Calculate the reactions at the points where constraints are imposed
C
DO 280 NC=1,NMPC
NDOF1=(IMC1(NC,1)-1)*NDF+IMC1(NC,2)
NDOF2=(IMC2(NC,1)-1)*NDF+IMC2(NC,2)
GU0 (NC)=-PNLTY*VMPC(NC,1)*(VMPC(NC,1)*GLF(NDOF1)
*           +VMPC(NC,2)*GLF(NDOF2)-VMPC(NC,3))
*           GU1 (NC)=-PNLTY*VMPC(NC,2)*(VMPC(NC,1)*GLF(NDOF1)
*           +VMPC(NC,2)*GLF(NDOF2)-VMPC(NC,3))
280 CONTINUE
WRITE(IT,545)
WRITE(IT,540)(GU0(I),I=1,NMPC)
WRITE(IT,540)(GU1(I),I=1,NMPC)
ENDIF
C
IF(ITEM.EQ.0)STOP
IF(NT.LT.NTIME)THEN
  IF(PRCNT.GT.TOLRNS)THEN
    GOTO 150
  ENDIF
ELSE
  WRITE(IT,710)
ENDIF
C
C-----F   O   R   M   A   T   S-----C
C-----F   O   R   M   A   T   S-----C
C-----F   O   R   M   A   T   S-----C
300 FORMAT(20A4)
310 FORMAT(8X,'OUTPUT from program FEM1D by J N REDDY')
320 FORMAT(/,4X,'*** ANALYSIS OF MODEL',I2,', AND TYPE',I2,
*           ' PROBLEM ***',/,15X,'(see the code below)',/,
*           /,4X,'MODEL=1,NTYPE=0: A problem described by MODEL EQ. 1',
*           /,4X,'MODEL=1,NTYPE=1: A circular DISK (PLANE STRESS)',
*           /,4X,'MODEL=1,NTYPE>1: A circular DISK (PLANE STRAIN)',
*           /,4X,'MODEL=2,NTYPE=0: A Timoshenko BEAM (RIE) problem',
*           /,4X,'MODEL=2,NTYPE=1: A Timoshenko PLATE (RIE) problem',
*           /,4X,'MODEL=2,NTYPE=2: A Timoshenko BEAM (CIE) problem',
*           /,4X,'MODEL=2,NTYPE>2: A Timoshenko PLATE (CIE) problem',
*           /,4X,'MODEL=3,NTYPE=0: A Euler-Bernoulli BEAM problem',
*           /,4X,'MODEL=3,NTYPE>0: A Euler-Bernoulli Circular plate',
*           /,4X,'MODEL=4,NTYPE=0: A plane TRUSS problem',
*           /,4X,'MODEL=4,NTYPE=1: A Euler-Bernoulli FRAME problem',
*           /,4X,'MODEL=4,NTYPE=2: A Timoshenko (CIE) FRAME problem',/)
330 FORMAT(/,4X,'TIME-DEPENDENT (TRANSIENT) ANALYSIS ',/)
340 FORMAT(/,4X,'E I G E N V A L U E A N A L Y S I S ',/)
350 FORMAT(/,8X,'Element type (0, Hermite,>0, Lagrange)...=',I4,/,
*           8X,'No. of deg. of freedom per node, NDF....=',I4,/,
*           8X,'No. of elements in the mesh, NEM.....=',I4,/,
*           8X,'No. of total DOF in the model, NEQ.....=',I4,/,
*           8X,'Half bandwidth of matrix [GLK], NHBW ....=',I4,/,
*           8X,'No. of specified primary DOF, NSPV.....=',I4,/,
*           8X,'No. of specified secondary DOF, NSSV.....=',I4,/,
*           8X,'No. of specified Newton B. C.: NNBC.....=',I4,/,
*           8X,'No. of speci. multi-pt. cond.: NMPC.....=',I4)
360 FORMAT(/,3X,'Element coefficient matrix, [ELM] : ',/)
370 FORMAT(/,3X,'Initial conditions on the primary variables:',/)
380 FORMAT(/,3X,'Initial cond. on time der. of primary variables:',/)
390 FORMAT(/,8X,'Coefficient, CT0.....=',E12.4,/,
*           8X,'Coefficient, CT1.....=',E12.4,/,
*           8X,'Parameter, ALFA.....=',E12.4,/,
*           8X,'Parameter, GAMA.....=',E12.4,/,
*           8X,'Time increment, DT.....=',E12.4,/,
*           8X,'No. of time steps, NTIME.....=',I4,/,
*           8X,'Time-step interval to print soln., INTVL=',I4,/)
400 FORMAT(/,8X,'Coefficient, CT0.....=',E12.4,/,
*           8X,'Coefficient, CT1.....=',E12.4,/)
410 FORMAT(/,3X,'Global coordinates of the nodes, {GLX}: ',/)
420 FORMAT(/,3X,'Coefficients of the differential equation:',/)
430 FORMAT(/,5X,'Properties of Element =',I3,/,
*           8X,'Element length, H ..... =',E12.4)
440 FORMAT( 8X,'AX0 =',E12.4,5X,'AX1 =',E12.4,/,
*           8X,'BX0 =',E12.4,5X,'BX1 =',E12.4,/,
*           8X,'CX0 =',E12.4,5X,'CX1 =',E12.4,/,
*           8X,'FX0 =',E12.4,5X,'FX1 =',E12.4,5X,'FX2 =',E12.4,/)
445 FORMAT( 8X,'AX0 =',E12.4,5X,'AX1 =',E12.4,/

```

```

*      8X,'BX0 =',E12.4,5X,'BX1 =',E12.4,/,  

*      8X,'CX0 =',E12.4,5X,'CX1 =',E12.4,/)
450 FORMAT(8X,'The poisson ratio,          PR..... =',E12.4,/,  

*      8X,'Modulus of elasticity,       SE..... =',E12.4,/,  

*      8X,'Length of the element,     SL..... =',E12.4,/,  

*      8X,'Area of cross section,    SA..... =',E12.4,/,  

*      8X,'Moment of inertia,        SI..... =',E12.4,/,  

*      8X,'Cosine of orientation,   CN..... =',E12.4,/,  

*      8X,'Sine of orientation,     SN..... =',E12.4,/,  

*      8X,'Axial body force (constant), HF..... =',E12.4,/,  

*      8X,'Transverse body force (cnst), VF..... =',E12.4,/,  

*      8X,'Internal point force,     PF..... =',E12.4,/,  

*      8X,'Location of PF from node 1, XB..... =',E12.4,/,  

*      8X,'Orientation of PF: cosine, CST..... =',E12.4,/,  

*      8X,'Orientation of PF: sine, SNT..... =',E12.4,/,  

*      8X,'Nodal connectivity:      NOD(I,J) .. =',2I6,/)
460 FORMAT(//,3X,'Element No. =', I3,/)  

470 FORMAT(8X,'Modulus of elasticity,       SE..... =',E12.4,/,  

*      8X,'Length of the element,     SL..... =',E12.4,/,  

*      8X,'Area of cross section,    SA..... =',E12.4,/,  

*      8X,'Cosine of orientation,   CN..... =',E12.4,/,  

*      8X,'Sine of orientation,     SN..... =',E12.4,/,  

*      8X,'Axial body force (constant), HF..... =',E12.4,/,  

*      8X,'Nodal connectivity:      NOD(I,J) .. =',2I6,/)
480 FORMAT(//,3X, 'Boundary information on primary variables:',/)  

490 FORMAT(5X,2I5,2E15.5)  

495 FORMAT(5X,2I5,2X,2I5,/,5X,4E15.5)

500 FORMAT(//,3X, 'Boundary information on secondary variables:',/)  

510 FORMAT(//,3X, 'Boundary information on mixed boundary cond.:',/)  

515 FORMAT(//,3X, 'Multi-point constraint information:',/)  

520 FORMAT(2X,78(' '),/)  

530 FORMAT(2X,55(' '),/)  

540 FORMAT(2X,5E13.5)  

545 FORMAT(//,3X,'Forces at the constrained points:',/)

550 FORMAT(//,3X,'Element coefficient matrix, [ELK] :',/)  

560 FORMAT(//,3X,'Element source vector, {ELF} :',/)  

570 FORMAT(//,3X,'Global coefficient matrix, [GLK] :',/)  

575 FORMAT(//,3X,'Global coefficient matrix, [GLM] :',/)  

580 FORMAT(//,3X,'Global source vector, {GLF} :',/)  

590 FORMAT(//,1X,'SOLUTION (values of PVs) at the NODES: ',/)  

600 FORMAT(//,1X,'TIME =',E12.4,5X,'Time step number =',I3,/)'  

610 FORMAT(7X,' x ',5X,'P. Variable',2X,'S. Variable')  

620 FORMAT(7X,' x ',3X,'Displacement',2X,'Radial Stress',2X,  

*      'Hoop Stress')  

630 FORMAT(//,15X,'Generalized internal forces in the element',/  

* 5X,'(second line gives the results in the global coordinates)')  

640 FORMAT(//,3X,'*** THE SOLUTION HAS REACHED A STEADY STATE ***',/  

* 3X,'SOLUTION AT THE TWO CONSECUTIVE TIME STEPS FOLLOWS:')  

645 FORMAT(//,2X,'FIRST TIME DERIVATIVE of the primary variables:',/)  

646 FORMAT(//,2X,'SECOND TIME DERIVATIVE of the primary variables:',/)  

647 FORMAT(3X,'x is the global coord. if ICONT=1 and it is the local',/  

*      ' coord. if ICONT=0')  

650 FORMAT(7X,' x ',6X,'Deflect.',5X,'Rotation',5X,'B. Moment',/  

* 3X,'Shear Force')  

