

Rosen, Discrete Mathematics and Its Applications, 8th edition  
Extra Examples  
Section 13.1—Modeling Computation



— Page references correspond to locations of Extra Examples icons in the textbook.

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**p.852, icon at Example 8**

#1. Let  $G = (V, T, S, P)$  be a grammar where  $V = \{S, A, B, a, b\}$  is the vocabulary and  $T = \{a, b\}$  is the set of terminal elements. Determine whether the following set of productions is a:

- (i) a type 0 grammar, but not a type 1 grammar.
- (ii) a type 1 grammar, but not a type 2 grammar.
- (iii) a type 2 grammar, but not a type 3 grammar.

$$S \rightarrow ABA, A \rightarrow bB, B \rightarrow ba.$$

See Solution

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**p.852, icon at Example 8**

#2. Let  $G = (V, T, S, P)$  be a grammar where  $V = \{S, A, B, a, b\}$  is the vocabulary and  $T = \{a, b\}$  is the set of terminal elements. Determine whether the following set of productions is a:

- (i) a type 0 grammar, but not a type 1 grammar.
- (ii) a type 1 grammar, but not a type 2 grammar.
- (iii) a type 2 grammar, but not a type 3 grammar.

$$S \rightarrow AB, B \rightarrow bAa, bAa \rightarrow a.$$

See Solution

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**p.855, icon at Example 13**

**#1.**

- (a) What is the Backus-Naur form of the grammar described as follows:
1. a sentence is made up of a noun phrase followed by a verb phrase or else by a noun phrase followed by a verb phrase followed by a noun phrase.
  2. a noun phrase is made up of a noun, an adjective followed by a noun, or an article followed by a noun.
  3. a verb phrase is made up of a verb.
  4. articles are *a* and *the*.
  5. adjectives are *lengthy*, *boring*, and *inaccurate*.
  6. nouns are *book*, *newspaper*, and *information*.
  7. verbs are *reads* and *contains*.
- (b) Explain how “the newspaper contains lengthy information” can be obtained.

See Solution

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**p.888, icon at Example 3**

**#1.** Let  $G$  be the grammar with Vocabulary  $\{ S, A, a, b \}$ , set of Terminals  $T = \{ a, b \}$ , starting symbol  $S$ , and productions  $P = \{ S \rightarrow aA, S \rightarrow Aab, A \rightarrow aa, A \rightarrow b \}$ . What is  $L(G)$ , the language of this grammar?

See Solution

**p.888, icon at Example 3**

**#2.** Let  $G$  be the grammar with Vocabulary  $\{ S, A, B, a, b \}$ , set of Terminals  $T = \{ a, b \}$ , starting symbol  $S$ , and productions  $P = \{ S \rightarrow bA, S \rightarrow aB, A \rightarrow ba, B \rightarrow ab \}$ . What is  $L(G)$ , the language of this grammar?

See Solution

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**p.888, icon at Example 3**

**#3.** Let  $G$  be the grammar with Vocabulary  $\{ S, A, B, a, b \}$ , set of Terminals  $T = \{ a, b \}$ , starting symbol  $S$ , and productions  $P = \{ S \rightarrow bA, S \rightarrow aB, S \rightarrow AB, A \rightarrow b, B \rightarrow a \}$ . What is  $L(G)$ , the language of this grammar?

See Solution

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Show All Solutions

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Extra Examples

Section 13.3—Finite-State Machines with Output



— Page references correspond to locations of Extra Examples icons in the textbook.

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**p.869, icon at Example 6**

**#1.** Construct a deterministic finite-state automaton that recognizes the set of all bit strings such that the first bit is 0 and all remaining bits are 1's.

See Solution

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**p.869, icon at Example 6**

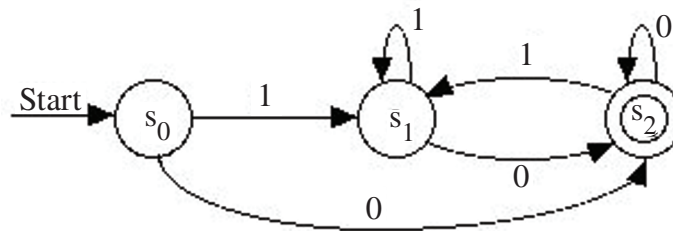
**#2.** Construct a deterministic finite-state automaton that recognizes the set of all bit strings that contain exactly one 0.