660 FORMAT(7X,' x ',6X,'Deflect.',5X,'Rotation',4X,'Moment, Mr',/  

* 3X,'Moment, Mt',3X,'Shear Force')  

670 FORMAT(3X,'Ele Force, H1 Force, V1 Moment, M1 Force, H2  

*Force, V2 Moment, M2')  

680 FORMAT(3X,'Ele Force, H1 Force, V1 Force, H2 Force, V2')  

690 FORMAT(//,5X,'Number of rotations taken in JACOBI =',I4,/)'  

700 FORMAT(//,5X,'EIGENVALUE(',I2,') = ',E14.6,2X,'SQRT(EGNVAL) = ',/  

* E13.5,/,5X,'EIGENVECTOR:')  

710 FORMAT(//,5X,'***** Number of time steps exceeded NTIME *****',/)  

close(in)  

close(it)  

STOP  

END

```

SUBROUTINE ASSEMBLE (NOD, MXELM, MXNEQ, NDF, NPE, NE, ITEM, GLK, GLM, GLF)

C
C
C The subroutine is called in MAIN to assemble element coefficient
matrices (in a upper banded matrix form) and right-hand vectors

```

C
C     {ELF}..... Element source vector, {f}
C     {ELK}..... Element coefficient matrix, [K]
C     {ELM}..... Element coefficient matrix, [M]
C     [NOD].... Connectivity matrix, [B]
C


---


C     IMPLICIT REAL*8 (A-H,O-Z)
C     DIMENSION GLK(MXNEQ,MXNEQ),GLM(MXNEQ,MXNEQ),GLF(MXNEQ),
C     *          NOD(MXELM,4)
C     COMMON/STF1/ELK(9,9),ELM(9,9),ELF(9),ELX(4),ELU(9),ELV(9),ELA(9)
C     IF (ITEM.LE.2) THEN
C
C     Assemble element coefficient matrix ELK and source vector ELF
C
C     DO 50 I = 1, NPE
C     NR = (NOD(NE,I) - 1)*NDF
C     DO 40 II = 1, NDF
C     NR = NR + 1
C     L = (I-1)*NDF + II
C     GLF(NR) = GLF(NR) + ELF(L)
C     DO 30 J = 1, NPE
C     NCL = (NOD(NE,J)-1)*NDF
C     DO 20 JJ = 1, NDF
C     M = (J-1)*NDF + JJ
C     NC = NCL-NR+JJ+1
C     IF (NC) 20,20,10
C 10    GLK(NR,NC) = GLK(NR,NC) + ELK(L,M)
C 20    CONTINUE
C 30    CONTINUE
C 40    CONTINUE
C 50    CONTINUE
C     ELSE
C
C     ASSEMBLE ELEMENT MATRICES INTO FULL GLOBAL MATRICES
C
C     DO 100 I=1,NPE
C     NR=(NOD(NE,I)-1)*NDF
C     DO 90 II=1,NDF
C     NR=NR+1
C     L=(I-1)*NDF+II
C     DO 80 J=1,NPE
C     NC=(NOD(NE,J)-1)*NDF
C     DO 70 JJ=1,NDF
C     M=(J-1)*NDF+JJ
C     NC=NC+1
C     GLK(NR,NC)=GLK(NR,NC)+ELK(L,M)
C 60    GLM(NR,NC)=GLM(NR,NC)+ELM(L,M)
C 70    CONTINUE
C 80    CONTINUE
C 90    CONTINUE
C 100   CONTINUE
C
C     ENDIF
C     RETURN
C     END
C
C     SUBROUTINE BOUNDARY (NEQ,NEQR,NHBW,NSPV,NSSV,NNBC,NDF,DT,ITEM,ALFA,
C     *                      IBDY,ISPV,ISSV,INBC,UREF,VSPV,VSSV,VNBC,
C     *                      GLK,GLM,GLF,GU0,MXEBC,MXNBC,MXMBC,MXNEQ)
C
C     The subroutine is called in MAIN to implement specified boundary
C     conditions on the assembled system of finite element equations
C


---


C     IMPLICIT REAL*8 (A-H,O-Z)
C     DIMENSION ISPV(MXEBC,2),ISSV(MXNBC,2),INBC(MXMBC,2),IBDY(MXEBC)
C     DIMENSION UREF(MXMBC),VSPV(MXEBC),VSSV(MXNBC),VNBC(MXMBC)
C     DIMENSION GLK(MXNEQ,MXNEQ),GLM(MXNEQ,MXNEQ),GLF(MXNEQ),GU0(MXNEQ)
C
C     Impose boundary conditions for STATIC and TIME-DEPENDENT problems
C
C     IF (ITEM.LE.2) THEN

```

```

C     Include specified PRIMARY degrees of freedom
C
IF(NSPV.NE.0)THEN
  DO 30 NB = 1,NSPV
    IE=(ISPV(NB,1)-1)*NDF+ISPV(NB,2)
    IT=NHBW-1
    I=IE-NHBW
    DO 10 II=1,IT
      I=I+1
      IF(I .GE. 1)THEN
        J=IE-I+1
        GLF(I)=GLF(I)-GLK(I,J)*VSPV(NB)
        GLK(I,J)=0.0
      ENDIF
10    CONTINUE
      GLK(IE,1)=1.0
      GLF(IE)=VSPV(NB)
      I=IE
      DO 20 II=2,NHBW
        I=I+1
        IF(I .LE. NEQ)THEN
          GLF(I)=GLF(I)-GLK(IE,II)*VSPV(NB)
          GLK(IE,II)=0.0
        ENDIF
20    CONTINUE
30    CONTINUE
  ENDIF
C
IF(NSSV.NE.0)THEN
C     Include specified SECONDARY degrees of freedom
C
DO 40 NF = 1,NSSV
  NB=(ISSV(NF,1)-1)*NDF+ISSV(NF,2)
  IF(ITEM.EQ.1)GLF(NB)=GLF(NB)+VSSV(NF)*DT
40  IF(ITEM.NE.1)GLF(NB)=GLF(NB)+VSSV(NF)
  ENDIF
C
IF(NNBC.NE.0)THEN
C     Include specified MIXED boundary conditions
C
DO 50 IC=1,NNBC
  NC=(INBC(IC,1)-1)*NDF+INBC(IC,2)
  IF(ITEM.EQ.1)THEN
    GLK(NC,1)=GLK(NC,1)+ALFA*DT*VNBC(IC)
    GLF(NC)=GLF(NC)+DT*VNBC(IC)*(UREF(IC)
*           -(1.0-ALFA)*GU0(NC))
  ELSE
    GLK(NC,1)=GLK(NC,1)+VNBC(IC)
    GLF(NC)=GLF(NC)+VNBC(IC)*UREF(IC)
  ENDIF
50  CONTINUE
  ENDIF
ELSE
C     Impose boundary conditions for EIGENVALUE problems
C
IF(NNBC.NE.0)THEN
C     Include specified MIXED boundary conditions
C
DO 70 IC=1,NNBC
  NC=(INBC(IC,1)-1)*NDF+INBC(IC,2)
  GLK(NC,NC)=GLK(NC,NC)+VNBC(IC)
70  CONTINUE
  ENDIF
C
C     Include specified PRIMARY degrees of freedom
C
IF(NSPV.NE.0)THEN
  DO 80 IB=1,NSPV
    IBDY(IB)=(ISPV(IB,1)-1)*NDF+ISPV(IB,2)
    DO 120 I=1,NSPV
      IMAX=IBDY(I)
      DO 110 J=I,NSPV

```

```

        IF (IBDY(J) .GE. IMAX) THEN
          IMAX=IBDY(J)
          IKEPT=J
        ENDIF
110      CONTINUE
        IBDY(IKEPT)=IBDY(I)
        IBDY(I)=IMAX
120      CONTINUE
        NEQR = NEQ
        DO 180 I=1,NSPV
          IB=IBDY(I)
          IF (IB .LT. NEQR) THEN
            NEQR1=NEQR-1
            DO 160 II=IB,NEQR1
            DO 140 JJ=1,NEQR
              GLM(II,JJ)=GLM(II+1,JJ)
              GLK(II,JJ)=GLK(II+1,JJ)
              DO 150 JJ=1,NEQR
                GLM(JJ,II)=GLM(JJ,II+1)
                GLK(JJ,II)=GLK(JJ,II+1)
140            CONTINUE
150          CONTINUE
160        ENDIF
        NEQR=NEQR-1
180      CONTINUE
        ENDIF
      RETURN
    END

```

```

SUBROUTINE COEFFCNT (IELEM, ITEM, MODEL, NDF, NPE, TIME, NTYPE,
*                      NE, F3, MXELM)

```

```

C
C
C The subroutine is called in MAIN to compute coefficient matrices
C and source vector for the model problem in Eq. (1) (see MAIN)
C
C      X..... Global (i.e., problem) coordinate
C      XI..... Local (i.e., element) coordinate
C      H..... Element length
C      {SF}.... Element interpolation (or shape) functions
C      {GDSF}... First derivative of SF w.r.t. X
C      {GDDSF}... Second derivative of SF w.r.t. X
C      GJ..... Determinant of the Jacobian matrix [J]
C      [GAUSPT].. 4x4 matrix of Gauss points: N-th column corresponds
C                  to the N-point Gauss rule
C      [GAUSWT].. 4x4 matrix of Gauss weights (see the comment above)
C      [A], [B]... Element matrices needed to compute ELK
C      [ELK]..... Element coefficient matrix [K]
C      [ELM]..... Element 'mass' matrix [M]
C
C
IMPLICIT REAL*8 (A-H,O-Z)
COMMON/STF1/ELK(9,9),ELM(9,9),ELF(9),ELX(4),ELU(9),ELV(9),ELA(9)
COMMON/STF2/A1,A2,A3,A4,A5,AX0,AX1,BX0,BX1,CX0,CX1,CT0,CT1,FX0,
*           FX1,FX2
COMMON/SHP/SF(4),GDSF(4),GDDSF(4),GJ
DIMENSION GAUSPT(5,5),GAUSWT(5,5),F3(MXELM)
C
DATA GAUSPT/5*0.0D0,-.57735027D0,.57735027D0,3*0.0D0,-.77459667D0,
* 0.0D0,.77459667D0,2*0.0D0,-.86113631D0,-.33998104D0,.33998104D0,
*.86113631D0,0.0D0,-.906180D0,-.538469D0,0.0D0,.538469D0,.906180D0/
C
DATA GAUSWT/2.0D0,4*0.0D0,2*1.0D0,3*0.0D0,.55555555D0,.88888888D0,
* 0.55555555D0,2*0.0D0,.34785485D0,2*.65214515D0,.34785485D0,0.0D0,
* 0.236927D0,.478629D0,.568889D0,.478629D0,.236927D0/
C
NN=NDF*NPE
H = ELX(NPE) - ELX(1)
IF (IELEM .EQ. 0) THEN
  NGP=4
ELSE
  NGP = IELEM+1
ENDIF
C
DO 10 J=1,NN

```

```

IF (ITEM.LE.2) THEN
  ELF(J) = 0.0
ENDIF
DO 10 I=1,NN
  IF (ITEM.GT.0) THEN
    ELM(I,J)=0.0
  ENDIF
10 ELK(I,J)=0.0
C
C   IF (MODEL.NE.2) THEN
C
C     DO-LOOP on number of Gauss points begins here
C
C       DO 100 NI=1,NGP
C         XI = GAUSPT(NI,NGP)
C
C       Call subroutine SHAPE1D to evaluate the interpolation functions
C         and their global derivatives at the Gauss point XI
C
C       CALL SHAPE1D(H,IELEM,NPE,XI)
C       CONST = GJ*GAUSWT(NI,NGP)
C       IF (IELEM.EQ.0) THEN
C         X = ELX(1) + 0.5*H*(1.0+XI)
C       ELSE
C         X = 0.0
C         DO 30 J=1,NPE
C           X = X + SF(J)*ELX(J)
C 30      ENDF
C
C       Compute coefficient matrices and vectors for various model problems
C         governed by single second-order and fourth-order equations
C         (MODEL = 1 or 3; NTYPE = 0 or 1)
C
C       CX=CX0+CX1*X
C       IF (ITEM.NE.3) THEN
C         FX=FX0+FX1*X+FX2*X*X
C       ENDIF
C       IF (ITEM.GT.0) THEN
C         CT=CT0+CT1*X
C       ENDIF
C       IF (MODEL.EQ.1) THEN
C
C         Coefficients for ALL SINGLE-VARIABLE PROBLEMS (MODEL=1)
C
C         IF (NTYPE.EQ.0) THEN
C
C           All problems governed by MODEL EQUATION (3.1) (NTYPE=0)
C
C             AX=AX0+AX1*X
C             DO 50 J = 1,NN
C               IF (ITEM.LE.2) THEN
C                 ELF(J) = ELF(J) + CONST*SF(J)*FX
C               ENDIF
C               DO 50 I = 1,NN
C                 IF (ITEM.NE.0) THEN
C                   ELM(I,J) = ELM(I,J) + CONST*SF(I)*SF(J)*CT
C                 ENDIF
C                 AIJ = CONST*GDSF(I)*GDSF(J)
C                 CIJ = CONST*SF(I)*SF(J)
C 50                ELK(I,J)=ELK(I,J) + AX*AIJ + CX*CIJ
C             ELSE
C
C               RADIALLY SYMMETRIC ELASTICITY problems (MODEL=1, NTYPE>0)
C               AX0=E1, AX1=E2, BX0=NU12, BX1=H, thickness
C
C                 ANU21=BX0*AX0/AX1
C                 IF (NTYPE.EQ.1) THEN
C                   C11=BX1*AX0/(1.0-BX0*ANU21)
C                   C22=C11*(AX1/AX0)
C                   C12=BX0*C22
C                 ELSE
C                   DENOM=1.0-BX0-ANU21
C                   C11=BX1*AX0*(1.0-BX0)/(1.0+BX0)/DENOM
C                   C22=BX1*AX1*(1.0-ANU21)/(1.0+ANU21)/DENOM
C                   C12=BX0*C22
C                 ENDIF

```

```

DO 60 J=1,NN
IF(ITEM.LE.2) THEN
  ELF(J) = ELF(J) + CONST*SF(J)*FX*X
ENDIF
DO 60 I=1,NN
IF(ITEM.NE.0) THEN
  ELM(I,J) = ELM(I,J) + CONST*SF(I)*SF(J)*CT*X
ENDIF
AIJ = CONST*GDSF(I)*GDSF(J)*C11*X
CIJ = CONST*SF(I)*SF(J)*CX*X
DIJ = CONST*(GDSF(I)*SF(J)+SF(I)*GDSF(J))*C12
EIJ = CONST*SF(I)*SF(J)*C22/X
60   ELK(I,J)=ELK(I,J) + AIJ + CIJ + DIJ + EIJ
ENDIF
ELSE
C
C      Coefficients for the EULER-BERNOULLI theory (MODEL=2)
C
IF(NTYPE.EQ.0) THEN
C      The Euler-Bernoulli BEAM element (MODEL=1 and NTYPE=0)
C
BX=BX0+BX1*X
CX=CX0+CX1*X
DO 70 J = 1,NN
IF(ITEM.LE.2) THEN
  ELF(J) = ELF(J) + CONST*SF(J)*FX
ENDIF
DO 70 I = 1,NN
IF(ITEM.GT.0) THEN
  IF(ITEM.LE.3) THEN
    ELM(I,J) = ELM(I,J) + CONST*SF(I)*SF(J)*CT
  ELSE
    ELM(I,J) = ELM(I,J) + CONST*GDSF(I)*GDSF(J)
  ENDIF
ENDIF
BIJ = CONST*GDDSF(I)*GDDSF(J)
CIJ = CONST*SF(I)*SF(J)
70   ELK(I,J)=ELK(I,J) + BX*BIJ + CX*CIJ
ELSE
C
C      The E-B CIRCULAR PLATE element (MODEL=1 and NTYPE>0)
C
ANU21=BX0*AX0/AX1
DI=(BX1**3)/12.0
D11=DI*AX0/(1.0-BX0*ANU21)
D22=D11*(AX1/AX0)
D12=BX0*D22
DO 80 J=1,NN
IF(ITEM.LE.2) THEN
  ELF(J) = ELF(J) + CONST*SF(J)*FX*X
ENDIF
DO 80 I=1,NN
BIJ = CONST*GDDSF(I)*GDDSF(J)*D11*X
CIJ = CONST*SF(I)*SF(J)*CX*X
DIJ = CONST*(GDDSF(I)*GDSF(J)+GDSF(I)*GDDSF(J))*D12
EIJ = CONST*GDSF(I)*GDSF(J)*D22/X
80   ELK(I,J)=ELK(I,J) + BIJ + CIJ + DIJ + EIJ
ENDIF
ENDIF
100  CONTINUE
ELSE
C
C      Coefficients for the TIMOSHENKO beam and circular plate (MODEL=2)
C      Full integration for bending coefficients
C
DO 160 NI=1,NGP
XI=GAUSPT(NI,NGP)
CALL SHAPE1D(H,IELEM,NPE,XI)
CONST=GJ*GAUSWT(NI,NGP)
X = 0.0
DO 110 J=1,NPE
X = X + SF(J)*ELX(J)
110  IF(NTYPE.EQ.0 .OR. NTYPE.EQ.2) THEN
C
C      The Timoshenko BEAM element (MODEL=2 and NTYPE=0 OR 2)

```

```

C
BX=BX0+BX1*X
CX=CX0+CX1*X
FX=FX0+FX1*X+FX2*X*X
JJ=1
DO 130 J=1,NPE
IF(ITEM.LE.2)THEN
  ELF(JJ)=ELF(JJ)+FX*SF(J)*CONST
ENDIF
II=1
DO 120 I=1,NPE
CIJ=SF(I)*SF(J)*CONST
BIJ=GDSF(I)*GDSF(J)*CONST
ELK(II,JJ)=ELK(II,JJ)+CX*CIJ
ELK(II+1,JJ+1)=ELK(II+1,JJ+1)+BX*BIJ
IF(ITEM.NE.0)THEN
  ELM(II,JJ)=ELM(II,JJ)+CT0*CIJ
  ELM(II+1,JJ+1)=ELM(II+1,JJ+1)+CT1*CIJ
ENDIF
120   II=NDF*I+1
130   JJ=NDF*J+1
ELSE
C      Timoshenko CIRCULAR PLATE element (MODEL=2 and NTYPE=1 or 3)
C      AX0=E1, AX1=E2, BX0=ANU12, BX1=H
C
ANU21=BX0*AX0/AX1
CX=CX0+CX1*X
FX=FX0+FX1*X
DI=(BX1**3)/12.0
D11=DI*AX0/(1.0-BX0*ANU21)
D22=D11*(AX1/AX0)
D12=BX0*D22
JJ=1
DO 150 J=1,NPE
IF(ITEM.LE.2)THEN
  ELF(JJ)=ELF(JJ)+FX*SF(J)*CONST*X
ENDIF
II=1
DO 140 I=1,NPE
BIJ = CONST*GDSF(I)*GDSF(J)*D11*X
CIJ = CONST*SF(I)*SF(J)*X
DIJ = CONST*(GDSF(I)*SF(J)+SF(I)*GDSF(J))*D12
EIJ = CONST*SF(I)*SF(J)*D22/X
ELK(II,JJ)=ELK(II,JJ)+CX*CIJ
ELK(II+1,JJ+1)=ELK(II+1,JJ+1)+BIJ+DIJ+EIJ
IF(ITEM.NE.0)THEN
  ELM(II,JJ)=ELM(II,JJ)+CT0*CIJ
  ELM(II+1,JJ+1)=ELM(II+1,JJ+1)+CT1*CIJ
ENDIF
140   II=NDF*I+1
150   JJ=NDF*J+1
ENDIF
160   CONTINUE
C      Reduced integration is used to evaluate the transverse shear terms
C
LGP=NGP-1
DO 230 NI=1,LGP
XI=GAUSPT(NI,LGP)
C
CALL SHAPE1D(H,IELEM,NPE,XI)
CONST=GJ*GAUSWT(NI,LGP)
C
X = 0.0
DO 170 J=1,NPE
X = X + SF(J)*ELX(J)
IF(NTYPE.EQ.0 .OR. NTYPE.EQ.2)THEN
C      The Timoshenko BEAM element (MODEL=2 and NTYPE=0 or 2)
C      AX = GAK = AX0 + AX1*X (reduced integration)
C
AX=AX0+AX1*X
JJ=1
DO 190 J=1,NPE
II=1

```