See Solution

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p.869, icon at Example 6

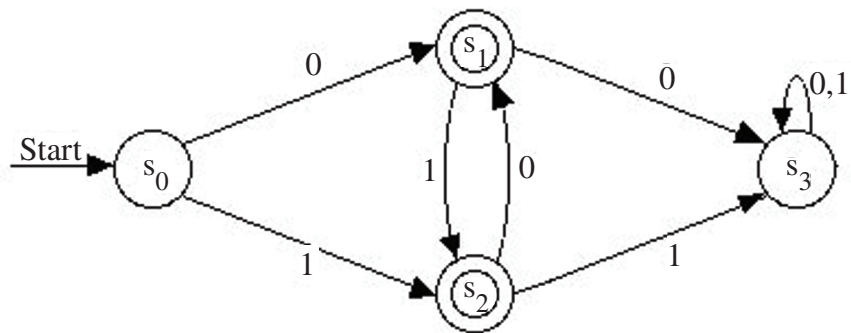
#3. Determine the set of bit strings recognized by the following deterministic finite-state automaton.



See Solution

p.869, icon at Example 6

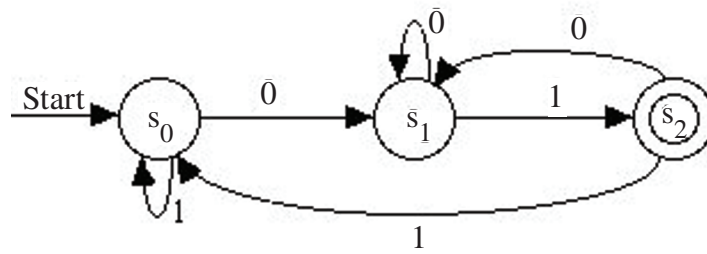
#4. Determine the set of bit strings recognized by the following deterministic finite-state automaton.



See Solution

p.869, icon at Example 6

#5. Determine the set of bit strings recognized by the following deterministic finite-state automaton.



See Solution

Show All Solutions

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Extra Examples

Section 13.5—Turing Machines



— Page references correspond to locations of Extra Examples icons in the textbook.

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**p.889, icon at Example 1**

#1. Let  $T$  be the Turing machine defined by these five-tuples:

$$(s_0, 0, s_1, 1, R), (s_0, 1, s_0, 0, R), (s_0, B, s_1, 0, R), (s_1, 0, s_0, 0, R), (s_1, 1, s_2, 0, R), (s_1, B, s_2, 1, L).$$

If  $T$  is run on the following tape, beginning in initial position, what is the final tape when  $T$  halts?

...	B	B	0	1	B	1	1	B	B	...
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See Solution

**p.889, icon at Example 1**

#2. Let  $T$  be the Turing machine defined by these five-tuples:

$$(s_0, 0, s_1, 1, R), (s_0, 1, s_0, 0, R), (s_0, B, s_1, 0, R), (s_1, 0, s_0, 0, R), (s_1, 1, s_2, 0, R), (s_1, B, s_2, 1, L).$$

If  $T$  is run on the following tape, beginning in initial position, what is the final tape when  $T$  halts?

...	B	B	1	B	0	1	0	B	B	...
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See Solution

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**p.889, icon at Example 1**

**#3.** Let  $T$  be the Turing machine defined by these five-tuples:

$(s_0, 0, s_1, 1, R), (s_0, 1, s_0, 0, R), (s_0, B, s_1, 0, R), (s_1, 0, s_0, 0, R), (s_1, 1, s_2, 0, R), (s_1, B, s_2, 1, L).$

If  $T$  is run on the following tape, beginning in initial position, what is the final tape when  $T$  halts?

...	B	B	0	0	0	1	0	B	B	...
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See Solution

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**p.889, icon at Example 1**

**#4.** Let  $T$  be the Turing machine defined by these five-tuples:

$$(s_0, 0, s_1, 1, R), (s_0, 1, s_0, 0, R), (s_0, B, s_1, 0, R), (s_1, 0, s_0, 0, R), (s_1, 1, s_2, 0, R), (s_1, B, s_2, 1, L).$$

If  $T$  is run on the following tape, beginning with the third blank from the left, what is the final tape when  $T$  halts?

...	B	B	B	B	B	B	B	B	B	...
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[See Solution](#)