```

DO 180 I=1,NPE
B11=GDSF(I)*GDSF(J)*CONST
B01=SF(I)*GDSF(J)*CONST
B10=GDSF(I)*SF(J)*CONST
B00=SF(I)*SF(J)*CONST
ELK(II,JJ) =ELK(II,JJ) +AX*B11
ELK(II,JJ+1) =ELK(II,JJ+1) +AX*B10
ELK(II+1,JJ) =ELK(II+1,JJ) +AX*B01
ELK(II+1,JJ+1)=ELK(II+1,JJ+1)+AX*B00
180   II=I*NDF+1
190   JJ=J*NDF+1
      ELSE
C
C      Timoshenko CIRCULAR PLATE element (MODEL=2 and NTYPE=1 or 3)
C          BX1=H, FX2=G13*K (reduced integration)
C
A33=BX1*FX2
JJ=1
DO 210 J=1,NPE
II=1
DO 200 I=1,NPE
BIJ = CONST*GDSF(I)*GDSF(J)*X
CIJ = CONST*SF(I)*SF(J)*X
DIJ = CONST*GDSF(I)*SF(J)*X
DJI = CONST*SF(I)*GDSF(J)*X
ELK(II,JJ) =ELK(II,JJ) + A33*BIJ
ELK(II,JJ+1) =ELK(II,JJ+1) + A33*DIJ
ELK(II+1,JJ) =ELK(II+1,JJ) + A33*DJI
ELK(II+1,JJ+1)=ELK(II+1,JJ+1) + A33*CIJ
200   II=NDF*I+1
210   JJ=NDF*J+1
      ENDIF
230   CONTINUE
      IF(ITEM.EQ.0 .AND. NTYPE.GT.1) THEN
          CALL TIMFORCE(ELF,ELX,FX0,FX1,FX2,H,NTYPE,NE,F3,MXELM)
      ENDIF
      ENDIF
C
      IF(ITEM.GT.2)RETURN
      IF(ITEM.EQ.1 .OR. ITEM.EQ.2)THEN
C
C      Equivalent coefficient matrices for TIME-DEPENDENT problems
C
      IF(ITEM .EQ. 1)THEN
C
C      Alfa-family of time approximation for PARABOLIC equations
C
          DO 250 J=1,NN
          SUM=0.0
          DO 240 I=1,NN
          SUM=SUM+(ELM(I,J)-A2*ELK(I,J))*ELU(I)
240          ELK(I,J)=ELM(I,J)+A1*ELK(I,J)
250          ELF(J)=(A1+A2)*ELF(J)+SUM
          ELSE
C
C      Newmark-family of approximation for HYPERBOLIC equations
C
          IF(TIME.EQ.0.0)THEN
              DO 260 J=1,NN
              DO 260 I=1,NN
              ELF(J)=ELF(J)-ELK(I,J)*ELU(I)
260              ELK(I,J)=ELM(I,J)
          ELSE
              DO 270 J=1,NN
              DO 270 I=1,NN
              ELF(J)=ELF(J)+ELM(I,J)*(A3*ELU(I)+A4*ELV(I)+A5*ELA(I))
270              ELK(I,J)=ELK(I,J)+A3*ELM(I,J)
          ENDIF
          ENDIF
          RETURN
      END

```

SUBROUTINE CONSTRNT(NEQ,NHBW,NDF,NCON,ICON,VCON,GLK,GLM,GLF,
* TRM,MXNEQ)

```

C
C The subroutine is called in MAIN to implement specified constraint
C conditions (e.g., inclined supports) on the condensed system of
C equations. Array GLM is used here as a temporary storage array.
C
IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION ICON(9),VCON(9),GLK(MXNEQ,MXNEQ),GLF(MXNEQ),
* GLM(MXNEQ,MXNEQ),TRM(MXNEQ,MXNEQ)
C
PI=3.14159265D0
C
Include specified constraint conditions
C
DO 20 IC=1,NEQ
  DO 10 JC=1,NEQ
    GLM(IC,JC)=0.0
10   TRM(IC,JC)=0.0
20   TRM(IC,IC)=1.0D0
  DO 30 IC=1,NCON
    BETA=VCON(IC)*PI/180.0D0
    IDOF=NDF*ICON(IC)-1
    TRM(IDOF, IDOF) = DCOS(BETA)
    TRM(IDOF, IDOF+1) = DSIN(BETA)
    TRM(IDOF+1, IDOF) = -DSIN(BETA)
30   TRM(IDOF+1, IDOF+1) = DCOS(BETA)
C
L=0
DO 50 I=1,NEQ
DO 40 J=1,NHBW
40 GLM(I,L+J)=GLK(I,J)
50 L=L+1
  DO 60 I=1,NEQ
    DO 60 J=I,NEQ
60 GLM(J,I)=GLM(I,J)
  DO 70 I=1,NEQ
    DO 70 J=1,NEQ
70 GLK(I,J)=GLM(I,J)
C
  DO 80 I=1,NEQ
    DO 80 J=1,NEQ
      GLM(I,J)=0.0
    DO 80 K=1,NEQ
80 GLM(I,J)=GLM(I,J)+TRM(I,K)*GLK(K,J)
C
  DO 90 I=1,NEQ
    DO 90 J=1,NEQ
      GLK(I,J)=0.0
    DO 90 K=1,NEQ
90 GLK(I,J)=GLK(I,J)+GLM(I,K)*TRM(J,K)
C
  DO 100 I=1,NEQ
    DO 100 J=1,NEQ
100 TRM(I,J)=GLK(I,J)
L=0
  DO 120 I=1,NEQ
    DO 110 J=1,NHBW
110 GLK(I,J)=TRM(I,L+J)
120 L=L+1
C
  DO 150 I=1,NEQ
    GLM(I,1)=0.0
    DO 140 K=1,NEQ
140 GLM(I,1)=GLM(I,1)+TRM(I,K)*GLF(K)
150 GLF(I)=GLM(I,1)
C
      RETURN
      END

SUBROUTINE ECHODATA(IN,IT)
IMPLICIT REAL*8 (A-H,O-Z)
C
DIMENSION AA(20)
WRITE(IT,40)

```

```

10 CONTINUE
  READ (IN,30,END=20) AA
  WRITE (IT,60) AA
  GO TO 10
20 CONTINUE
  REWIND (IN)
  WRITE (IT,50)
  RETURN
30 FORMAT (20A4)
40 FORMAT (5X,'*** ECHO OF THE INPUT DATA STARTS ***',/)
50 FORMAT (5X,'*** ECHO OF THE INPUT DATA ENDS ***',/)
60 FORMAT (1X,20A4)
END

SUBROUTINE EGNSOLVR (N,A,B,XX,X,NEGN,NR,MXNEQ)

C
C
C   The subroutine is called in MAIN to solve the EIGENVALUE PROBLEM
C
C           [A] {X} = Lambda. [B] {X}
C
C   The program can be used only for positive-definite [B] matrix.
C   The dimensions of V, VT, W, and IH should be equal to MXNEQ.

IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION A(MXNEQ,MXNEQ), B(MXNEQ,MXNEQ), XX(MXNEQ), X(MXNEQ,MXNEQ)
DIMENSION V(500,500), VT(500,500), W(500,500), IH(500)
C
C   Call subroutine JACOBI to diagonalize [B]
C
CALL JACOBI (N,B,NEGN,NR,V,XX,IH,MXNEQ)
C
C   Make diagonalized [B] symmetric
C
DO 10 I=1,N
  DO 10 J=1,N
10 B(J,I)=B(I,J)
C
C   Check (to make sure) that [B] is positive-definite
C
DO 30 I=1,N
  IF (B(I,I))20,30,30
20 WRITE(6,80)
  STOP
30 CONTINUE
C
C   The eigenvectors of [B] are stored in array V(I,J)
C   Form the transpose of [V] as [VT]
C
DO 40 I=1,N
  DO 40 J=1,N
40 VT(I,J)=V(J,I)
C
C   Find the product [F]=[VT] [A] [V] and store in [A] to save storage
C
CALL MATRXMLT (MXNEQ,N,VT,A,W)
CALL MATRXMLT (MXNEQ,N,W,V,A)
C
C   Get [GI] from diagonalized [B], but store it in [B]
C
DO 50 I=1,N
50 B(I,I)=1.0/DSQRT(B(I,I))
C
C   Find the product [Q]=[GI] [F] [GI]=[B] [A] [B] and store in [A]
C
CALL MATRXMLT (MXNEQ,N,B,A,W)
CALL MATRXMLT (MXNEQ,N,W,B,A)
C
C   We now have the form [Q] {Z}=Lamda{Z}. Diagonalize [Q] to obtain
C   the eigenvalues by calling JACOBI.
C
CALL JACOBI (N,A,NEGN,NR,VT,XX,IH,MXNEQ)
C
C   The eigenvalues are returned as diag [A].

```

```

C
      DO 60 J=1,N
60  XX(J)=A(J,J)
C
C      The eigenvectors are computed from the relation,
C          {X}=[V] [GI] {Z}=[V] [B] [VT]
C      since {Z} is stored in [VT].
C
C      CALL MATRXMLT (MXNEQ,N,V,B,W)
C      CALL MATRXMLT (MXNEQ,N,W,VT,X)
C
80 FORMAT('/*** Matrix [GLM] is NOT positive-definite ***')
      RETURN
      END

SUBROUTINE EQNSOLVR (NRM,NCM,NEQNS,NBW,BAND,RHS,IRES)
C
C
C      The subroutine is called in MAIN to solve symmetric and banded set
C      of equations using the Gauss elimination method: [BAND]{U} = {RHS}.
C      The coefficient matrix is input as BAND(NEQNS,NBW) and the column
C      vector is input as RHS(NEQNS), where NEQNS is the actual number
C      of equations and NBW is the half band width. The true dimensions
C      of the matrix [BAND] in the calling program, are NRM by NCM. When
C      IRES is greater than zero, the right hand elimination is skipped.
C
C
C      IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION BAND (NRM,NCM) ,RHS (NRM)
C
      MEQNS=NEQNS-1
      IF (IRES.LE.0) THEN
        DO 30 NPIV=1,MEQNS
        NPIVOT=NPIV+1
        LSTSUB=NPIV+NBW-1
        IF (LSTSUB.GT.NEQNS) THEN
          LSTSUB=NEQNS
        ENDIF
      C
        DO 20 NROW=NPIVOT,LSTSUB
        NCOL=NROW-NPIV+1
        FACTOR=BAND (NPIV,NCOL) /BAND (NPIV,1)
        DO 10 NCOL=NROW,LSTSUB
        ICOL=NCOL-NROW+1
        JCOL=NCOL-NPIV+1
10      BAND (NROW,ICOL)=BAND (NROW,ICOL) -FACTOR*BAND (NPIV,JCOL)
20      RHS (NROW)=RHS (NROW) -FACTOR*RHS (NPIV)
30      CONTINUE
      ELSE
40      DO 60 NPIV=1,MEQNS
        NPIVOT=NPIV+1
        LSTSUB=NPIV+NBW-1
        IF (LSTSUB.GT.NEQNS) THEN
          LSTSUB=NEQNS
        ENDIF
        DO 50 NROW=NPIVOT,LSTSUB
        NCOL=NROW-NPIV+1
        FACTOR=BAND (NPIV,NCOL) /BAND (NPIV,1)
50      RHS (NROW)=RHS (NROW) -FACTOR*RHS (NPIV)
60      CONTINUE
      ENDIF
C
C      Back substitution
C
      DO 90 IJK=2,NEQNS
      NPIV=NEQNS-IJK+2
      RHS (NPIV)=RHS (NPIV) /BAND (NPIV,1)
      LSTSUB=NPIV-NBW+1
      IF (LSTSUB.LT.1) THEN
        LSTSUB=1
      ENDIF
      NPIVOT=NPIV-1
      DO 80 JKI=LSTSUB,NPIVOT
      NROW=NPIVOT-JKI+LSTSUB

```

```

NCOL=NPIV-NROW+1
FACTOR=BAND (NROW, NCOL)
80 RHS (NROW) =RHS (NROW) -FACTOR*RHS (NPIV)
90 CONTINUE
  RHS (1)=RHS (1)/BAND (1,1)
  RETURN
END

SUBROUTINE JACOBI (N,Q,JVEC,M,V,X,IH,MXNEQ)
C
C      Called in EGNSOLVR to diagonalize [Q] by successive rotations
C
C      DESCRIPTION OF THE VARIABLES:
C
C      N      .... Order of the real, symmetric matrix [Q] (N > 2)
C      [Q]    .... The matrix to be diagonalized (destroyed)
C      JVEC   .... 0, when only eigenvalues alone have to be found
C      [V]    .... Matrix of eigenvectors
C      M      .... Number of rotations performed
C
C
IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION Q(MXNEQ,MXNEQ),V(MXNEQ,MXNEQ),X(MXNEQ),IH(MXNEQ)
EPSI=1.0D-08
C
  IF(JVEC)10,50,10
10 DO 40 I=1,N
    DO 40 J=1,N
      IF(I-J)30,20,30
20 V(I,J)=1.0
  GO TO 40
30 V(I,J)=0.0
40 CONTINUE
50 M=0
  MI=N-1
  DO 70 I=1,MI
    X(I)=0.0
    MJ=I+1
    DO 70 J=MJ,N
      IF(X(I)-DABS(Q(I,J)))60,60,70
60 X(I)=DABS(Q(I,J))
  IH(I)=J
70 CONTINUE
75 DO 100 I=1,MI
  IF(I-1)90,90,80
80 IF(XMAX-X(I))90,100,100
90 XMAX=X(I)
  IP=I
  JP=IH(I)
100 CONTINUE
  IF(XMAX-EPSI)500,500,110
110 M=M+1
  IF(Q(IP,IP)-Q(JP,JP))120,130,130
120 TANG=-2.0*Q(IP,JP)/(DABS(Q(IP,IP)-Q(JP,JP))+DSQRT((Q(IP,IP)
  1-Q(JP,JP))**2+4.0*Q(IP,JP)**2))
  GO TO 140
130 TANG= 2.0*Q(IP,JP)/(DABS(Q(IP,IP)-Q(JP,JP))+DSQRT((Q(IP,IP)
  1-Q(JP,JP))**2+4.0*Q(IP,JP)**2))
140 COSN=1.0/DSQRT(1.0+TANG**2)
  SINE=TANG*COSN
  QII=Q(IP,IP)
  Q(IP,IP)=COSN**2*(QII+TANG*(2.*Q(IP,JP)+TANG*Q(JP,JP)))
  Q(JP,JP)=COSN**2*(Q(JP,JP)-TANG*(2.*Q(IP,JP)-TANG*QII))
  Q(IP,JP)=0.0
  IF (Q(IP,IP)-Q(JP,JP)) 150,190,190
150 TEMP=Q(IP,IP)
  Q(IP,IP)=Q(JP,JP)
  Q(JP,JP)=TEMP
  IF(SINE) 160,170,170
160 TEMP=COSN
  GOTO 180
170 TEMP=-COSN
180 COSN=DABS(SINE)

```

```

SINE=TEMP
190 DO 260 I=1,MI
   IF (I-IP) 210,260,200
200 IF (I-JP) 210,260,210
210 IF (IH(I)-IP) 220,230,220
220 IF (IH(I)-JP) 260,230,260
230 K=IH(I)
   TEMP=Q(I,K)
   Q(I,K)=0.0
   MJ=I+1
   X(I)=0.0
   DO 250 J=MJ,N
      IF (X(I)-DABS(Q(I,J))) 240,240,250
240 X(I)=DABS(Q(I,J))
   IH(I)=J
250 CONTINUE
   Q(I,K)=TEMP
260 CONTINUE
   X(IP)=0.0
   X(JP)=0.0
   DO 430 I=1,N
      IF (I-IP) 270,430,320
270 TEMP=Q(I,IP)
   Q(I,IP)=COSN*TEMP+SINE*Q(I,JP)
   IF (X(I)-DABS(Q(I,IP))) 280,290,290
280 X(I)=DABS(Q(I,IP))
   IH(I)=IP
290 Q(I,JP)=-SINE*TEMP+COSN*Q(I,JP)
   IF (X(I)-DABS(Q(I,JP))) 300,430,430
300 X(I)=DABS(Q(I,JP))
   IH(I)=JP
   GO TO 430
320 IF (I-JP) 330,430,380
330 TEMP=Q(IP,I)
   Q(IP,I)=COSN*TEMP+SINE*Q(I,JP)
   IF (X(IP)-DABS(Q(IP,I))) 340,350,350
340 X(IP)=DABS(Q(IP,I))
   IH(IP)=I
350 Q(I,JP)=-SINE*TEMP+COSN*Q(I,JP)
   IF (X(I)-DABS(Q(I,JP))) 300,430,430
380 TEMP=Q(IP,I)
   Q(IP,I)=COSN*TEMP+SINE*Q(JP,I)
   IF (X(IP)-DABS(Q(IP,I))) 390,400,400
390 X(IP)=DABS(Q(IP,I))
   IH(IP)=I
400 Q(JP,I)=-SINE*TEMP+COSN*Q(JP,I)
   IF (X(JP)-DABS(Q(JP,I))) 410,430,430
410 X(JP)=DABS(Q(JP,I))
   IH(JP)=I
430 CONTINUE
   IF (JVEC) 440,75,440
440 DO 450 I=1,N
   TEMP=V(I,IP)
   V(I,IP)=COSN*TEMP+SINE*V(I,JP)
450 V(I,JP)=-SINE*TEMP+COSN*V(I,JP)
   GOTO 75
500 RETURN
END

```

SUBROUTINE MATRXMLT(MXNEQ,N,A,B,C)

```

C
C
C     Called in EGNSOLVR to compute the product of matrices [A] & [B] :
C           [C] = [A] [B]
C
IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION A(MXNEQ,MXNEQ), B(MXNEQ,MXNEQ), C(MXNEQ,MXNEQ)
DO 10 I=1,N
DO 10 J=1,N
C(I,J)=0.0
DO 10 K=1,N
10 C(I,J)=C(I,J)+A(I,K)*B(K,J)
RETURN
END

```

```

C SUBROUTINE MESH1D(NEM,NPE,NOD,MXELM,MXNOD,DX,GLX)
C
C The subroutine is called in MAIN to compute arrays {GLX} and [NOD]
C
C {GLX}..... Vector of global coordinates
C {DX}..... Vector of element lengths [DX(1) = node 1 coord.]
C [NOD].... Connectivity matrix
C
C IMPLICIT REAL*8 (A-H,O-Z)
C DIMENSION GLX(MXNOD),DX(MXNOD),NOD(MXELM,4)
C
C Generate the elements of the connectivity matrix
C
DO 10 I=1,NPE
10 NOD(1,I)=I
DO 20 N=2,NEM
DO 20 I=1,NPE
20 NOD(N,I) = NOD(N-1,I)+NPE-1
C
C Generate global coordinates of the global nodes
C
GLX(1)=DX(1)
IF(NPE.EQ.2)THEN
  DO 30 I=1,NEM
30   GLX(I+1) = GLX(I) + DX(I+1)
ELSE
  DO 40 I=1,NEM
    II=2*I
    GLX(II) = GLX(II-1) + 0.5*DX(I+1)
40   GLX(II+1)=GLX(II-1) + DX(I+1)
ENDIF
RETURN
END

SUBROUTINE POSTPROC(DCAX,DCBX,DCCX,F3,GLF,GLX,NOD,ICONT,IELEM,NPE,
*                      MODEL,NTYPE,ITEM,MXELM,MXNEQ,MXNOD,NEM,NDF)
C
C The subroutine is called in MAIN to compute the solution and its
C derivatives at five points, including the nodes of the element.
C The bending moment (BM) and shear force (VF) are computed as per
C the definitions given in Fig. 5.2.1 and Eq. (5.3.1) of the book.
C
C X..... Global (i.e., problem) coordinate
C XI..... Local (i.e., element) coordinate
C SF..... Element interpolation (or shape) functions
C GDSF.... First derivative of SF w.r.t. global coordinate
C GDDSF.... Second derivative of SF w.r.t. global coordinate
C ELU..... Element solution vector
C U..... Interpolated solution
C DU..... Interpolated derivative of the solution
C W..... Interpolated transverse deflection
C S..... Interpolated rotation function
C DS..... Interpolated derivative of the rotation
C DW..... Interpolated derivative of the transverse deflection
C DDW.... Interpolated second derivative of trans. deflection
C DDDW.... Interpolated third derivative of trans. deflection
C
C IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION DCAX(MXELM,2),DCBX(MXELM,2),DCCX(MXELM,2)
DIMENSION F3(MXELM),GLF(MXNEQ),GLX(MXNOD),NOD(MXELM,4)
DIMENSION XP(9),ELX(4),ELU(9)
COMMON/IO/IN,IT
COMMON/SHP/SF(4),GDSF(4),GDDSF(4),GJ
COMMON/STF2/A1,A2,A3,A4,A5,AX0,AX1,BX0,BX1,CX0,CX1,CT0,CT1,FX0,
*          FX1,FX2
DATA XP/-1.0D0, -0.750D0, -0.50D0, -0.250D0, 0.0D0, 0.250D0,
*          0.50D0, 0.750D0, 1.0D0/

```

```

NPTS=9
DO 80 NE = 1, NEM
  IF (ICONT.NE.1) THEN
    AX0=DCAX(NE,1)
    AX1=DCAX(NE,2)
    BX0=DCBX(NE,1)
    BX1=DCBX(NE,2)
    CX0=DCCX(NE,1)
    CX1=DCCX(NE,2)
  ENDIF
  L=0
  DO 10 I=1,NPE
    NI=NOD(NE,I)
    IF (ICONT.NE.1) THEN
      ELX(1)=0.0
      ELX(2)=0.5*GLX(NE)
      ELX(NPE)=GLX(NE)
    ELSE
      ELX(I)=GLX(NI)
    ENDIF
    LI=(NI-1)*NDF
    DO 10 J=1,NDF
      LI=LI+1
      L=L+1
    10 ELU(L)=GLF(LI)
    H = ELX(NPE) - ELX(1)
  C
    DO 70 NI=1,NPTS
      XI = XP(NI)
      CALL SHAPE1D(H,IELEM,NPE,XI)
      IF (MODEL.EQ.3) THEN
        W=0.0
        DW=0.0
        DDW=0.0
        XC=ELX(1)+0.5*H*(1.0+XI)
        DO 20 I=1,4
          W = W + SF(I)*ELU(I)
          DW = DW + GDSF(I)*ELU(I)
          DDW=DDW+ GDDSF(I)*ELU(I)
        20 DDDW= ((ELU(1)-ELU(3))*2.0/H- (ELU(4)+ELU(2)))*6.0/(H*H)
        THETA=-DW
        IF (NTYPE.EQ.0) THEN
          BM=-(BX0+XC*BX1)*DDW
          VF=-(BX0+XC*BX1)*DDDW - BX1*DDW
          WRITE(IT,90) XC,W,THETA,BM,VF
        ELSE
          ANU21=BX0*AX0/AX1
          DI=(BX1**3)/12.0
          D11=DI*AX0/(1.0-BX0*ANU21)
          D22=D11*(AX1/AX0)
          D12=BX0*D22
          BMR=-(D11*DDW*XC+D12*Dw)
          BMT=-(D12*DDW*XC+D22*Dw)
          IF (XC.NE.0.0) THEN
            SFV=-D11*(XC*DDDW+DDW)+D22*Dw/XC
            WRITE(IT,90) XC,W,THETA,BMR,BMT,SFV
          ELSE
            WRITE(IT,90) XC,W,THETA,BMR,BMT
         ENDIF
        ENDIF
      ELSE
        XC=0.0
        DO 30 I=1,NPE
          XC=XC+SF(I)*ELX(I)
        IF (MODEL.EQ.1) THEN
          U=0.0
          DU=0.0
          DO 40 I=1,NPE
            U=U+SF(I)*ELU(I)
            DU=DU+GDSF(I)*ELU(I)
          40 IF (NTYPE.EQ.0) THEN
            SV=(AX0+AX1*XC)*DU
            WRITE(IT,90) XC,U,SV
          ELSE
            ANU21=BX0*AX0/AX1
            IF (NTYPE.EQ.1) THEN

```

```

C11=BX1*AX0/(1.0-BX0*ANU21)
C22=C11*(AX1/AX0)
C12=BX0*C22
ELSE
  DENOM=1.0-BX0-ANU21
  C11=BX1*AX0*(1.0-BX0)/(1.0+BX0)/DENOM
  C22=BX1*AX1*(1.0-ANU21)/(1.0+ANU21)/DENOM
  C12=BX0*C22
ENDIF
IF(XC.NE.0.0)THEN
  SR=C11*DU+C12*U/XC
  ST=C12*DU+C22*U/XC
  WRITE(IT,90)XC,U,SR,ST
ELSE
  WRITE(IT,90)XC,U,DU
ENDIF
ENDIF
ELSE
C
C MODEL.EQ.2 Calculations
C
IF(ITEM.EQ.0 .AND. NTYPE.GT.1)THEN
  H=ELX(NPE)-ELX(1)
  CALL TIMSTRES(AX0,ELU,XI,W,DW,PSI,DPSI,NE,F3,H,MXELM)
ELSE
  W=0.0
  DW=0.0
  PSI = 0.0
  DPSI=0.0
  DO 50 I=1,NPE
    L=2*I-1
    W = W + SF(I)*ELU(L)
    DW=DW+GDSF(I)*ELU(L)
    PSI = PSI + SF(I)*ELU(L+1)
    DPSI=DPSI+GDSF(I)*ELU(L+1)
  ENDIF
  IF(NTYPE.EQ.0 .OR. NTYPE.EQ.2)THEN
    BM=(BX0+BX1*XC)*DPSI
    VF=(AX0+AX1*XC)*(DW+PSI)
    WRITE(IT,90)XC,W,PSI,BM,VF
  ELSE
    ANU21=BX0*AX0/AX1
    DI=(BX1**3)/12.0
    D11=DI*AX0/(1.0-BX0*ANU21)
    D22=D11*(AX1/AX0)
    D12=BX0*D22
    BMR=(D11*DPSI*XC+D12*PSI)
    BMT=(D12*DPSI*XC+D22*PSI)
    SFV=FX2*(DW+PSI)*XC
    WRITE(IT,90)XC,W,PSI,BMR,BMT,SFV
  ENDIF
ENDIF
ENDIF
70 CONTINUE
80 CONTINUE
RETURN
90 FORMAT(2X,6E13.5)
END

```

```

SUBROUTINE REACTION(MXELM,MXNEQ,NDF,NEM,NOD,NPE,NTYPE,PR,GLF,
*                      SE,SL,SA,SI,CS,SN,CNT,SNT,HF,VF,PF,XB)

```

C
C
C The subroutine is called in MAIN to compute generalized reaction
C forces in each element of truss (NDF=2) or frame (NDF=3) structure
C
C

```

IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION PR(MXELM),SE(MXELM),SL(MXELM),SA(MXELM),SI(MXELM)
DIMENSION CS(MXELM),SN(MXELM),CNT(MXELM),SNT(MXELM)
DIMENSION HF(MXELM),VF(MXELM),PF(MXELM),XB(MXELM)
DIMENSION NOD(MXELM,4),GLF(MXNEQ),ELR(6)
COMMON/STF1/ELK(9,9),ELM(9,9),ELF(9),ELX(4),ELU(9),ELV(9),ELA(9)

```

```

C
NN=NPE*NDF

```

```

DO 140 N=1,NEM
CN1=CS(N)
SN1=SN(N)
C
C      Call TRANSFRM to compute element stiffness matrix and force vector
C
L=0
DO 100 I=1,NPE
NI=NOD(N,I)
LI=(NI-1)*NDF
DO 100 J=1,NDF
LI=LI+1
L=L+1
100 ELU(L)=GLF(LI)
      CALL TRANSFRM(MXELM,N,NTYPE,PR,SE,SL,SA,SI,CS,SN,
*                  CNT,SNT,HF,VF,PF,XB)
C
C      Compute the FORCE and MOMENT RESULTANTS
C
DO 120 I=1,NN
ELR(I) = 0.0
DO 110 J=1,NN
110 ELR(I) = ELR(I) + ELK(I,J)*ELU(J)
120 ELR(I) = ELR(I) - ELF(I)
ELF(1) = ELR(1)*CN1+ELR(2)*SN1
ELF(2) = -ELR(1)*SN1+ELR(2)*CN1
IF (NTYPE.NE.0) THEN
  ELF(3) = ELR(3)
  ELF(4) = ELR(4)*CN1+ELR(5)*SN1
  ELF(5) = -ELR(4)*SN1+ELR(5)*CN1
  ELF(6) = ELR(6)
ELSE
  ELF(3) = ELR(3)*CN1+ELR(4)*SN1
  ELF(4) = -ELR(3)*SN1+ELR(4)*CN1
ENDIF
WRITE(6,150)N, (ELF(I),I=1,NN)
WRITE(6,160) (ELR(I),I=1,NN)
140 CONTINUE
RETURN
150 FORMAT (3X,I2,6E12.4)
160 FORMAT (5X,6E12.4,/)
END

```

SUBROUTINE SHAPE1D(H,IELEM,NPE,XI)

```

C
C      Called in MAIN to compute shape functions and their derivatives
C      for Hermite cubic and Lagrange linear, quadratic and cubic elements
C
C      X..... Global (i.e., problem) coordinate
C      XI..... Local (i.e., element) coordinate
C      H..... Element length
C      {SF}.... Interpolation (or shape) functions
C      {DSF}.... First derivative of SF w.r.t. XI
C      {DDSF}.... Second derivative of SFH w.r.t. XI
C      {GDSF}.... First derivative of SF w.r.t. X
C      {GDDSF}... Second derivative of SFH w.r.t. X
C      GJ..... Jacobian of the transformation
C
C
IMPLICIT REAL*8 (A-H,O-Z)
COMMON/SHP/SF(4),GDSF(4),GDDSF(4),GJ
DIMENSION DSF(4),DDSF(4)
IF (IELEM.EQ.0) THEN
C
C      HERMITE interpolation functions (for the Euler-Bernoulli theory)
C
NET=4
SF(1) = 0.25*(2.0-3.0*XI+XI**3)
SF(2) = -H*(1.0-XI)*(1.0-XI*XI)/8.0
SF(3) = 0.25*(2.0+3.0*XI-XI**3)
SF(4) = H*(1.0+XI)*(1.0-XI*XI)/8.0
DSF(1) = -0.75*(1.0-XI*XI)
DSF(2) = H*(1.0+2.0*XI-3.0*XI*XI)/8.0
DSF(3) = 0.75*(1.0-XI*XI)

```

```

DSF(4) = H*(1.0-2.0*XI-3.0*XI*XI)/8.0
DDSF(1)= 1.5*XI
DDSF(2)= 0.25*H*(1.0-3.0*XI)
DDSF(3)= -1.5*XI
DDSF(4)=-0.25*(1.0+3.0*XI)*H
ELSE
  NET=NPE
  IF (IELEM.EQ.1) THEN
C
C   LAGRANGE interpolation functions used for linear, quadratic and
C   cubic approximation of second-order equations
C
C   LINEAR interpolation functions
C
  SF(1) = 0.5*(1.0-XI)
  SF(2) = 0.5*(1.0+XI)
  DSF(1) = -0.5
  DSF(2) = 0.5
  DDSF(1)= 0.0
  DDSF(2)= 0.0
ELSE
  IF (IELEM.EQ.2) THEN
C
C   QUADRATIC interpolation functions
C
  SF(1) = -0.5*XI*(1.0-XI)
  SF(2) = 1.0-XI*XI
  SF(3) = 0.5*XI*(1.0+XI)
  DSF(1) = -0.5*(1.0-2.0*XI)
  DSF(2) = -2.0*XI
  DSF(3) = 0.5*(1.0+2.0*XI)
  DDSF(1)= 1.0
  DDSF(2)= -2.0
  DDSF(3)= 1.0
ELSE
C
C   CUBIC interpolation functions
C
  SF(1) = 0.0625*(1.0-XI)*(9.0*XI*XI-1.)
  SF(2) = 0.5625*(1.0-XI*XI)*(1.0-3.0*XI)
  SF(3) = 0.5625*(1.0-XI*XI)*(1.0+3.0*XI)
  SF(4) = 0.0625*(9.0*XI*XI-1.0)*(1.0+XI)
  DSF(1) = 0.0625*(1.0+18.0*XI-27.0*XI*XI)
  DSF(2) = 0.5625*(-3.0-2.0*XI+9.0*XI*XI)
  DSF(3) = 0.5625*(3.0-2.0*XI-9.0*XI*XI)
  DSF(4) = 0.0625*(18.0*XI+27.0*XI*XI-1.0)
  DDSF(1)= 0.0625*(18.0-54.0*XI)
  DDSF(2)= 0.5625*(-2.0+18.0*XI)
  DDSF(3)= 0.5625*(-2.0-18.0*XI)
  DDSF(4)= 0.0625*(18.0+54.0*XI)
ENDIF
ENDIF
ENDIF
C
C   Compute derivatives of the interpolation functions w.r.t. X
C
80 GJ = H*0.5
DO 90 I = 1,NET
  GDSF(I) = DSF(I)/GJ
90 GDDSF(I) = DDSF(I)/GJ/GJ
RETURN
END

SUBROUTINE TIMFORCE(ELF,ELX,FX0,FX1,FX2,H,NTYPE,NE,F3,MXELM)
C
C
C   Called in COEFFCNT to compute element force vector for the
C   consistent interpolation Timoshenko element (CIE)
C
IMPLICIT REAL*8 (A-H,O-Z)
COMMON/SHP/SF(4),GDSF(4),GDDSF(4),GJ
DIMENSION GAUSPT(5,5),GAUSWT(5,5),ELF(9),ELX(4),EX(3),F3(MXELM)
C
DATA GAUSPT/5*0.0D0,-.57735027D0,.57735027D0,3*0.0D0,-.77459667D0,

```

```

* 0.0D0, .77459667D0, 2*0.0D0, -.86113631D0, -.33998104D0, .33998104D0,
* .86113631D0, 0.0D0, -.906180D0, -.538469D0, 0.0D0, .538469D0, .906180D0/
C
  DATA GAUSWT/2.0D0,4*0.0D0,2*1.0D0,3*0.0D0,.55555555D0,.88888888D0,
* 0.55555555D0,2*0.0D0,.34785485D0,2*.65214515D0,.34785485D0,0.0D0,
* 0.236927D0,.478629D0,.568889D0,.478629D0,.236927D0/
C
  NPE=3
  IEL=2
  NDF=2
  NGP=IEL+1
  DO 10 I=1,6
  ELF(I)=0.0
10
C
  EX(1)=ELX(1)
  EX(2)=ELX(1)+0.5*H
  EX(3)=ELX(2)
C
  DO 50 NI=1,NGP
  XI=GAUSPT(NI,NGP)
  CALL SHAPE1D(H,IEL,NPE,XI)
  CONST=GJ*GAUSWT(NI,NGP)
  X = 0.0
  DO 20 J=1,NPE
  X = X + SF(J)*EX(J)
20
C
C Compute the polynomial variation of FX
C
  IF (NTYPE.EQ.2) THEN
    FX=FX0+(FX1+FX2*X)*X
  ELSE
    FX=(FX0+FX1*X)*X
  ENDIF
C
C Element force vector for the consistent interpolation beam element
C
25  II=1
  DO 40 I=1,NPE
  ELF(II)=ELF(II)+FX*SF(I)*CONST
40
  II=NDF*I+1
50  CONTINUE
C
C Rearrange the element coefficients
C
  F3(NE)=ELF(3)
  ELF(1)=ELF(1)+0.5*F3(NE)
  ELF(2)=-0.125*F3(NE)*H
  ELF(3)=ELF(5)+0.5*F3(NE)
  ELF(4)= 0.125*F3(NE)*H
  RETURN
END

SUBROUTINE TIMSTRES(GA,ELU,XI,W,DW,S,DS,NE,F3,H,MXELM)
C
C
C Called in POSTPROC to compute solution and its global derivatives
C at nine points (including the nodes) of the Timoshenko element
C
C      XC..... Global (i.e., problem) coordinate
C      XI ..... Local (i.e., element) coordinate
C      SFL, SFQ.. Lagrange linear and quadratic shape functions
C      DSFL,DSFQ: First derivative of SF w.r.t. global coordinate
C      ELU..... Column vector of generalized displacements
C      W, DW.... Transverse deflection and its derivative
C      S, DS.... Rotation and its derivative
C
IMPLICIT REAL*8 (A-H,O-Z)
COMMON/IO/IN,IT
DIMENSION ELU(9),SFL(2),SFQ(3),DSFL(2),DSFQ(3),F3(MXELM)
C
GJ = H*0.5
C
C Interpolation functions for the Lagrange LINEAR element
C

```

```

SFL(1) = 0.5*(1.0-XI)
SFL(2) = 0.5*(1.0+XI)
DSFL(1) = -0.5/GJ
DSFL(2) = 0.5/GJ
C
C   Interpolation functions for the Lagrange QUADRATIC element
C
SFQ(1) = -0.5*XI*(1.0-XI)
SFQ(2) = 1.0-XI*XI
SFQ(3) = 0.5*XI*(1.0+XI)
DSFQ(1) = -0.5*(1.0-2.0*XI)/GJ
DSFQ(2) = -2.0*XI/GJ
DSFQ(3) = 0.5*(1.0+2.0*XI)/GJ
C
W3=(3.0*H*F3(NE)/GA + 8.0*(ELU(1)+ELU(3))
*           + 2.0*(ELU(4)-ELU(2))*H)/16.0
W = SFQ(1)*ELU(1) + SFQ(2)*W3 + SFQ(3)*ELU(3)
DW= DSFQ(1)*ELU(1) +DSFQ(2)*W3 +DSFQ(3)*ELU(3)
S = SFL(1)*ELU(2) + SFL(2)*ELU(4)
DS= DSFL(1)*ELU(2) +DSFL(2)*ELU(4)
C
RETURN
END

SUBROUTINE TRANSFRM(MXELM,N,NTYPE,PR,SE,SL,SA,SI,CS,SN,CNT,SNT,
*                   HF,VF,PF,XB)
C
C   Called in both MAIN and REACTION to compute stiffness matrix and
C   force vector for the truss (NDF=2) and frame (NDF=3) elements
C
C   SE.....Young's modulus
C   SL.....Element length
C   SA.....Cross-sectional area
C   SI.....Moment of inertia
C   CS.....Cosine of the angle of orientation
C   SN.....Sine of the angle of orientation
C   HF.....Distributed force along the length of the element
C   VF.....Distributed force transverse to the element
C   PF.....Point force at point other than nodes
C   XB.....Distance along the length from node 1 of the element
C          of the location of the point force, PF
C   CNT,SNT:Direction cosines of the point force's line of application
C
IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION PR(MXELM),SE(MXELM),SL(MXELM),SA(MXELM),SI(MXELM)
DIMENSION CS(MXELM),SN(MXELM),CNT(MXELM),SNT(MXELM)
DIMENSION HF(MXELM),VF(MXELM),PF(MXELM),XB(MXELM)
DIMENSION TRM(6,6),TMPK(6,6)
COMMON/STF1/ELK(9,9),ELM(9,9),ELF(9),ELX(4),ELU(9),ELV(9),ELA(9)
C
CN1=CS(N)
SN1=SN(N)
CN2=CN1*CN1
SN2=SN1*SN1
CSN=CN1*SN1
C
C   Element coefficients
C
IF (NTYPE.EQ.0) THEN
C
C   The plane TRUSS element
C
NN=4
C1=SA(N)*SE(N)/SL(N)
ELK(1,1) = C1*CN2
ELK(2,1) = C1*CSN
ELK(2,2) = C1*SN2
ELK(3,1) = -ELK(1,1)
ELK(3,2) = -ELK(2,1)
ELK(3,3) = ELK(1,1)
ELK(4,1) = -ELK(2,1)
ELK(4,2) = -ELK(2,2)
ELK(4,3) = -ELK(3,2)

```

```

ELK(4,4) = ELK(2,2)
C
DO 10 I=1,NN
DO 10 J=I,NN
10 ELK(I,J) = ELK(J,I)
C
C Contribution of the point force to nodal forces
C
XI=XB(N)/SL(N)
SFL1 = 1.0-XI
SFL2 = XI
C
F1=0.5*HF(N)*SL(N)
F3=0.5*HF(N)*SL(N)
ELF(1) = F1*CN1
ELF(2) = F1*SN1
ELF(3) = F3*CN1
ELF(4) = F3*SN1
ELSE
NN=6
IF (NTYPE.EQ.1) THEN
C
The EULER-BERNOULLI FRAME element
C
AMU=0.5*SA(N)*SL(N)*SL(N)/SI(N)
C1=2.0*SE(N)*SI(N)/(SL(N)**3)
C2=6.0*SE(N)*SI(N)/(SL(N)*SL(N))
C3=C1*(AMU*CN2+6.0*SN2)
C4=C1*(AMU-6.0)*CSN
C5=C1*(AMU*SN2+6.0*CN2)
C6=4.0*SE(N)*SI(N)/SL(N)
C
ELK(1,1) = C3
ELK(2,1) = C4
ELK(2,2) = C5
ELK(3,1) = C2*SN1
ELK(3,2) = -C2*CN1
ELK(3,3) = C6
ELK(4,1) = -C3
ELK(4,2) = -C4
ELK(4,3) = -C2*SN1
ELK(4,4) = C3
ELK(5,1) = -C4
ELK(5,2) = -C5
ELK(5,3) = C2*CN1
ELK(5,4) = C4
ELK(5,5) = C5
ELK(6,1) = C2*SN1
ELK(6,2) = -C2*CN1
ELK(6,3) = 0.5*C6
ELK(6,4) = -C2*SN1
ELK(6,5) = C2*CN1
ELK(6,6) = C6
C
DO 20 I=1,NN
DO 20 J=I,NN
20 ELK(I,J) = ELK(J,I)
C
C Contribution of the point force to nodal generalized forces
C
XI=XB(N)/SL(N)
TF=PF(N)*SNT(N)
AF=PF(N)*CNT(N)
SFL1 = 1.0-XI
SFL2 = XI
SFH1 = 1.0 - 3.0*XI*XI + 2.0*(XI**3)
SFH2 = -XI*(1.0+XI*XI-2.0*XI)*SL(N)
SFH3 = 3.0*XI*XI - 2.0*(XI**3)
SFH4 = -XI*(XI*XI - XI)*SL(N)
C
F1=0.5*HF(N)*SL(N) + SFL1*AF
F2=0.5*VF(N)*SL(N) + SFH1*TF
F3=-VF(N)*SL(N)*SL(N)/12.0 + SFH2*TF
F4=0.5*HF(N)*SL(N) + SFL2*AF
F5=0.5*VF(N)*SL(N) + SFH3*TF
F6=VF(N)*SL(N)*SL(N)/12.0 + SFH4*TF

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ELF(1) = F1*CN1-F2*SN1
ELF(2) = F1*SN1+F2*CN1
ELF(3) = F3
ELF(4) = F4*CN1-F5*SN1
ELF(5) = F4*SN1+F5*CN1
ELF(6) = F6
ELSE
C
C      The TIMOSHENKO FRAME element (shear coefficient=5/6)
C
SG=5.0*SE(N)/(1.0+PR(N))/12.0
C1=SA(N)*SE(N)/SL(N)
C2=SG*SA(N)/SL(N)
C3=0.5*SG*SA(N)
C4=0.25*SG*SA(N)*SL(N)
C5=SE(N)*SI(N)/SL(N)
ELK(1,1)=C1
ELK(2,1)=0.0
ELK(2,2)=C2
ELK(3,1)=0.0
ELK(3,2)=-C3
ELK(3,3)=C4+C5
ELK(4,1)=-C1
ELK(4,2)=0.0
ELK(4,3)=0.0
ELK(4,4)=C1
ELK(5,1)=0.0
ELK(5,2)=-C2
ELK(5,3)=C3
ELK(5,4)=0.0
ELK(5,5)=C2
ELK(6,1)=0.0
ELK(6,2)=-C3
ELK(6,3)=C4-C5
ELK(6,4)=0.0
ELK(6,5)=C3
ELK(6,6)=C4+C5
C
DO 25 I=1,NN
DO 25 J=1,NN
TRM(J,I)=0.0
C
25
      TRM(1,1)=CN1
      TRM(1,2)=SN1
      TRM(2,1)=-SN1
      TRM(2,2)=CN1
      TRM(3,3)=1.0
      TRM(4,4)=CN1
      TRM(4,5)=SN1
      TRM(5,4)=-SN1
      TRM(5,5)=CN1
      TRM(6,6)=1.0
C
DO 30 I=1,NN
DO 30 J=I,NN
30      ELK(I,J) = ELK(J,I)
C
DO 40 I=1,NN
DO 40 J=1,NN
TMPK(I,J)=0.0
DO 40 K=1,NN
40      TMPK(I,J)=TMPK(I,J)+TRM(K,I)*ELK(K,J)
C
DO 50 I=1,NN
DO 50 J=1,NN
ELK(I,J)=0.0
DO 50 K=1,NN
50      ELK(I,J)=ELK(I,J)+TMPK(I,K)*TRM(K,J)
C
C      Contribution of the point force to nodal generalized forces
C
XI=XB(N)/SL(N)
TF=PF(N)*SNT(N)
AF=PF(N)*CNT(N)
SFL1 = 1.0-XI
SFL2 = XI

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```

SFQ1 = (1.0-XI)*(1.0-2.0*XI)
SFQ2 = -XI*(1.0-2.0*XI)
SFQ3 = 4.0*XI*(1.0-XI)
C
F1=0.5*HF(N)*SL(N)           + SFL1*AF
F2=0.5*VF(N)*SL(N)           + (SFQ1+0.5*SFQ3)*TF
F3=-VF(N)*SL(N)*SL(N)/12.0   - 0.125*SFQ3*SL(N)*TF
F4=0.5*HF(N)*SL(N)           + SFL2*AF
F5=0.5*VF(N)*SL(N)           + (SFQ2+0.5*SFQ3)*TF
F6=VF(N)*SL(N)*SL(N)/12.0    + 0.125*SFQ3*SL(N)*TF
ELF(1) = F1*CN1-F2*SN1
ELF(2) = F1*SN1+F2*CN1
ELF(3) = F3
ELF(4) = F4*CN1-F5*SN1
ELF(5) = F4*SN1+F5*CN1
ELF(6) = F6
ENDIF
ENDIF
RETURN
END

```